Parallel Performance, Speedup and Efficiency

Mark Greenstreet and Ian M. Mitchell

CpSc 418 - January 24, 2018



Unless otherwise noted or cited, these slides are copyright 2017 by Mark Greenstreet & Ian M. Mitchell and are made available under the terms of the Creative Commons Attribution 4.0 International license http://creativecommons.org/licenses/by/4.0/

Table of Contents



Measuring Performance

- Latency vs. Throughput
- Speedup and Efficiency

2 Amdahl, Gustafson, and Work/Span

3 More Observations about Performance

- Modest Returns
- Super-Linear Speedup
- Embarrassingly Parallel Problems

Objectives

- Compare and contrast common measures of performance:
 - Latency vs. throughput
 - Wall-clock time vs. operation count
- Evaluate quantitative measures of parallel performance:
 - Speedup.
 - Efficiency.
- Explain common observations about parallel performance
 - Amdahl's and Gustafson's laws: Limitations on parallel performance (and how to evade them).
 - The law of modest returns: High complexity problems are bad, and worse on a parallel machine.
 - Superlinear speed-up: More CPUs means more fast memory, and sometimes you win.
 - Embarrassingly parallel problems: Sometimes you win without even trying.

Outline



Measuring Performance

- Latency vs. Throughput
- Speedup and Efficiency

2 Amdahl, Gustafson, and Work/Span

3 More Observations about Performance

- Modest Returns
- Super-Linear Speedup
- Embarrassingly Parallel Problems

Measuring Performance

- The main motivation for parallel programming is performance.
 - Time: make a program run faster.
 - Space: allow a program to run with more memory.
- Two common measures of speed:
 - Latency: time from starting a task until it completes.
 - Throughput: the rate at which tasks are completed.
 - Key observation:

throughput =
$$\frac{1}{latency}$$
, sequential programming
throughput $\geq \frac{1}{latency}$, parallel programming

 High throughput is achieved through pipelining and/or latency hiding (which often increase latency).

Speed Up

• Simple definition:

• We can also describe speedup as how many percent faster:

% faster = (speedup - 1) * 100%

• Efficiency is a related measure of what fraction of the *P* processors are kept busy:

%efficiency = $\frac{speedup}{P} = \frac{time(sequential_execution)}{time(parallel_execution)P}$

- We will focus on speed-up because speed is currently the most common reason for parallelization.
- Efficiency becomes more important when looking at resources other than time, such as energy (next lecture!) or capital cost.

Simple Equation, So Many Interpretations

Simply reporting a speedup number tells us almost nothing.

- Is "time" latency or (inverse of) throughput?
- How big is the problem? Is the same size used for sequential and parallel version?
- What is the sequential version:
 - The parallel code run on one processor?
 - The fastest possible sequential implementation?
 - Something else?
- How are we measuring "time"?

Speedup – Example

- Let's say that count 3s of a million items takes 10ms on a single processor.
- If I run count 3s with four processes on a four CPU machine, and it takes 3.2ms, what is the speedup?
- If I run count 3s with 16 processes on a four CPU machine, and it takes 1.8ms, what is the speedup?
- If I run count 3s with 128 processes on a 32 CPU machine, and it takes 0.28ms, what is the speedup?

Outline



- Latency vs. Throughput
- Speedup and Efficiency

2 Amdahl, Gustafson, and Work/Span

3 More Observations about Performance

- Modest Returns
- Super-Linear Speedup
- Embarrassingly Parallel Problems

Work and Span

- Describe computation as a graph.
 - Vertices correspond to operations.
 - * Which operations should we count?
 - ★ For example, with count 3s, we count the x==3 test and the adds for the tallies.
 - ★ For parallel count 3s, we also count the send and receive operations.
 - Should we count the details of the recursive calls of the count3s (List) function?
 - Equivalently, should we count the operations for setting up and maintaining a loop in an imperative language?
 - Edges represent dependencies
 - * An edge from V_1 to V_2 if V_2 needs the result from V_1 to perform its operation.
- Work: is the total number of vertices. Work corresponds to the sequential execution time.
- Span: is the depth of the tree.
 - Span corresponds to the minimum parallel time.
 - Span ignores communication cost but we could add that by "coloring" vertices.
 - Span still gives us an idea of how parallelizable an algorithm is.

Amdahl's Law

- Given a sequential program where
 - fraction s of the execution time is inherently sequential.
 - fraction 1 s of the execution time benefits perfectly from speedup.
- The run-time on P processors is:

$$T_{parallel} = T_{sequential} * (s + \frac{1-s}{P})$$

- Consequences:
 - Define

$$speedup = rac{T_{sequential}}{T_{parallel}}$$

- speedup on *P* processors is at most $\frac{1}{s}$.
- Gene Amdahl argued in 1967 that this limit means that parallel computers are only useful for a few special applications where *s* is very small.

Amdahl's Law



• See also MRR Figure 2.5 (and Figure 2.6 for equivalent efficiency plots).

Greenstreet & Mitchell

Amdahl's Law, 50 years later

Amdahl's "law" is a mathematical theorem, not a physical law.

Amdahl's is also an economic observation.

- Amdahl's law was formulated when CPUs were expensive.
- Today, CPUs are cheap!
 - The cost of fabricating eight cores on a die is very little more that the cost of fabricating one.
 - MRR argues that per-core performance grows as

 $\sqrt{\text{#transistors}}$.

- Adding cores can be a better use of transistors than trying to improve single processor performance.
- Computer cost is dominated by the rest of the system: memory, disk, network, monitor, ...

Gustafson's Law

Amdahl's law assumes a fixed problem size.

- Gustafson observed in 1988 that when more powerful computers are available, the users solve bigger problems.
 - Many computations have s (sequential fraction) that decreases as N (problem size) increases.
- Examples:
 - Scientific computing.
 - Animation, games and multi-media.
 - Data science and data mining of massive data sets.
- Having lots of cheap CPUs available will
 - Change our ideas of what computations are easy and what are hard.
 - Determine what the next generation of "killer-apps" will be.

Gustafson's Law



• Example: Speedup of a problem where parallel work grows as $N^{3/2}$ and sequential work as log *P*.

Greenstreet & Mitchell

Speedup

Outline



Latency vs. Throughput

Speedup and Efficiency

2 Amdahl, Gustafson, and Work/Span

3 More Observations about Performance

- Modest Returns
- Super-Linear Speedup
- Embarrassingly Parallel Problems

The Law of Modest Returns

More bad news. 🔅

- Let's say we have an algorithm with a sequential run-time
 - $T = (12ns)N^4$.
 - If we're willing to wait for one hour for it to run, what's the largest value of N we can use?
 - If we have 10000 machines, and perfect speedup (i.e. speedup = 10000), now what is the largest value of N we can use?
 - What if the run-time is (5ns)1.2^N?
- Parallelism offers modest returns unless the problem is of fairly low complexity.
- But:
 - Sometimes, modest returns are good enough: weather forecasting, climate models.
 - Sometimes, problems have huge N and low complexity: data mining, graphics, machine learning.

Super-Linear Speedup

Sometimes, speedup > P. ©

- But if that is true, wouldn't the best sequential algorithm be to simulate *P* workers by time-sharing a single processor?
 - Probably not: Time-sharing has overhead.
- Memory: a common explanation
 - P machines have more main memory (DRAM)
 - and more cache memory and registers (total)
 - and more I/O bandwidth, ...
- Multi-threading: another common explanation
 - The sequential algorithm cannot full utilize each CPU's parallel capabilities.
 - A parallel algorithm can make better use through, for example, latency hiding.
- Algorithmic advantages: Some problems are naturally parallel.

BUT: be skeptical, especially if speedup $\gg P$.

Embarrassingly Parallel Problems

Problems that can be solved by a large number of processors with very little communication or coordination.

- Rendering images for computer-animation: each frame is independent of all the others.
- Brute-force searches for cryptography.
- Analyzing large collections of images: astronomy surveys, facial recognition, ...
- Monte-Carlo simulations: same model, run with different random values.
- Don't be ashamed if your code is embarrassingly parallel:
 - Embarrassingly parallel problems are great: you can get excellent performance without heroic efforts.
 - The only thing to be embarrassed about is if you don't take advantage of easy parallelism when it is available.

Summary

- Speed-up is sequential time divided by parallel time.
 - Simple definition, can be messy in practice.
 - How do we measure "time" latency, throughput, throughput under deadline, some other measure?
 - What is the sequential time? Best algorithm? What if the program cannot run on one machine?
- Modeling performance
 - Amdahl's law: what if some fixed fraction of the computation is non-parallelizable?
 - Gustafson's law: what if the overhead grows slower that the amount of parallel work as the problem size grows?
 - Work-Span: a graph model that unifies these models.
- Other issues:
 - Super-linear speed-up: usually because more machines have more memory.
 - Embarrassingly parallel problems:
 - * Sometimes task are (very nearly) independent.
 - ★ This is great don't be ashamed of an embarrassingly parallel problem.
 - The law of modest returns
 - * Parallel computing is not a panacea for high computational complexity problems.

Preview

January 26: Energy, Power, and Time	
January 29: Performance Loss	
Reading:	McCool et al., Chapter 2, Section 2.6.
Homework:	HW 2 earlybird (11:59pm), HW 3 goes out.
January 31: Parallel Performance: Models	
Homework:	HW 2 due (11:59pm).
February 2-9: Sorting	
February 13: Tuesday – Mark's office hours	
Homework:	HW 3 earlybird (11:59pm).
	HW 4 goes out – midterm review, maybe some simple CUDA
February 14: Intro. to GPUs & CUDA	
Homework:	HW 3 due (11:59pm).
February 16: A CUDA example	
February 19-23: break week	
February 28: midterm	

Review Questions

- What is speedup? Give an intuitive, English answer and a mathematical formula.
- Why can it be difficult to determine the sequential time for a program when measuring speedup?
- What is Amdahl's law? Give a mathematical formula. Why is Amdahl's law a concern when developing parallel applications? Why in many cases is it not a show-stopper?
- Is parallelism an effective solution to problems with high big-O complexity? Why or why not?
- What is super-linear speedup? Describe two causes.
- What is an embarrassingly parallel problem? Give an example.