20 points. Please submit your solution using the handin program. Submit your solution as cs418 mini3
Your submission should consist of the one file called mini3.erl or mini3.txt sepending on which problem you choose to solve.

Submit a solution to any one of the three questions below.

1. Erlang Review Let LL be a list-of-lists.
(a) (5 points) Write an Erlang function, is lol ( X ) that returns true iff X is a list and every element of X is a list. Note that is_lol([]) $\rightarrow$ true because [] is a list and every element of [] (there aren't any) is a list as well.
(b) (5 points) Write an Erlang function, is_rect ( X ) that returns true iff X is a list and all elements of X are lists of the same length.
(c) (10 points) Write an Erlang function, transpose (X) such that

- transpose([]) -> [];
- If $X$ is a list where every element of $X$ is the empty list, then transposeX $->$ [];
- If is_rect ( X ), X is non-empty, and the elements of X are non-empty lists, let $\mathrm{N} 1=$ length $(\mathrm{X})$, and $\mathrm{N} 2=$ length (hd $(\mathrm{X})$ ). Then, transposeX $->$ Y where is_rect $(\mathrm{Y})$, length $(\mathrm{Y})=:=$ N2, every element of $Y$ is a list of length N1, and lists:nth(I, lists:nth(J, Y)) =:= lists:nth(J, lists:nth(I, X)) for all $0<I=<N 1$ and $0<J=<N 2$.
- If not is_rect (X) then transpose (X) fails with an error.

Note: I will not ask you to write this much code on the midterm. OTOH, I might state a similar problem, write a partial solution, and ask you to fill-in 3-5 lines.
2. Reduce and/or Scan Let

```
goodness([]) -> 0;
goodness([good | Tl]) -> 1 + goodness(Tl);
goodness([bad | Tl]) -> -1 + goodness(Tl);
goodness([_ | Tl]) -> goodness(Tl);
```

(a) ( $\mathbf{1 0}$ points) Write a function, stop_while_your_ahead (List) that returns $\{\mathrm{I}, \mathrm{G}\}$ where $0=<\mathrm{I}=<$ length(List) maximizes $G=$ goodness (element(1, lists:split(I, List))). If there's a tie, return the smallest such I.
(b) $\mathbf{1 0}$ points Use wtree : reduce to write
stop_while_your_ahead_par ( $W$, Key) that returns $\{I, G\}$ as above for the list associated with Key that is distributed across the workers of codeW.
3. Speed-Up Consider a problem that can be executed sequentially in time $(20 \mathrm{~ns}) * N \log _{2} N$, where $N$ is the size of the input problem. A parallel implementation with $P$ processors takes time:

$$
(20 \mathrm{~ns}) * \frac{N}{P} \log _{2}\left(\frac{N}{P}\right)+\left(10 \mathrm{~ns} * \frac{N}{P}+\lambda\right) \log _{2}(P)\left(\log _{2}(P)+1\right) / 2
$$

Where $\lambda$ is the cost of a communication action. For this problem, assume $\lambda=5 \mu \mathrm{~s}$.
(a) (10 points) Plot speed-up as a function of $P$ for $P$ chosen from $4,16,64$, and 256 , and for $N$ chosen from $2^{10}$, $2^{20}$, and $2^{30}$.
(b) (10 points) How large must $N$ be to get a speed-up of at least $P / 2$ for each of the values of $P$ suggested above? You only need to consider power-of-two values for $N$, but you do need to consider powers of two other than the ones listed for part a.

## Why?

Review for the midterm.

