## Rendering



## OpenGL Rendering Pipeline <br> (with some details abstracted away)

Javascript, three.js


## Thus far...

- triangles
- vertices: $\mathrm{v}=[\mathrm{xyz}]^{\top}$ local coords, on GPU
- vertex shader: $v^{\prime}=\mathrm{M} v$ to image coords
- fragment shader: colour $=(1,0,0)$

$$
\text { colour }=N \cdot \mathrm{~L}
$$

- instancing: redraw with $M_{1}, M_{2}, M_{3}, \ldots$
- many coordinate frames:
e.g., wheel $\rightarrow$ car $\rightarrow$ world $\rightarrow$ camera $\rightarrow$ image


## Algorithm: "Projective Rendering"

for each frame
clear screen
for each object instance for each triangle j // project onto image: transform vertices // vertex shader for each pixel in j // rasterization compute colour // fragment shader

## Linear Algebra Review

## vectors

dot product

## Math Review

## matrix-vector multiplication

(a)as dot products with the rows
(b) as weighted combinations of the columns

## Math Review

## Cross Product



## Right Handed Coordinate System

(curl fingers from $\mathbf{u}$ to $\mathbf{v}$; thumb points to $u \times v$ )

## Math Review

## Coordinate Systems

## Right-handed Coordinate System


using right-hand rule

Left-handed Coordinate System

using left-hand rule

## Math Review

## Points and Vectors


vector space
vectors are invariant under translation

## affine space:

allows vector-to-point addition

## Math Review

## Coordinate System vs Frame


coordinate system: frame:

## Math Review

## Working with Frames



$$
\begin{aligned}
& P=O+x \vec{i}+y \vec{j} \\
& \mathrm{~F}_{1} \\
& \mathrm{~F}_{2} \\
& \mathrm{~F}_{3} \\
& \mathrm{~F}_{4}
\end{aligned}
$$

## Many Coordinate Frames in a Scene

(and using transformation matrices to move between them)

