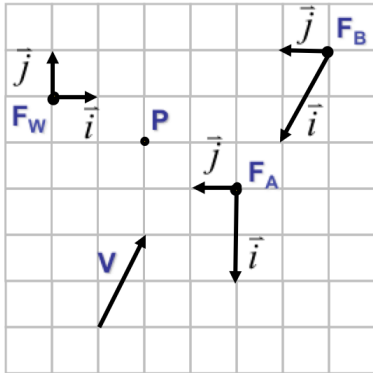


## 1. Coordinate Frames



$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix}_W = \begin{bmatrix} 0 & -1 & 4 \\ -2 & 0 & -2 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}_A$$

$$\begin{bmatrix} x \\ y \\ 1 \end{bmatrix}_A = \begin{bmatrix} 1 & 0 & -1.5 \\ 1 & 1 & -2 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}_B$$

- (a) (3 points) Express point
- $P$
- in each of the three coordinate frames.

$$P_W(2, -1) \quad P_A(-0.5, 2) \quad P_B(1, 3)$$

- (b) (3 points) Express
- vector
- $V$
- in each of the three coordinate frames.

$$V_W(1, 2) \quad V_A(-1, -1) \quad V_B(-1, 0)$$

- (c) (2 points) Find the
- $3 \times 3$
- homogeneous transformation matrix which takes a point from
- $F_A$
- and expresses it in terms of
- $F_W$
- . I.e., determine
- $M$
- , where
- $P_W = MP_A$
- .

see above

- (d) (2 points) Find the
- $3 \times 3$
- homogeneous transformation matrix which takes a point from
- $F_B$
- and expresses it in terms of
- $F_A$
- . I.e., determine
- $M$
- , where
- $P_A = MP_B$
- .

see above