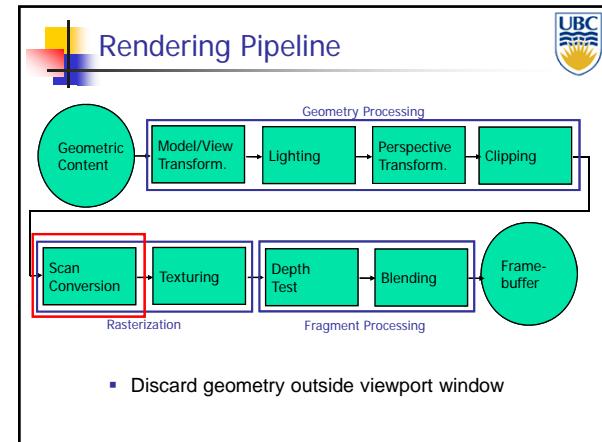


# Computer Graphics

## Scan Conversion

### Chapter 8

Scan Conversion – Drawing on Raster Display (part 1 – Lines)

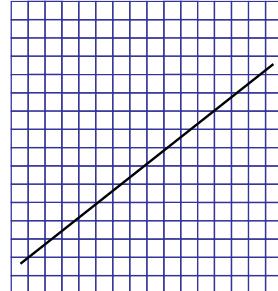


### Scan Conversion - Rasterization

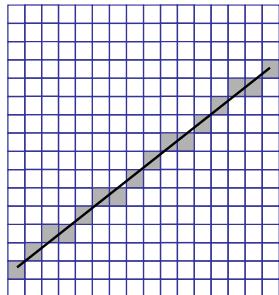
Convert continuous rendering primitives into discrete fragments/pixels

- Lines
  - Basic (explicit)
  - Bresenham (Midpoint)
- Triangles
  - Implicit formulation
  - Scanline
- Interpolation

### Scan Conversion - Lines



### Scan Conversion - Lines



### Idea: Use Explicit Line Formula

Explicit - one coordinate as function of the others

$$y = f(x)$$

$$z = f(x, y)$$

line  $y = mx + b$

$$y = \frac{(y_2 - y_1)}{(x_2 - x_1)}(x - x_1) + y_1$$

Typically separate into 4 (or 8) cases (why?)

# Computer Graphics

## Scan Conversion

### Basic Line Drawing

Assume  $x_1 < x_2$  & line slope absolute value is  $\leq 1$

```

Line ( x1, y1, x2, y2 )
begin
float dx, dy, x, y, slope ;
dx = x2 - x1;
dy = y2 - y1;
slope = dy/dx;
y = y1;
for x from x1 to x2 do
begin
PlotPixel ( x, Round ( y ) );
y = y + slope;
end;
end;

```

**Questions:**  
Can this algorithm use integer arithmetic?

### Midpoint (Bresenham) Algorithm

- Key Observation 1:**
  - At each step have ONLY 2 choices
    - East/North-East

### Midpoint (Bresenham) Algorithm

- Key Observation 2:**
  - Can decide based on whether midpoint is above/below line
  - How?
    - Evaluate implicit line equation at  $(x+1, y+1/2)$

### Bresenham Algorithm

Implicit formulation = distance (up to scale)

$$d = \{(x, y) | ax + by + c = xdy - ydx + c = 0\}$$

$$d(x, y) = 2(xdy - ydx + c)$$

- Given point  $P = (x, y), d(x, y)$  is signed distance of  $P$  to  $\tau$  (up to scale)
- $d$  is zero for  $P \in \tau$

### Bresenham (Midpoint) Algorithm

- Starting point satisfies  $d(x<sub>1</sub>, y<sub>1</sub>) = 0$
- Each step moves right (east) or upper right (northeast)
- Sign of  $d(x + 1; y + 1/2)$  indicates if to move east or northeast

### Bresenham (Midpoint) Algorithm

```

Line ( x1, y1, x2, y2 )
begin
int x, y, dx, dy, d;
x = x1; y = y1;
dx = x2 - x1; dy = y2 - y1;
PlotPixel ( x, y );
while ( x < x2 ) do
  d = (2x + 2)dy - (2y + 1)dx + 2c; // 2((x + 1)dy - (y + .5)dx + c)
  if ( d < 0 ) then
    begin
      x = x + 1;
    end;
  else begin
      x = x + 1;
      y = y + 1;
    end;
  PlotPixel ( x, y );
end;

```

# Computer Graphics

# Scan Conversion

## Bresenham (Midpoint) Algorithm

UBC Logo

- Insanely efficient version (less computations inside the loop)
  - compute d incrementally
- At  $(x_1, y_1)$   
 $d_{start} = d(x_1 + 1, y_1 + \frac{1}{2}) = 2dy - dx$
- Increment in  $d$  (after each step)
  - If move east  $\Delta_e = d(x + 2, y + \frac{1}{2}) - d(x + 1, y + \frac{1}{2}) = 2((x + 2)dy - (y + \frac{1}{2})dx + c) - 2((x + 1)dy - (y + \frac{1}{2})dx + c) = 2dy$
  - If move northeast  $\Delta_{ne} = d(x_1 + 2, y_1 + \frac{3}{2}) - d(x_1 + 1, y_1 + \frac{1}{2}) = 2((x + 2)dy - (y + \frac{3}{2})dx + c) - 2((x + 1)dy - (y + \frac{1}{2})dx + c) = 2(dy - dx)$

## Bresenham (Midpoint) Algorithm

UBC Logo

```

Line ( x1, y1, x2, y2 )
begin
    int x, y, dx, dy, d, Δx, Δw ;
    x <= x1 ; y <= y1 ;
    dx <= x2 - x1 ; dy <= y2 - y1 ;
    d <= 2 * dy - dx ;
    Δx <= 2 * dy ; Δw <= 2 * (dy - dx) ;
    PlotPixel ( x, y ) ;
    while ( x < x2 ) do
        if ( d < 0 ) then
            begin
                d <= d + Δx ;
                x <= x + 1 ;
            end ;
        else begin
            d <= d + Δw ;
            x <= x + 1 ;
            y <= y + 1 ;
        end ;
        PlotPixel ( x, y ) ;
    end ;
end ;

```

## Bresenham Examples

UBC Logo

- Intensity depends on angle

- Comment: extends to higher order curves – e.g. circles

## Comparison: float/integer

UBC Logo

Assume  $x_1 < x_2$  & line slope is  $\leq 1$

```

Line ( x1, y1, x2, y2 )
begin
    int x, y, dx, dy, d, Δx, Δw ;
    x <= x1 ; y <= y1 ;
    dx <= x2 - x1 ; dy <= y2 - y1 ;
    d <= 2 * dy - dx ;
    Δx <= 2 * dy ; Δw <= 2 * (dy - dx) ;
    PlotPixel ( x, y ) ;
    while ( x < x2 ) do
        if ( d < 0 ) then
            begin
                d <= d + Δx ;
            end ;
        else begin
            d <= d + Δw ;
            y <= y + 1 ;
        end ;
        x <= x + 1 ;
        PlotPixel ( x, y ) ;
    end ;
end ;

```

## Implicit test

UBC Logo

- Instead of clipping line in continuous space
  - For each integer value of  $(x, y)$  test if inside window just before drawing
  - Inefficient on CPU
  - On a parallel (GPU) processor can be surprisingly fast

```

Line ( x1, y1, x2, y2 )
begin
    float dx, dy, x, y, slope ;
    dx <= x2 - x1 ;
    dy <= y2 - y1 ;
    slope <= dy / dx ;
    y <= y1 ;
    for x from x1 to x2 do
        begin
            y_int = Round ( y ) ;
            if inside (x, y_int) PlotPixel ( x, y_int ) ;
            y <= y + slope ;
        end ;
    end ;

```

## Scan Conversion of Lines

UBC Logo

### Discussion

- Integer: Bresenham
  - Good for hardware implementations (integer)!
- Floating Point
  - May be faster for software (depends on system)!
  - Easier to parallelize