



## Chapter 7

### Illumination Models & Shading




## Shading Models


- Realistic interaction of light and objects
  - Simulate physical phenomena
- Fast - Fake it!!!
  - Ignore real physics, approximate the look
- Physically based reflection models
  - BRDFs: Bidirectional Reflection Distribution Functions



## Photorealistic Illumination



77 K polygons  
24 area lights  
solution render time : around 7200 sec

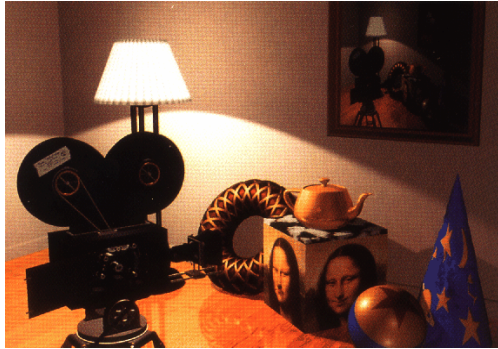


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[electricimage.com]



## Local vs. Global Illumination Models

- Local model - interaction of each object with light
- Global model: interactions between objects



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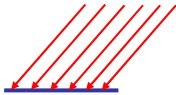
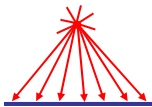
## Fast Local Illumination



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## Light Sources


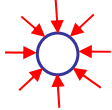
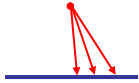
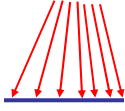
- Point source
  - light originates at a point
  - Rays hit planar surface at different angles
- Parallel source
  - light rays are parallel
  - Rays hit a planar surface at identical angles
  - May be modeled as point source at infinity
  - *Directional light*



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## Light Sources


- Area source
  - Light originates at finite area in space.
  - In-between point and parallel sources
- spotlights
  - position, direction, angle
- ambient light (environment light)



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## Light Sources - OpenGL



- Specify parameters  
`glLightfv(GL_LIGHTi, GL_POSITION, light[])`  
i – between 0 & 8 (or more)
- Directional  $[x \ y \ z \ 0]$
- Point source  $[x \ y \ z \ 1]$
- Spotlight has extra parameters:
  - `GL_SPOT_DIRECTION`, `GL_SPOT_EXPONENT`, `GL_SPOT_CUTOFF`
- Area source – too complex for projective pipeline (e.g. OpenGL)



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## Ambient Light


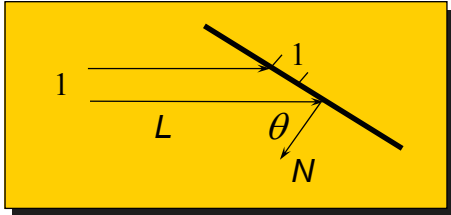
- non-directional light – environment light
- Object illuminated with same light everywhere
  - Looks like silhouette
- Illumination equation  $I = I_a k_a$ 
  - $I_a$  - ambient light intensity
  - $k_a$  - fraction of this light reflected from surface
  - Defines object color



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## Diffuse Light


- Dull surfaces - such as solid matte plastic- reflect uniformly in all directions
- This is called diffuse or Lambertian reflection
- For light source normalized direction  $L$  & surface with normal  $N$  reflected light is proportional to  $LN$




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## Diffuse Reflection

- Illumination equation is now:
$$I = I_a k_a + I_p k_d (N \cdot L) = I_a k_a + I_p k_d \cos \theta$$
- $I_p$  - point source's intensity
- $k_d$  - surface diffuse reflection coefficient



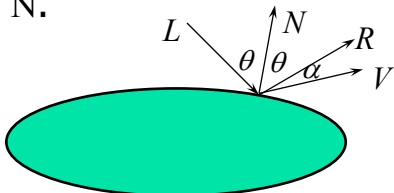
- Can we locate light source from shading?




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## Specular Reflection

- Shiny objects (e.g. metallic) reflect light in preferred direction  $R$  determined by surface normal  $N$ .



- Most objects are not ideal mirrors - reflect in the immediate vicinity of  $R$



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## Specular

Phong Model (Phong Bui-Tuong, 1975)

- Assume exponential attenuation of form  $\cos^n \alpha$
- Computing reflection direction  $R$  of  $L$ 
  - $N$  and  $L$  are unit length!

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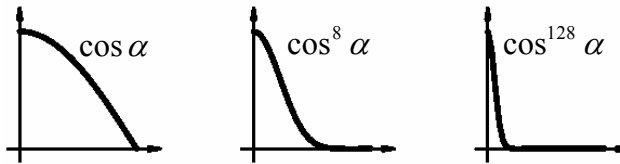
## Specular Reflection (Phong Model)

- Illumination equation:
$$I = I_a k_a + I_p (k_d (N \cdot L) + k_s (R \cdot V)^n)$$
  - $k_s$  - Specular reflection coefficient
  - $n$  - Specularity exponent



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## Specular Reflection (cont'd)

- Exponent  $n$  of cosine controls concentration of *attenuation* function:

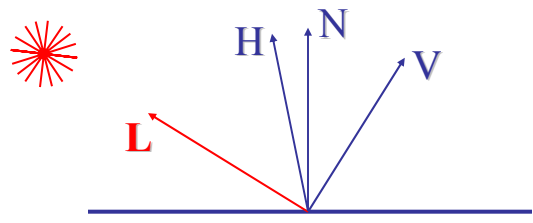



- No physical basis BUT looks good

## Specular

- Blinn-Phong model (Jim Blinn, 1977)
  - Variation with better physical interpretation
    - $H$ : halfway vector;  $n$ : shininess

$$I_{out}(\mathbf{x}) = k_s \cdot (H \cdot N)^n \cdot I_{in}(\mathbf{x}); \text{ with } H = (L + V) / 2$$






## ■ Illumination Equation


- For multiple light sources:

$$I = I_a k_a + \sum_p \frac{I_p}{d_p} (k_d (N \cdot L_p) + k_s (R_p \cdot V)^n)$$

- $d_p$  - distance between surface and light source + distance between surface and viewer (Heuristic atmospheric attenuation)
- Other attenuations: e.g. quadratic




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## ■ Lighting in OpenGL

- Light source: amount of RGB light emitted
  - value represents percentage of full intensity, e.g., (1.0,0.5,0.5)
  - every light source emits ambient, diffuse, and specular light
- Materials: amount of RGB light reflected
  - value represents percentage reflected e.g., (0.0,1.0,0.5)




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## In OpenGL

- $k_a, k_d, k_s$  - surface color (RGB)
- Modify by `glMaterialfv(GL_FRONT_AND_BACK, pname, RGB[])`
- `pname` - `GL_AMBIENT`, `GL_DIFFUSE`, `GL_SPECULAR`
- Light source properties (also RGB)  
`glLightfv(GL_LIGHTi, pname, light[])`




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## Lighting in OpenGL

```
glLightfv(GL_LIGHT0, GL_AMBIENT, amb_light_rgba );
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif_light_rgba );
glLightfv(GL_LIGHT0, GL_SPECULAR, spec_light_rgba );
glLightfv(GL_LIGHT0, GL_POSITION, position);
glEnable(GL_LIGHT0);


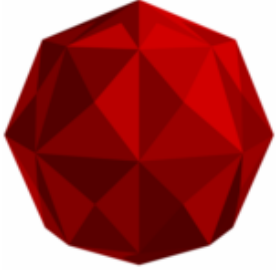
glMaterialfv( GL_FRONT, GL_AMBIENT, ambient_rgba );
glMaterialfv( GL_FRONT, GL_DIFFUSE, diffuse_rgba );
glMaterialfv( GL_FRONT, GL_SPECULAR, specular_rgba );
glMaterialfv( GL_FRONT, GL_SHININESS, n );
```



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## Flat Shading


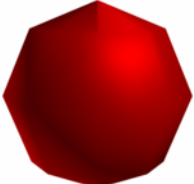
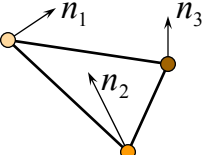
- Illumination value depends only on polygon normal
  - each polygon colored with uniform intensity
- Not adequate for polygons approximating smooth surface
- Looks non-smooth
  - worsened by Mach bands effect



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## Gourard Shading

- Polyhedron - approximation of smooth surface
  - Assign to each vertex normal of original surface at point
  - If surface not available use estimate normal
- Compute illumination intensity at vertices using those normals
- Linearly interpolate vertex intensities over interior pixels of polygon projector



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## Gourard Shading (cont'd)

$c_4 = \alpha_1 c_1 + (1 - \alpha_1) c_2$

$c_5 = \alpha_2 c_1 + (1 - \alpha_2) c_3$

scanline  $Y=y$

$(x, y)$

$c_2$

$c_3$

$c(x, y) = \alpha_3 c_4 + (1 - \alpha_3) c_5$

- Assign pixel color during scan conversion
- Can Gourard shading support specular reflection ?

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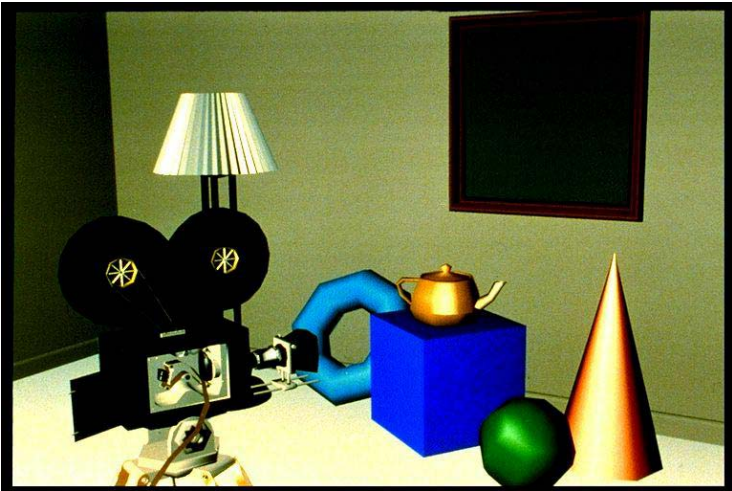
## Flat Shading

- Example:

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## Gouraud Shading

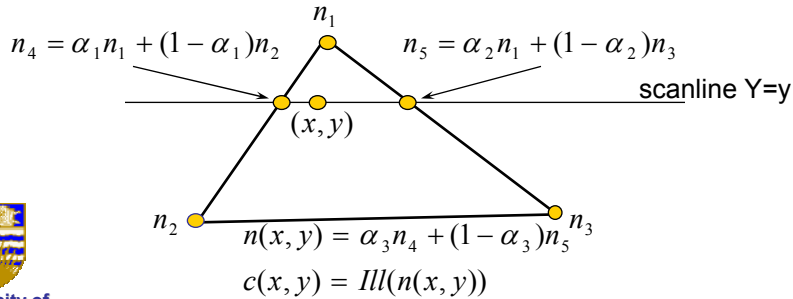
- Example:



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## Phong Shading

- Interpolate (in image space) normal vectors instead of intensities
- Apply illumination equation for each interior pixel with its own normal



$$n_4 = \alpha_1 n_1 + (1 - \alpha_1) n_2$$

$$n_5 = \alpha_2 n_1 + (1 - \alpha_2) n_3$$


$$n(x, y) = \alpha_3 n_4 + (1 - \alpha_3) n_5$$

$$c(x, y) = Ill(n(x, y))$$


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## Shading

- Phong shading is clearly more expensive (why ?)- but well worth the effort
- Can achieve specular effects
- Both Gourard & Phong schemes are performed in the image plane  $\Rightarrow$  view dependent
- Can cause artifacts during animation




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## Materials

- Bi-directional Reflectance Distribution Function (BRDF):
  - Describes fraction of light reflected for all combinations of incoming (light) and outgoing (viewing) directions
  - Color channels (R, G, B) are treated separately
    - Actually: wavelengths (see later in course)



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## Materials

- Bi-directional Reflectance Distribution Function (BRDF):

$$I_{out}(\mathbf{x}) = f_r(\phi_{in}, \theta_{in}, \phi_{out}, \theta_{out}) \cdot I'_{in}(\mathbf{x})$$

$$= f_r(\mathbf{l} \rightarrow \mathbf{v}) \cdot (\mathbf{n} \cdot \mathbf{l}) \cdot I_{in}(\mathbf{x})$$

- $f_r(\mathbf{l} \rightarrow \mathbf{v})$  is called *BRDF*
- $(\mathbf{t}, \mathbf{n}, \mathbf{b})$  is *local coordinate frame* (normal, tangent, binormal)

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## Materials

- Polar plot of BRDF
  - Fix incoming light direction  $\mathbf{l}$
  - Plot  $f_r(\mathbf{l} \rightarrow \mathbf{v}) \cdot \mathbf{v}$  for all viewing directions  $\mathbf{v}$
  - Works for 2D and 3D plots
  - Example: 2D polar plot for diffuse BRDF

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