CPSC 314 Assignment 2 Theory

due: Monday, January 30, 2017, 11:59pm Worth 5% of your final grade.

Note: this version has corrections to Q2 and Q3, as posted on Piazza.

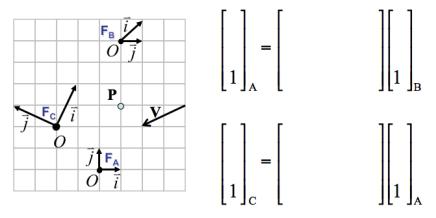
Answer the questions in the spaces provided on the question sheets.

Name: _

Student Number: _____

Question 1	/ 15
Question 2	/ 8
Question 3	/ 9
Question 4	/ 11
Question 5	/ 4
TOTAL	/ 47

1. Transformations as a change of coordinate frame

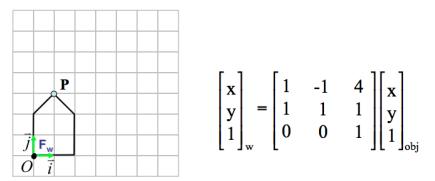


- (a) (3 points) Express the coordinates of point P with respect to coordinate frames A, B, and C.
- (b) (3 points) Express the coordinates of vector V with respect to coordinate frames A, B, and C.

- (c) (3 points) Fill in the 2D transformation matrix that takes points from F_B to F_A , as given to the right of the above figure.
- (d) (3 points) Fill in the 2D transformation matrix that takes points from F_A to F_C , as given to the right of the above figure. Hint: You might first want to determine what combination of i_C and j_C are needed to reproduce $5i_A$ and $5j_A$.
- (e) (3 points) Using your answers for the above two matrices, develop a 2D transformation matrix that takes points from F_B to F_C . Test your solution using point P.

Assignment 2

2. Interpreting a Matrix Transformation



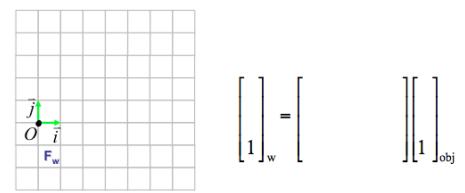
- (a) (2 points) On the above diagram, sketch the origin and basis vectors of the coordinate frame F_{obj} that results from the given transformation matrix.
- (b) (2 points) The drawing of the above house represents its untransformed shape. Sketch the transformed version of the house in the above diagram.
- (c) (2 points) Given $M = Translate(a, b, 0)Rotate(z, \theta)Scale(c, c, c)$, provide the values of a, b, c and θ that would implement the given transformation.

(d) (2 points) Given $M = Rotate(z, \theta)Translate(a, b, 0)Scale(c, c, c)$, provide the values of a, b, c and θ that would implement the given transformation.

Assignment 2

CPSC 314

3. Composing Transformations



(a) (3 points) Consider a house in the xy-plane, defined by the coordinates (0,0), (2,0), (2,2), (1,3), 0,2). Assume z = 0 for all vertices.
Sketch the house resulting from the following transformations. Assume that the matrix M is initialised to the identity matrix.
M.identity();

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M.ruentity(),
M.translate(5,-1,0);
M.rotate(90, 0,0,1);
M.scale(2,1,1);
M.translate(1,0,0);
drawHouse();
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(b) (3 points) Give the resulting 4×4 transformation matrix, M.

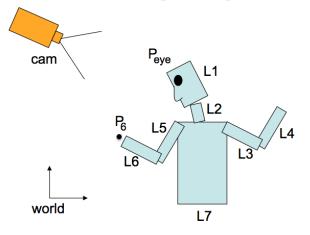
(c) (3 points) What values would need to be assigned to theta, a, b, c, d, e, f
in order for the following transformations to yield an identical final transformation?
M.identity();
M.rotate(theta, 0,0,1);
M.translate(a,b,c);
M.scale(d,e,f);
drawHouse();

Assignment 2

4. Scene Graphs

CPSC 314

(a) (3 points) Sketch a scene graph for the scene below. Use directed edges, i.e., arrows, to represent transformations that connect the nodes in the graph. Label each edge with a unique name, M_n , which indicates the transformation matrix that takes points from the frame F_n (for link Ln) to its parent frame. Use the world coordinate frame as the root note of the scene graph. Assume that the body (L7) and the camera are positioned relative to the world frame. Assume that all other parts are defined relative to their proximal parent links, i.e., the links closer to the body.



- (b) (2 points) Give an expression for the composite transformation that would be used when drawing point P_6 , as defined in frame F_6 for link L6. i.e., it should transform point P_6 to the camera coordinate frame. Your answer should be expressed as a product of the matrices used to label your scene graph.
- (c) (2 points) Give an expression for the composite transformation that transforms point, P_6 , as defined in frame F_6 , to the head coordinate frame, F_1 . Your answer should be expressed as a product of the matrices used to label your scene graph.

CPSC 314

- (d) (2 points) Give an expression for the opposite transformation, i.e., one that transforms a point, P_1 , in the head coordinate frame, F_1 , to the coordinate frame F_6 .
- (e) (2 points) Give the value of the matrix M_4 that is implemented by the code below, i.e., the relative transformation of L4 with respect to L3.

// implement M4: transformation of L4 relative to L3
M.translate(4,0,0); // translate in x
M.rotate(90,0,0,1); // rotate by 90 degrees around z
DrawL4();

Give all the elements of the implemented matrix M_4 .

5. (4 points) Viewing Transformation

Determine the viewing transformation, M_{view} , that takes points from WCS (world coordinates) to VCS (viewing or camera coordinates), for the following camera parameters: $P_{eye} = (-50, 20, 20), P_{ref} = (0, 20, 20), V_{up} = (1, 0, 1)$. There is no need to numerically invert any matrices, i.e., it is ok to specify $M_{view} = M_{cam}^{-1}$.