## Ray-Tracing



Figure 1: Reflection test: (left) with environment map. (right) with environment map and ray-traced interreflections.
[Pixar: Ray Tracing for the Movie 'Cars' http://graphies.pixar.com/library/RayTracingCars/paper.polf ]

## Ray-tracing Overview

- handles multiple inter-reflections of light
- partly physics-based: geometric optics
- well suited to transparent and reflective objects

Trace light path from the eye backwards(!) into the scene; recursively apply to reflected and refracted rays.


## Ray-Tracing

```
raytrace( ray ) {
    find closest intersection: P
    colour_local = (0,0,0);
    if visible(P,L) // cast shadow ray
        colour_local = Phong(N,L,rayDir)
    colour_reflect = raytrace(reflected_ray ) // if reflective
    colour_refract = raytrace(refracted_ray ) // if refractive
    colour = k1*colour_local +
        k2*colour_reflect +
        k3*colour_refract
    return( colour)
}
```

- "raycasting" : only cast first ray from eye

Ray Tree

$S=$ shadow ray
$R=$ reflected ray
$T=$ transmitted ray (refracted)


## Ray termination

- ray hits a diffuse object
- ray exits the scene
- when exceeding max recursion depth
- when final contribution will be too small


## Generation of Rays

- distance to image plane: $d$
- image resolution (in pixels): $N_{x}, N_{y}$
- image plane dimensions: left,right,top,bot
- pixel $i, j$

$$
\begin{aligned}
& P_{0,0}=C+d \vec{w}+\text { left } \vec{u}+\text { bot } \vec{v} \\
& P_{i, j}=P_{0,0}+i \Delta u \vec{u}+j \Delta v \vec{v}
\end{aligned}
$$

where

$$
\begin{aligned}
& \Delta u=(\text { right }- \text { left }) / N_{x} \\
& \Delta v=(\text { top }- \text { bot }) / N_{y}
\end{aligned}
$$



## Ray-Sphere Intersections

Ray

Sphere

$$
\begin{aligned}
\mathrm{R}_{i, j}(t) & =C+t \cdot\left(P_{i, j}\right. \\
& =C+t \cdot \mathbf{v}_{i, j}
\end{aligned}
$$

$$
F(x, y, z)=r^{2}-\left((x)-S_{x}\right)^{2}-(\underbrace{z(t)=C_{z}+V_{z} t}_{\left.\left.(y)-S_{y}\right)^{2}-(z)-S_{z}\right)^{2}}
$$ $\Rightarrow$ quadratic equation in $t$



## Ray-Tracing: Optimizations

- process rays in parallel (multi-core, GPU, $\cdots$ )
- efficient ray-object culling
- hierarchical bounding volumes


Ray-Triangle Intersections
(covered as Q4 of 14)

