# CPSC 314 <br> Assignment 3 

Due Wednesday Nov 9th, 2016, in class

Answer the questions in the spaces provided on the question sheets. If you run out of space for an answer, use separate pages and staple them to your assignment.

Name: $\qquad$

Student Number: $\qquad$

| Question 1 | $/ 5$ |
| :--- | ---: |
| Question 2 | $/ 9$ |
| Question 3 | $/ 10$ |
| Question 4 | $/ 6$ |
| TOTAL | $/ 49$ |

1. (5 points) Scan Conversion

Give the pseudocode for scan converting the region shown to the right.

It is the portion of the circle on the right side of the line defined by fixed points $c=$ $(1,0)$ and $d=(2,2)$. The circle is centered at $\left(x_{o}, y_{o}\right)$ and has radius $r$. Use implicit equations to develop your solution.
2. (9 points) Interpolation

A triangle has device coordinates $P_{1}=(1,4), P_{2}=(9,2)$, and $P_{3}=(7,9)$. You wish to interpolate a value $v$ for point $P=(7,5)$, given the value of $v$ at the vertices:
$v_{1}=2, v_{2}=6, v_{3}=5$.
(a) (1 point) Sketch the triangle and the point $P$ (this drawing will help you further down).
(b) (4 points) Derive a plane equation for $v$ as a function of $x$ and $y$, i.e. $A x+B y+C v+$ $D=0$. To do this, determine the constraints based on the given triangle points and their respective values $v_{i}$. You can use Matlab or an online linear solver to solve a set of linear equations for your plane parameters. Write down your derived equation. Compute the value $v$ for the point $P$ using the plane equation.
(c) (4 points) Compute the barycentric coordinates for point $P$. Compute $v$ for point $P$ using the Barycentric coordinates.
3. (10 points) Clipping

Suppose that a perspective view-volume is defined by
near $=-1$, far $=-10$, bottom $=-5$, top $=5$, left $=-10$, right $=10$.
Consider the triangle defined by the view coordinate frame coordinates

$$
P_{1}=(0,2,-3), \quad P_{2}=(30,-10,-4), \quad P_{3}=(0,30,-4) .
$$

(a) (3 points) Sketch a side-view and top-view of the view-volume and the triangle.
(b) (3 points) Determine if view-frustum culling should be applied to the triangle, i.e., if any vertices are "outside" with respect to any one of the six view frustum planes. Use the implicit plane equation

$$
A x+B y+C z+D=0
$$

Hint: remember what we discussed in class about plane equation and its sign.
Hint 2: If you find you have to do a lot of tedious calculations, think more.
(c) (1 point) Based on your work for the question above, determine the view-frustum planes that the triangle intersects.
(d) (3 points) Compute the final clipped polygon of the triangle in VCS. Show your work.
4. (6 points) Local Illumination

Sketch the illumination for the following scene when computed using the Phong illumination model. The scene is viewed from above using an orthographic projection and is lit by the single light source L. Draw 4 curves (overlay these in the graph below), one for each of ambient, diffuse, specular, and total illumination. The Phong illumination model is given by:

$$
I=k_{a} I_{a}+k_{d} I_{d}(N \cdot L)+k_{s} I_{s}(R \cdot V)^{n}
$$

with the following values:

$$
I_{a}=I_{d}=I_{s}=1.0, k_{a}=0.2, k_{d}=0.8, k_{s}=0.8, n=10
$$

Hint: it may be useful to draw vertical lines marking critical points the surface. We do not expect numerically accurate plots, but do expose the characteristics of the curves.


