

Name: \_\_\_\_\_  
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① Compute the following, where:  $M = \begin{bmatrix} 2 & 5 & 1 \\ 1 & 3 & 0 \\ 0 & -2 & -1 \end{bmatrix}$   $a = \begin{bmatrix} 0 \\ 3 \\ 1 \end{bmatrix}$   $b = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$

(a)  $Ma = \begin{bmatrix} 16 \\ 9 \\ -7 \end{bmatrix}$

(b)  $(M \cdot M)a = \begin{bmatrix} 70 \\ 43 \\ -11 \end{bmatrix}$

(c)  $(a^T M^T)(Ma)^T = a^T M^T = [16 \ 9 \ -7]$

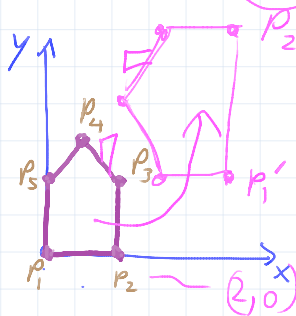
(d)  $a^T b = [ \quad ] [ \quad ] = 9$

(e)  $a \cdot b = 9$

(f)  $ab = [ \quad ] [ \quad ]$  non sense

② Transform the vertices of the following object (a house) using

$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 0 & -1 & 5 \\ 2 & 0 & 2 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$  and then draw the transformed object.



$P_1' = (5, 2)$

$P_2' = (5, 6)$

1 grid cell = 1 unit

③ Give three ways in which one might "multiply" two vectors,

$a \in \mathbb{R}^3, b \in \mathbb{R}^3$  e.g.,  $a = \begin{bmatrix} 1 \\ 2 \\ 4 \end{bmatrix}, b = \begin{bmatrix} -2 \\ 1 \\ 3 \end{bmatrix}$

$a \cdot b$  scalar  
 $a \times b$  vector  
 $a \cdot b^T$  matrix  
 $b \cdot a^T$  matrix