




## Lighting/Shading




- Goal
  - Model the interaction of light with surfaces to render realistic images
  - Generate per (pixel/vertex) color




## Factors





- Light sources
  - Location, type & color
- Surface materials
  - How surfaces reflect light
- Transport of light
  - How light moves in a scene
- Viewer position




## Illumination Models/Algorithms






- Local illumination - Fast
  - Ignore real physics, approximate the look
  - Interaction of each object with light
    - Compute on surface (light to viewer)
- Global illumination – Slow
  - Physically based
  - Interactions between objects

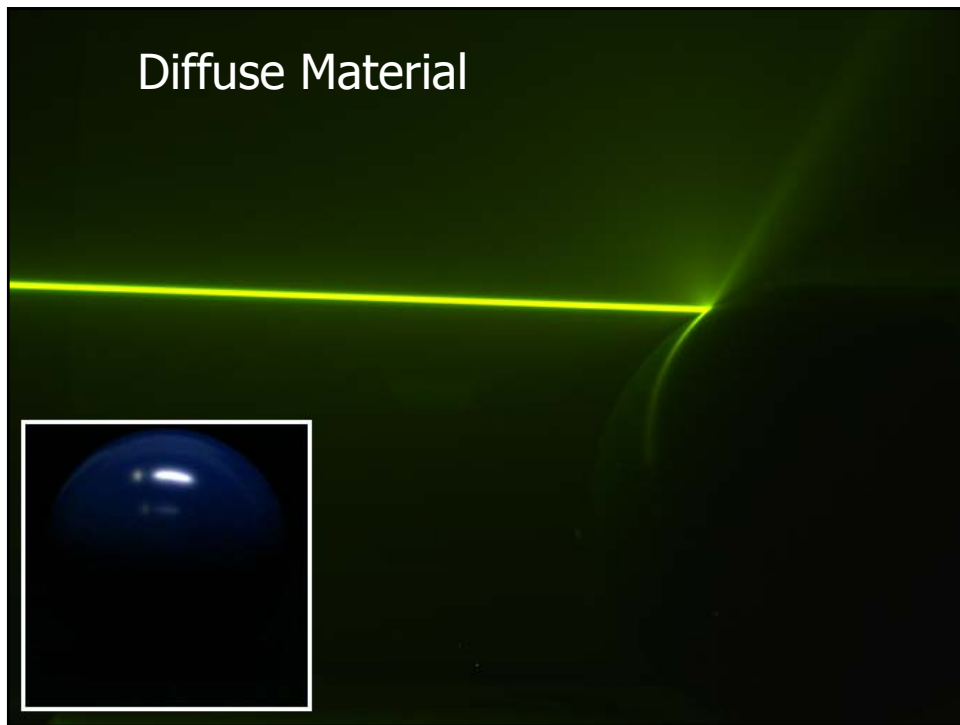
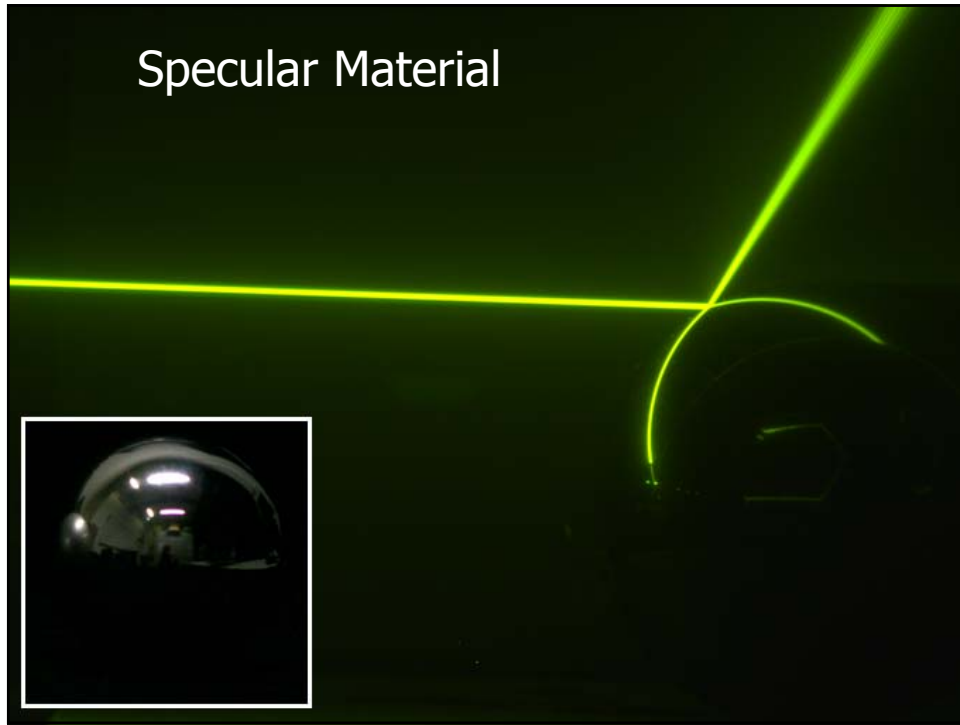


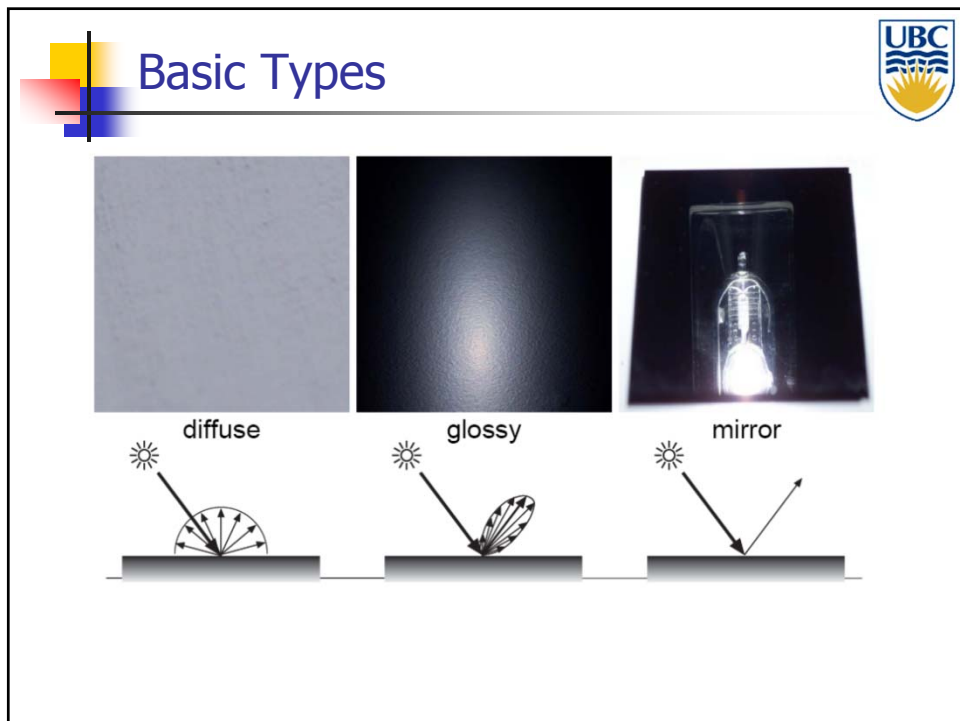
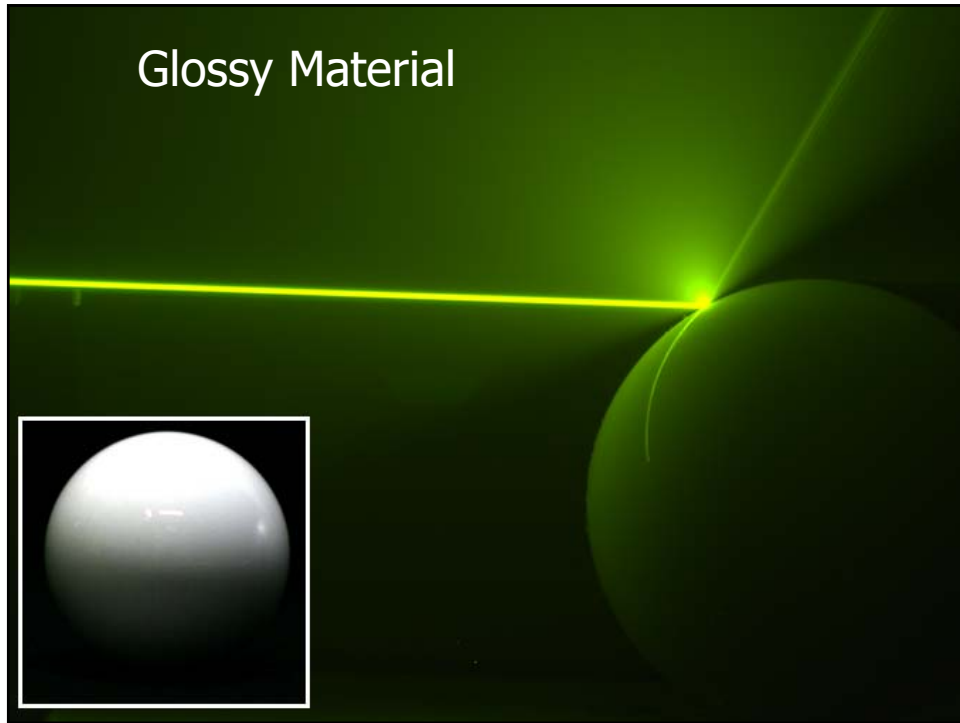
## Materials




- Surface reflectance:
  - Illuminate surface point with a ray of light from different directions
  - How much light is reflected in each direction?






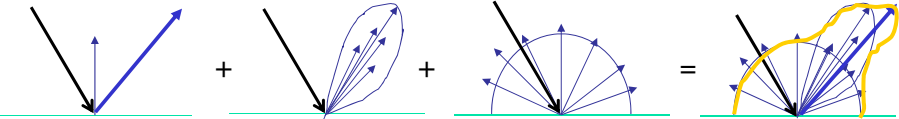





## Reflectance Distribution Model




- Most surfaces exhibit complex reflectances
  - Vary with incident and reflected directions.
  - Model with combination – known as BRDF
    - BRDF: *Bidirectional Reflectance Distribution Function*

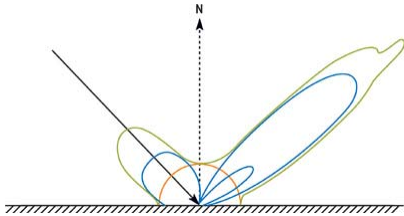


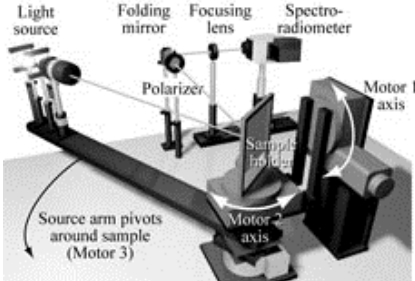



## BRDF measurements/plots




■ 2D slice












## Practical Considerations



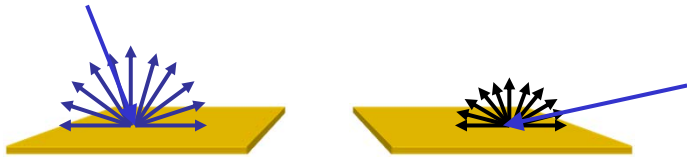
- In practice, often simplify (computational efficiency)
- Derive specific formulas that describe basic reflectance behaviors
  - diffuse, glossy, specular
  - OpenGL choice




## Physics of Diffuse Reflection




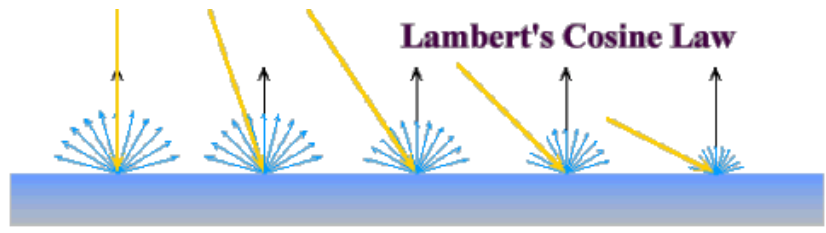
- Ideal diffuse reflection
  - Very rough surface at the microscopic level
    - Real-world example: chalk
    - Microscopic variations mean incoming ray of light equally likely to be reflected in any direction over the hemisphere
  - **Reflected intensity only depends on light direction!**





## Lambert's "Law"

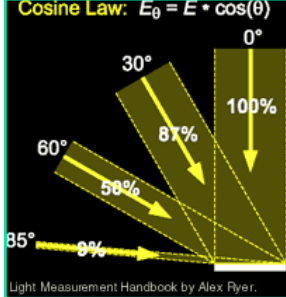





**Lambert's Cosine Law**

Intuitively: cross-sectional area of the "beam" intersecting an element of surface area is smaller for greater angles with the normal.


**Cosine Law:  $E_{\theta} = E \cdot \cos(\theta)$**



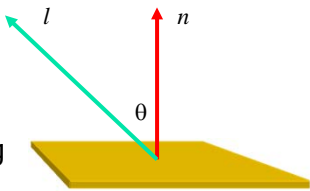
Light Measurement Handbook by Alex Fryer.




## Computing Diffuse Reflection




- Depends on **angle of incidence**: angle between surface normal and incoming light
  - $I_{diffuse} = k_d I_{light} \cos \theta$
- In practice use vector arithmetic
  - $I_{diffuse} = k_d I_{light} (\mathbf{n} \cdot \mathbf{l})$
- Always normalize vectors used in lighting
  - $\mathbf{n}$ ,  $\mathbf{l}$  should be unit vectors
- Scalar (B/W intensity) or 3-tuple or 4-tuple (color)
  - $k_d$ : diffuse coefficient, surface color
  - $I_{light}$ : incoming light intensity
  - $I_{diffuse}$ : outgoing light intensity (for diffuse reflection)








## Diffuse Lighting Examples




- Lambertian sphere from several lighting angles:

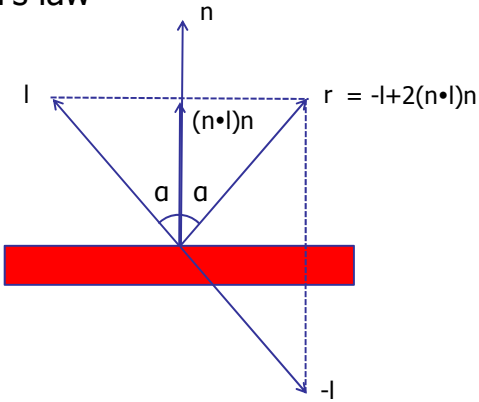


- need only consider angles from  $0^\circ$  to  $90^\circ$ 
  - *Why?*


## Physics of Specular Reflection




- Geometry of specular (perfect mirror) reflection
  - Snell's law




The diagram illustrates the geometry of specular reflection. A red horizontal bar represents the surface. A vertical blue arrow labeled  $n$  points upwards from the surface, representing the normal. An incident ray labeled  $I$  is shown as a blue arrow pointing towards the surface. The angle between  $I$  and  $n$  is labeled  $\alpha$ . A reflected ray labeled  $r$  is shown as a blue arrow pointing away from the surface. The angle between  $r$  and  $n$  is also labeled  $\alpha$ . A dashed blue line represents the projection of  $I$  onto the surface. The reflected ray  $r$  is labeled with the equation  $r = -I + 2(n \cdot I)n$ . A dashed blue line also extends downwards from the surface, labeled  $-I$ .




## Empirical Approximation



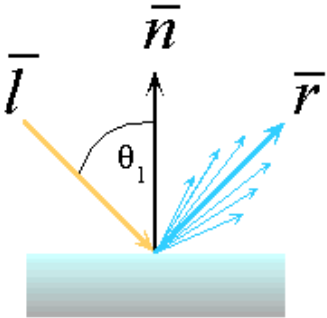
- Snell's law = perfect mirror-like surfaces
  - But ..
    - few surfaces exhibit perfect specular
    - Gaze and reflection directions never EXACTLY coincide
- Expect **most** reflected light to travel in direction predicted by Snell's Law
- But some light may be reflected in a direction slightly off the ideal reflected ray
- As angle from ideal reflected ray increases, we expect less light to be reflected




## Empirical Approximation




- Angular falloff



- How to model this falloff?



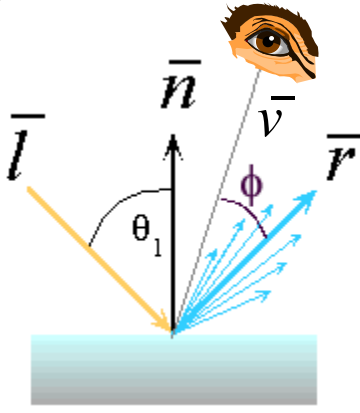
## Phong Lighting




- Most common lighting model in computer graphics
  - (Phong Bui-Tuong, 1975)


$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\cos \phi)^{n_s}$$

$\phi$ : angle between  $\mathbf{r}$  and view direction  $\mathbf{v}$   
 $n_s$ : purely empirical constant, varies rate of falloff  
 $k_s$ : specular coefficient, highlight color  
 no physical basis, works ok in practice



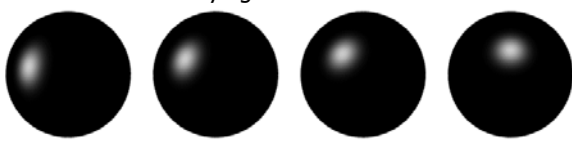


## Phong Examples

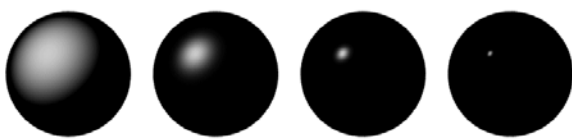
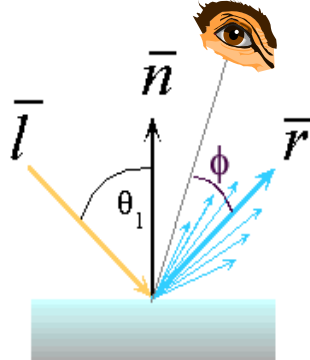



$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\cos \phi)^{n_s}$$

varying  $k_s$




varying  $n_s$



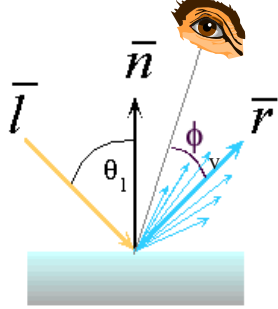
## Calculating Phong Lighting





- compute cosine term of Phong lighting with vectors

$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\mathbf{v} \cdot \mathbf{r})^{n_s}$$


- $\mathbf{v}$ : unit vector towards viewer/eye
- $\mathbf{r}$ : ideal reflectance direction (unit vector)
- $k_s$ : specular component = highlight color
- $\mathbf{I}_{\text{light}}$ : incoming light intensity








## Materials (last bit)




- Light is **linear**
  - If multiple rays illuminate the surface point the result is just the sum of the individual reflections for each ray

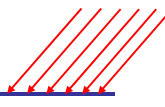
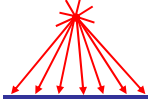
$$\sum_p I_p (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$




## Light Sources




- Point source
  - light originates at a point
  - Rays hit planar surface at different angles
- Parallel source
  - light rays are parallel
  - Rays hit a planar surface at identical angles
  - Can model as point source at infinity
  - *Directional light*

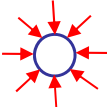
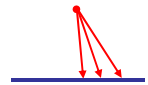
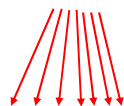




## Light Sources




- Area source
  - Light originates at finite area in space.
  - In-between point and parallel sources
- Spotlights
  - position, direction, angle
- Ambient light (environment light)
  - Hack for replacing true global illumination
    - (light bouncing off from other objects)



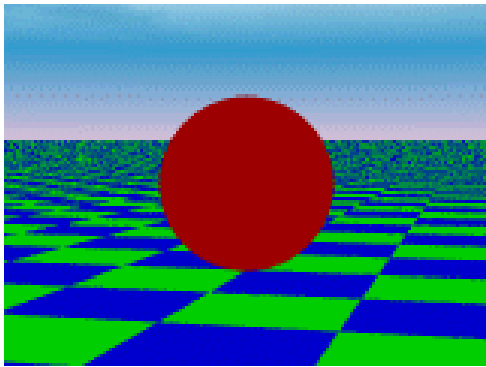
## Ambient Light

- Non-directional light – environment light
- Object illuminated with same light everywhere
  - Looks like silhouette
- Illumination equation  $I = I_a k_a$ 
  - $I_a$  - ambient light intensity
  - $k_a$  - fraction of this light reflected from surface




## Ambient Light Sources

- Scene lit only with an ambient light source

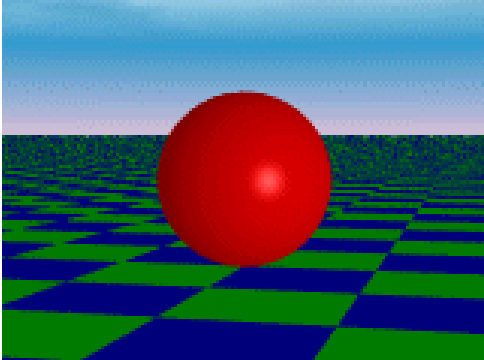


- Light Position  
Not Important
- Viewer Position  
Not Important
- Surface Angle  
Not Important

## Directional Light Sources



- Scene lit with directional and ambient light




Surface Angle Important

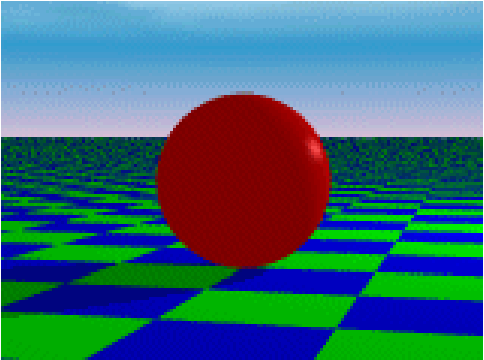
Viewer Position Important

Light Position Not Important

## Point Light Sources




- Scene lit with ambient and point light source




Light Position Important

Viewer Position Important

Surface Angle Important

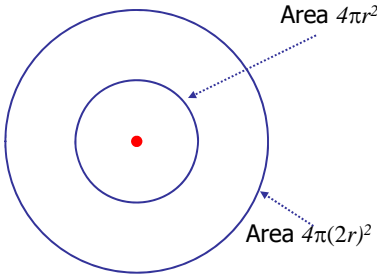



## Light Source Falloff




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- Quadratic falloff (point- and spot lights)
  - Brightness of objects depends on power per unit area that hits the object
  - The power per unit area for a point or spot light decreases quadratically with distance





## Light Source Falloff




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- Non-quadratic falloff
  - Many systems allow for other falloffs
  - Allows for faking effect of area light sources
  - OpenGL / graphics hardware
    - $I_0$ : intensity of light source
    - $\mathbf{x}$ : object point
    - $r$ : distance of light from  $\mathbf{x}$

$$I_{in}(\mathbf{x}) = \frac{1}{ar^2 + br + c} \cdot I_0$$





## Illumination Equation





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- For multiple light sources:


$$I = I_a k_a + \sum_p \frac{I_p}{A(d_p)} (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$

- $d_p$  - distance between surface and light source  
+ distance between surface and viewer, A – attenuation function






shadingmodel



## Light



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- Light has color
- Interacts with object color (r,g,b)


$$I = I_a k_a$$


$$I_a = (I_{ar}, I_{ag}, I_{ab})$$

$$k_a = (k_{ar}, k_{ag}, k_{ab})$$


$$I = (I_r, I_g, I_b) = (I_{ar} k_{ar}, I_{ag} k_{ag}, I_{ab} k_{ab})$$

- Blue light on white surface?
- Blue light on red surface?







## Lighting in OpenGL




- Light source: amount of RGB light emitted
  - value = percentage of full intensity, e.g., (1.0,0.5,0.5)
  - every light source emits ambient, diffuse, and specular light
- Materials: amount of RGB light reflected
  - value represents percentage reflected e.g., (0.0,1.0,0.5)
- Interaction: multiply components
  - Red light (1,0,0) x green surface (0,1,0) = black (0,0,0)




## In OpenGL



- $k_a, k_d, k_s$  - surface color (RGB)
- Modify by `glMaterialfv(GL_FRONT_AND_BACK, pname, RGB[] )`
- `pname` - `GL_AMBIENT`, `GL_DIFFUSE`, `GL_SPECULAR`
- Light source properties (also RGB)  
`glLightfv(GL_LIGHTi, pname, light[])`




## Lighting in OpenGL




```
glLightfv(GL_LIGHT0, GL_AMBIENT, amb_light_rgba );
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif_light_rgba );
glLightfv(GL_LIGHT0, GL_SPECULAR, spec_light_rgba );
glLightfv(GL_LIGHT0, GL_POSITION, position);
glEnable(GL_LIGHT0);


glMaterialfv( GL_FRONT, GL_AMBIENT, ambient_rgba );
glMaterialfv( GL_FRONT, GL_DIFFUSE, diffuse_rgba );
glMaterialfv( GL_FRONT, GL_SPECULAR, specular_rgba );
glMaterialfv( GL_FRONT, GL_SHININESS, n );
```




## Light Sources - OpenGL



- Specify parameters  
`glLightfv(GL_LIGHTi, GL_POSITION, light[])`  
i – between 0 & 8 (or more)
- Directional  $[x \ y \ z \ 0]$
- Point source  $[x \ y \ z \ 1]$
- Spotlight has extra parameters:
  - `GL_SPOT_DIRECTION`, `GL_SPOT_EXPONENT`,  
`GL_SPOT_CUTOFF`
- Area source – too complex for projective pipeline (e.g. OpenGL)



## Lighting in Rendering Pipeline



- Notes:
  - Lighting is applied to every **vertex**
    - i.e. the three vertices in a triangle
    - Per-vertex lighting
  - Will later see how the interior points of the triangle obtain their color
    - This process is called **shading**
    - Will discuss in the context of scan conversion