This exam has 5 questions, for a total of 27 points.
1. (5 points) Scan Conversion

Write the pseudocode needed to scan-convert the given shape below. Use implicit functions for lines and circles to construct your solution. Use `setPixel(x, y)` to set a given pixel “on”. 

![Diagram of a circle with center (x_c, y_c) and radius r]
2. Barycentric coordinates

Consider the triangle vertices with device coordinates $P_1(0,0)$, $P_2(100,0)$, $P_3(0,100)$, which also have the associated attribute values $v_1 = 10$, $v_2 = 0$, $v_3 = 20$. Assume that the barycentric coordinates are modeled according to: $P = \alpha P_1 + \beta P_2 + \gamma P_3$.

(a) (0 points) Sketch the triangle in the space above.

(b) (2 points) Sketch three lines that correspond to $\beta = 0$, $0.5$, $1$.

(c) (1 point) Give $\alpha, \beta, \gamma$ for point $P_2$. Give $\alpha, \beta, \gamma$ for the point $P(50,50)$.

(d) (1 point) Give the interpolated value of $v$ for point $P$ specified by $\beta = 0.2$ and $\gamma = 0.3$.

(e) (1 point) Give the expression to compute $\beta$ for the given triangle, i.e., $\beta(x, y)$.

(f) (1 point) For what kind of 3D triangles would normal barycentric interpolation yield the same result as perspective-correct interpolation?
3. Clipping and Culling

Consider the viewing frustum shown below. Assume that all the labeled edges represent faces of solid objects. Consider back-face culling and view-frustum culling as happening independently of each other.

(a) (2 points) In alphabetical order, list the faces that would be removed by back-face culling.

(b) (2 points) In alphabetical order, list the faces that would be removed by view-frustum culling.

(c) (1 point) After view-frustum culling and back-face culling, which remaining faces would be completely removed by z-buffer tests?

(d) (1 point) Consider a detailed model of a statue that consists of a million triangles that will not be visible on screen because it is occluded by another object. Briefly describe how an occlusion culling test could be performed for the object, therefore avoiding the need to transform and render all its triangles.

(e) (1 point) At what point does the line $P_A(1, 1, 1)P_B(6, 5, -2)$ intersect the plane given by $x + 2y + z - 9 = 0$?
4. Texture Mapping

Consider the texture map below, which is to be mapped to Objects A and B. Assume that the REPEAT texture mode is being used.

(a) (2 points) In the Object A diagram above, sketch the image that would appear for Object A for the assigned texture coordinates.

(b) (2 points) In the Object B diagram above, assign texture coordinates to Object B so that it would yield the given image.

(c) (1 point) Why are texture coordinates defined using normalized coordinates, i.e., \( u, b \in [0, 1] \), as opposed to directly using the pixel coordinates of the texture map?

5. Short answer

(a) (1 point) Where clipping can clipping be done? Circle any of: VCS CCS NDCS

(b) (1 point) Where can back-face culling be done? Circle any of: VCS NDCS

(c) (1 point) If points are transformed using \( P' = MP \), how should normals be transformed?

(d) (1 point) The effective ability of the z-buffer to distinguish which of two objects is “in front” is worse when those objects are close to the back of the viewing frustum. Circle one of: True False