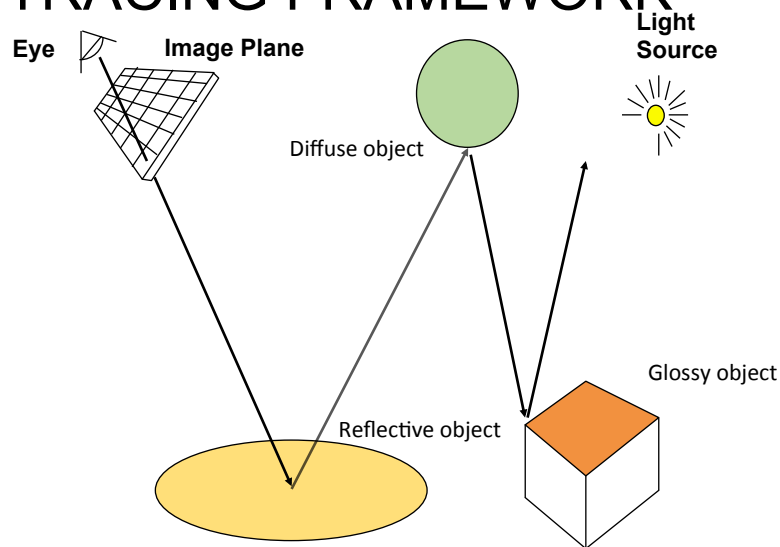
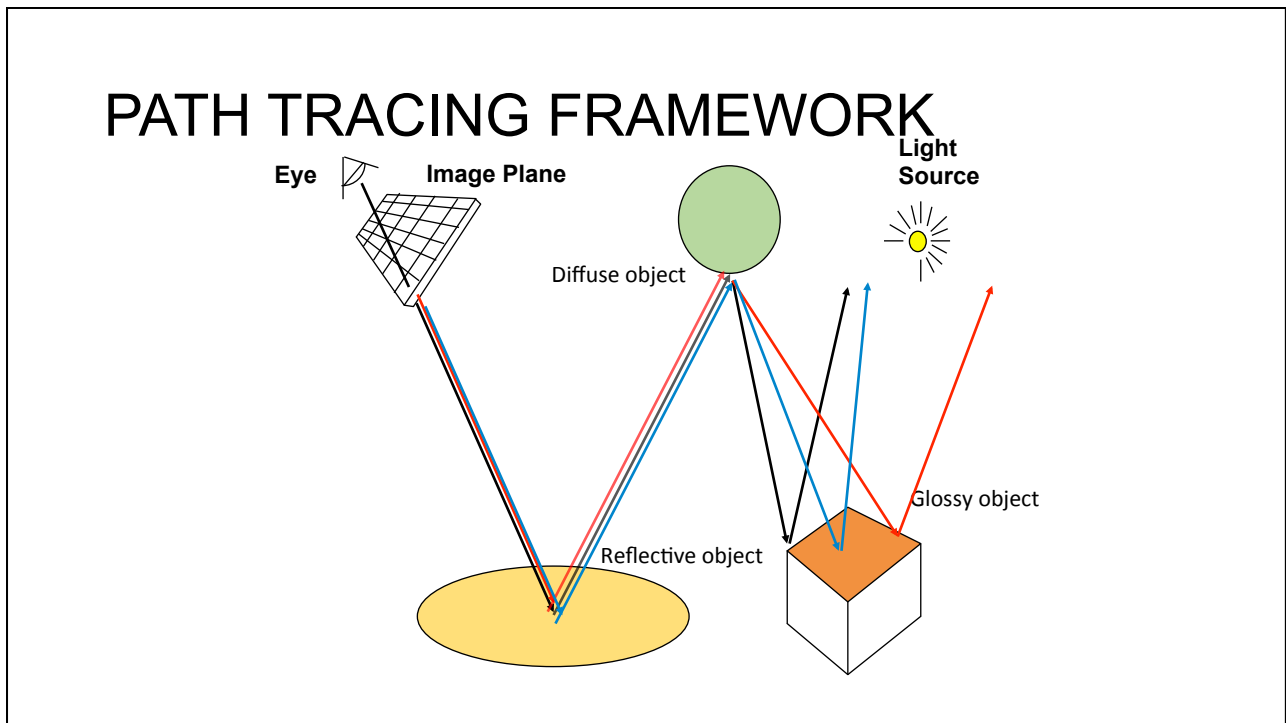
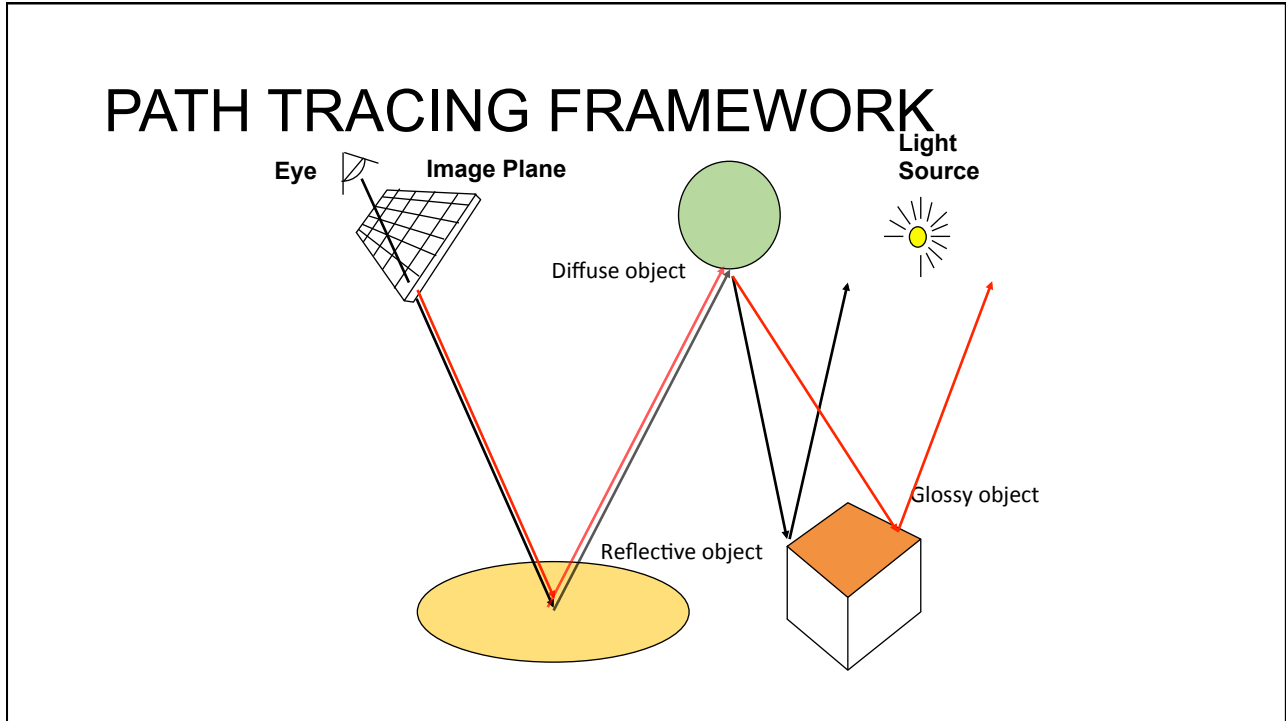


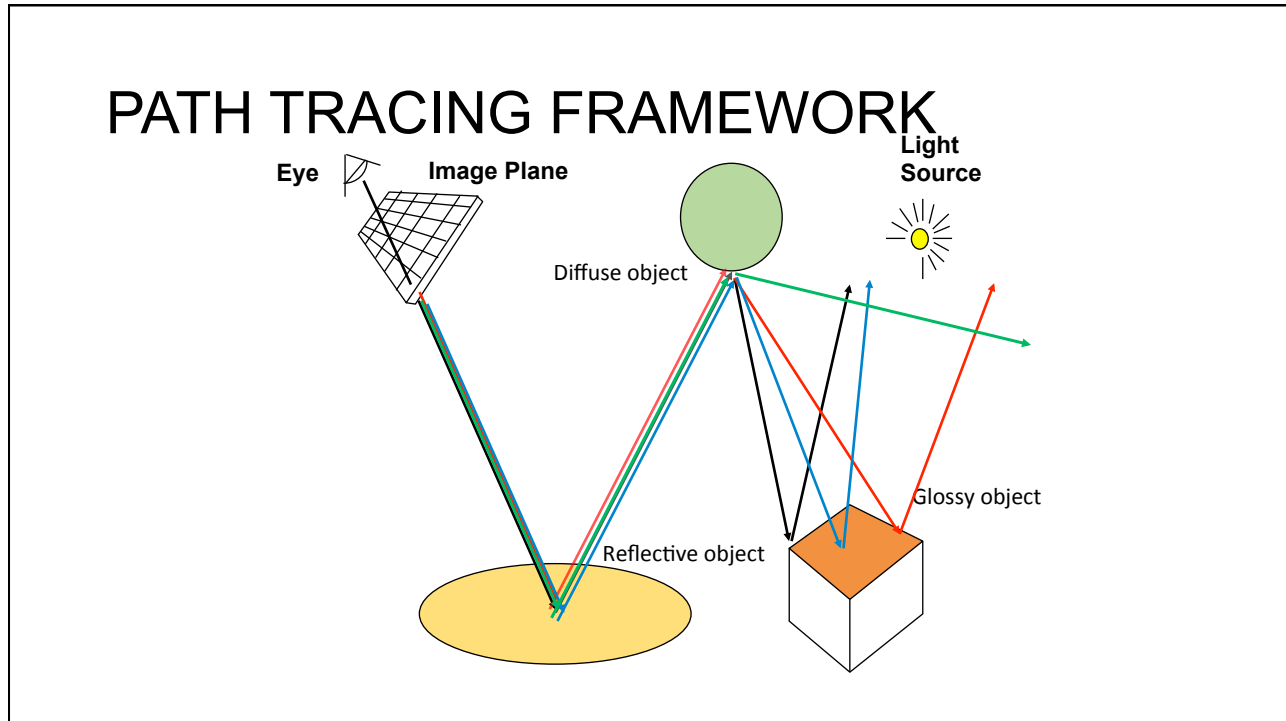
RAY TRACING LIMITATION

- Only specular reflections consider other objects
 - Well okay, refractions too
- Diffuse and glossy surfaces will only reflect light source!
- We're using Lambert and Phong models of **direct illumination**
- How can we model diffuse/glossy models in a similar way?

PATH TRACING FRAMEWORK







PATH TRACING ALGORITHM

1. Shoot a ray through pixel (i,j) . Set *attenuation* to 1.0.
2. Find the closest intersection of the ray with an object
3. Randomly choose between “*emission*” and “*reflection*”
 - a. If “*emission*”, return **emissionColor**;
 - b. If “*reflection*”,
 - Reflect a ray in a random direction
 - rayWeight *= reflectance;
 - Go to 2.

SIMPLEST PATH TRACER

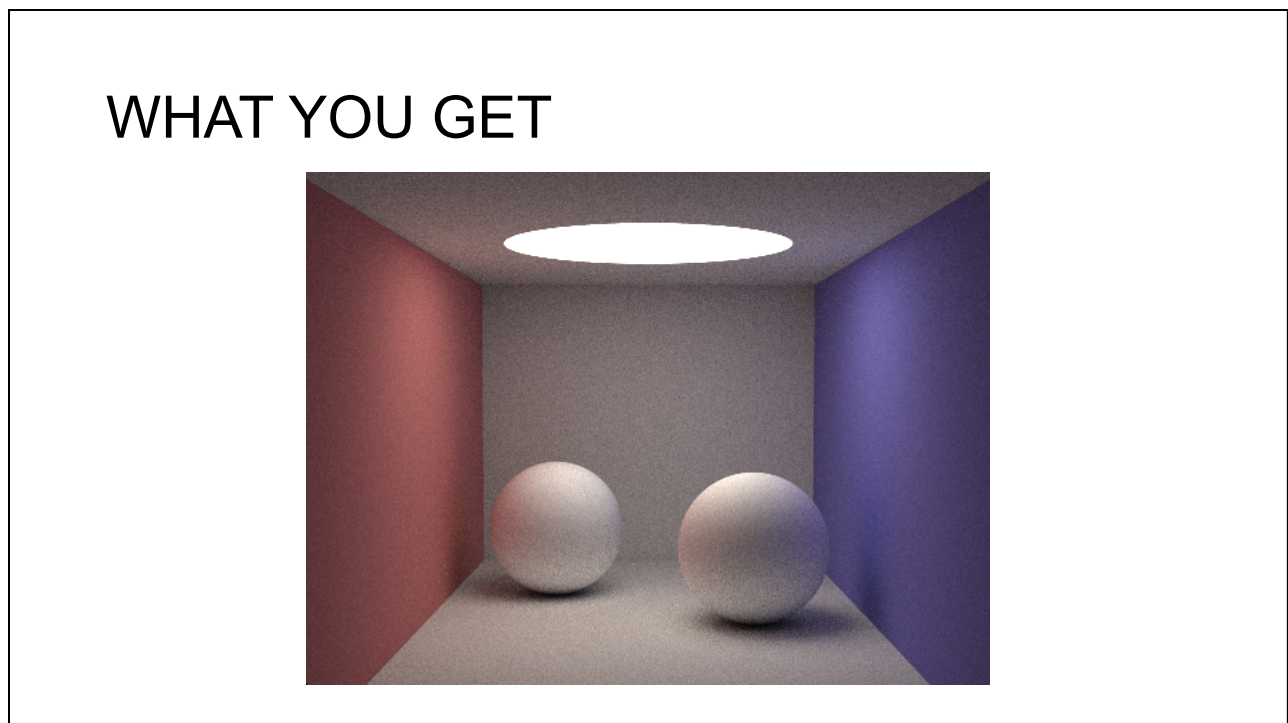
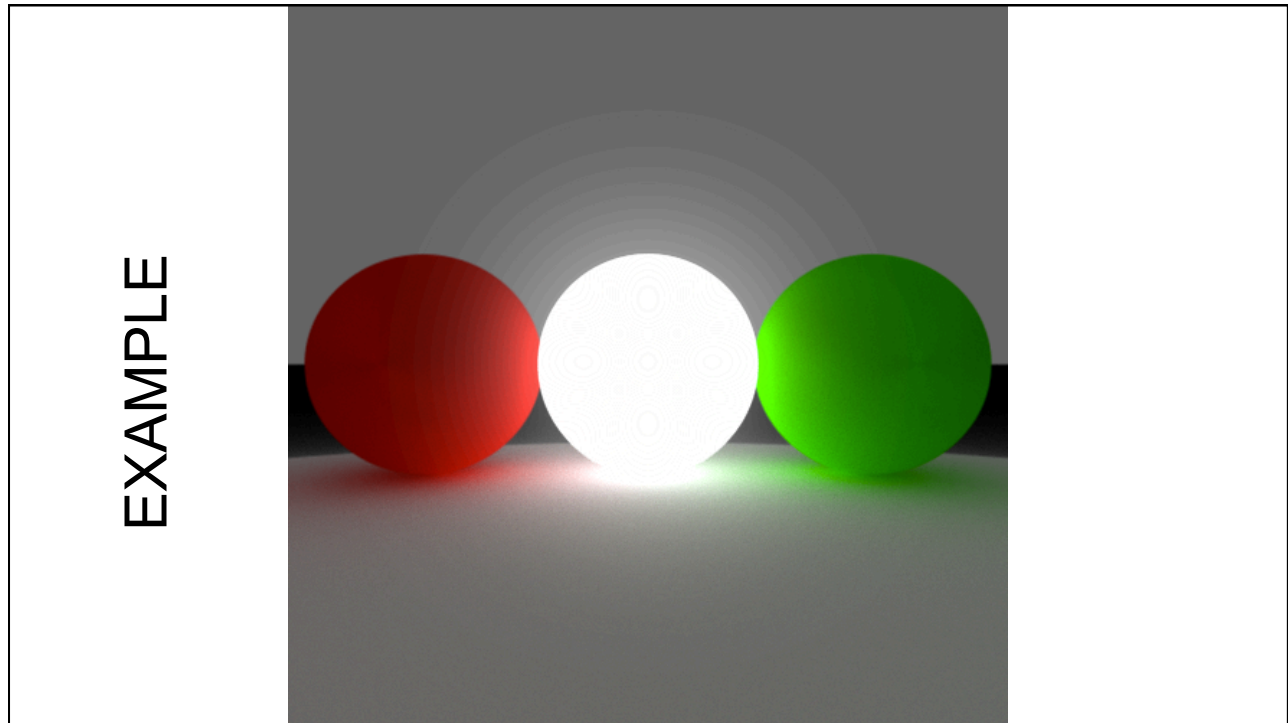
- For all pixels (i,j):
 - Ray r = generateRay (i,j);
 - For k=1,...,N:
 - PixelColor(i,j) += pathTrace(r)/N;

SIMPLEST PATH TRACER

```

PathTrace(Ray r) {
  P = closestIntersection(r);
  if (random(emit, reflect) == emit)
    return EmissionColor;
  else {
    Ray v = {intersectionPt,
             randomDirectionInHemisphere(r.normalWhereObjWasHit)};
    double cos_theta = dot(v.direction, r.normalWhereObjWasHit);
    return PathTrace(v)*cos_theta*reflectance;
  }
}

```

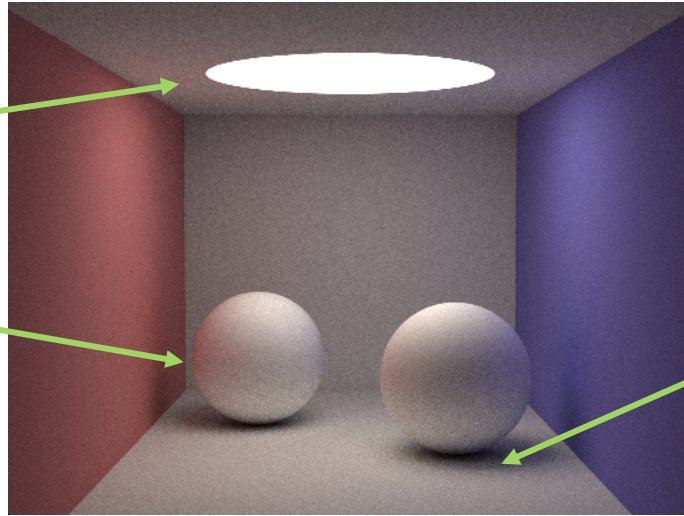


WHAT YOU GET

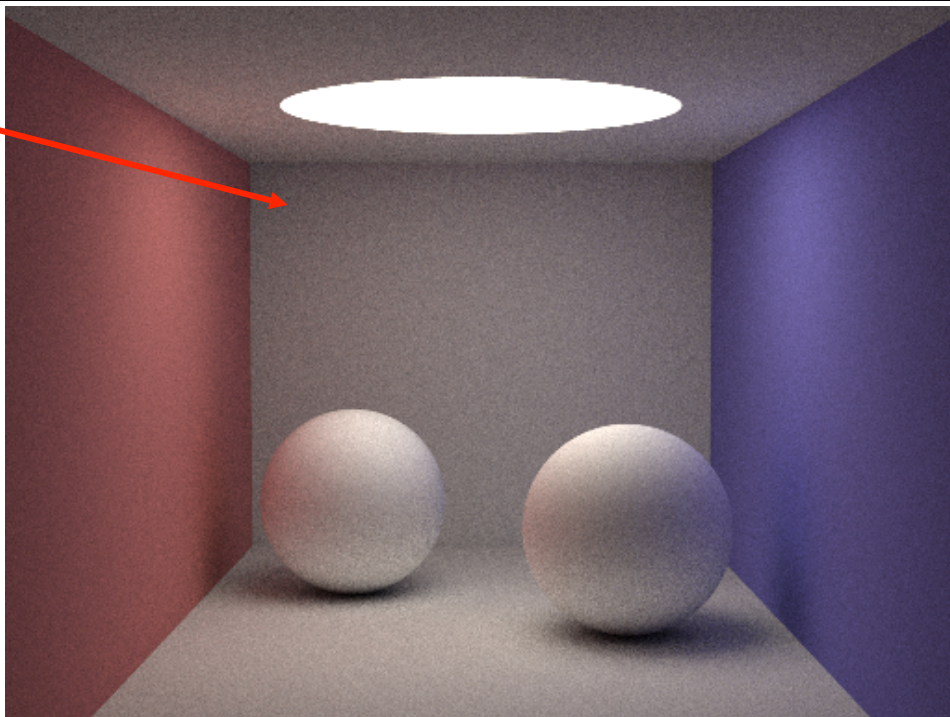
Area light

Reflections from
diffuse objects
'color bleeding'

Soft shadows



Noise

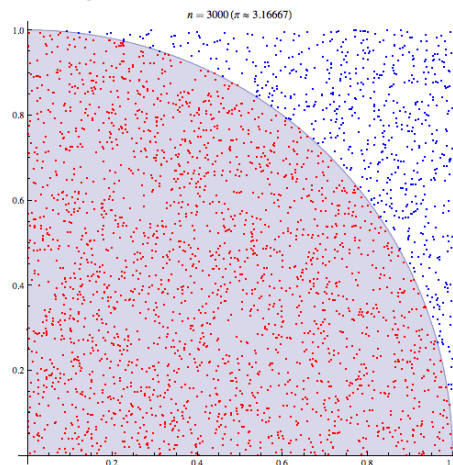


MONTE CARLO METHODS

- General idea: compute something using random sampling
- Used for computing integrals of complex functions
- E.g. areas or volumes
 - If it's hard to compute analytically
 - But easy to test if a point is inside
- If we throw enough random samples, by the law of large numbers, mean \sim empirical mean

MONTE CARLO METHODS

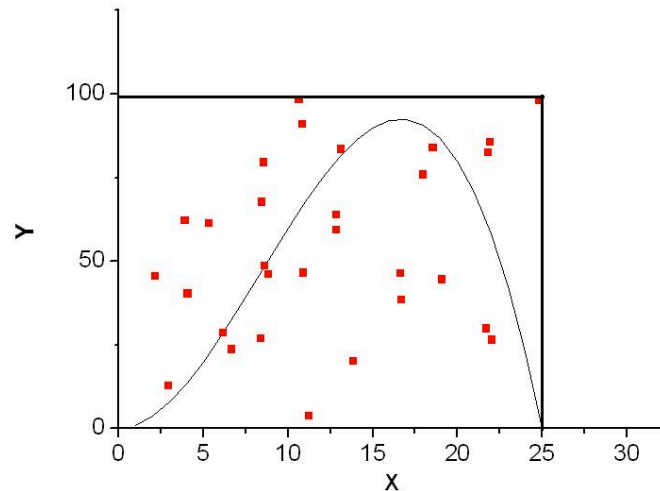
- Example: approximating π :



"Pi 30K" by CaitlinJo - Own work. This mathematical image was created with Mathematica. Licensed under CC BY 3.0 via Commons - https://commons.wikimedia.org/wiki/File:Pi_30K.gif#/media/File:Pi_30K.gif

MONTE CARLO METHODS

- Example: computing a weird integral



"Pi 30K" by CaitlinJo - Own
commons.wikimedia.org/wiki/File:Pi_30K.gif#/media/File:Pi_30K.gif

Commons - <https://>

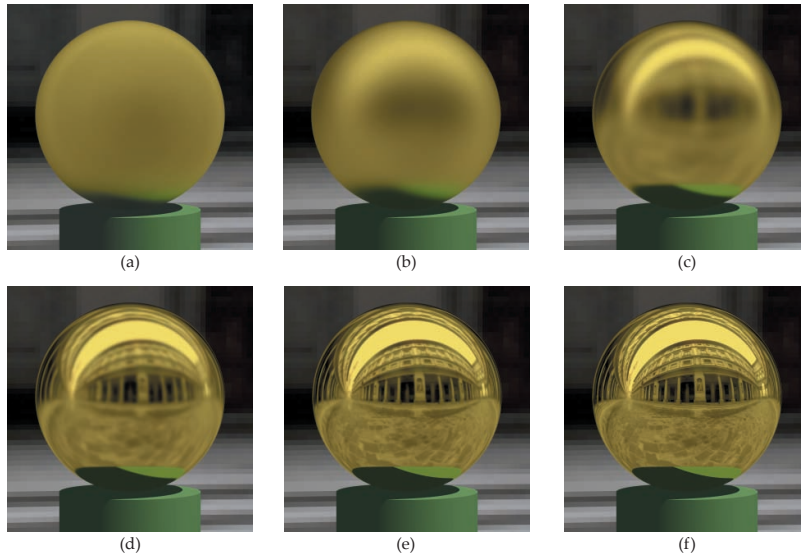
MONTE-CARLO: RAY TRACING

- Now in RAY tracing, we can generate rays randomly from an area light source
- Instead of shooting a single shadow ray,
 - Generate many randomly towards a light source
 - Generate a point on the light source
 - Shoot a ray towards that point
 - Average their contribution
- Soft shadows in RAY tracing!

SIMPLEST PATH TRACER

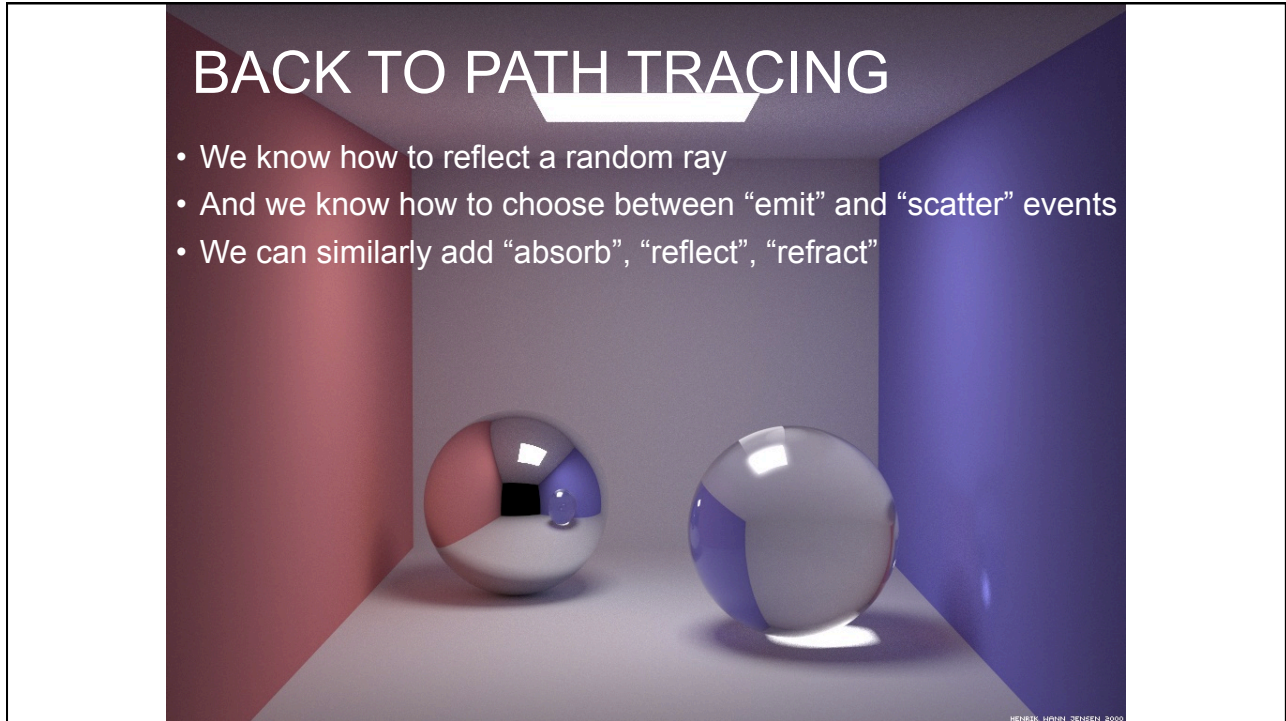
```
PathTrace(Ray r) {  
    P = closestIntersection(r);  
    if (random(emit, reflect) == emit)  
        return EmissionColor;  
    else {  
        Ray v = {intersectionPt,  
                randomDirectionInHemisphere(r.normalWhereObjWasHit)};  
        double cos_theta = dot(v.direction, r.normalWhereObjWasHit);  
        return PathTrace(v)*cos_theta*reflectance;  
    }  
}
```

HOW TO GENERATE REFLECTION FOR A GLOSSY SURFACE



BACK TO PATH TRACING

- We know how to reflect a random ray
- And we know how to choose between “emit” and “scatter” events
- We can similarly add “absorb”, “reflect”, “refract”



RAY TRACING VS PATH TRACING

- Global illumination algorithms
- Rays emitted FROM camera
- Ray Tracing
 - Single ray per pixel
 - Supports indirect lighting only from specular surfaces
 - No color bleeding
 - Shoots shadow rays to compute direct illumination
 - Soft shadows are harder to get
- Path Tracing (*may produce renders indistinguishable from photos*)
 - Many rays per pixel, their color averaged
 - At each interaction, ray direction changes randomly with some distribution
 - No difference between light sources and objects
 - Soft shadows, complex materials, etc.
 - Supports all sorts of indirect lighting