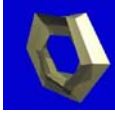
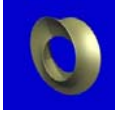


University of British Columbia



Chapter 13

Geometric Modeling Meshes & Subdivision

Meshes



- Simplest boundary representation – polygonal mesh
- Properties
 - Triangular/Quad
 - Manifold
- Simplicity of representation & manipulation
- Base representation for scanned data
- Input to hardware rendering algorithms (Z-buffer, polygon fill, etc..)
- Manipulation algorithms well defined (computational geometry)

University of British Columbia

Processing




- Construction
 - From scans
 - From free-form/volumetric data
- Compression – typical meshes are very large due to
 - Origin (scan)
 - Required LOD
- Manipulation
 - Note: No (u,v) parameterization
- Smoothing
 - Simulate via lighting methods
 - Refine - subdivision

University of British Columbia

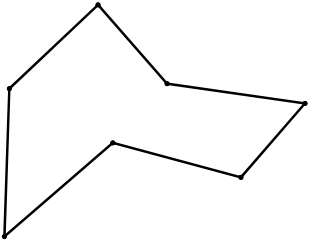
Subdivision Curves and Surfaces

- Subdivision – given polyline/polygon/polyhedron recursively modify its vertices to achieve smooth curve


→

→


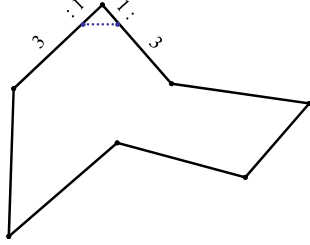
University of British Columbia

Corner Cutting

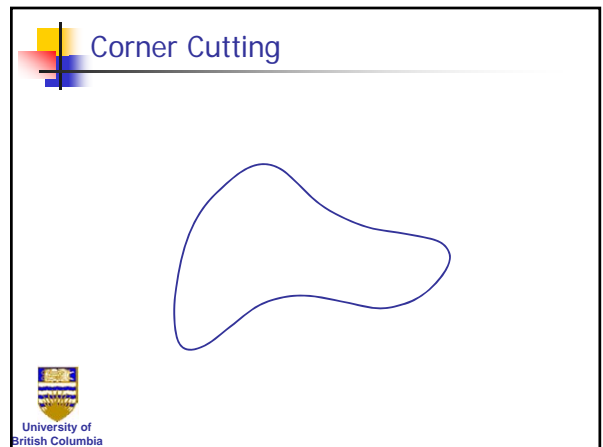
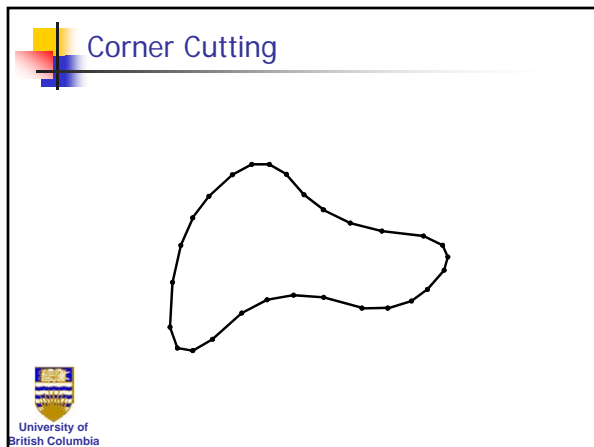
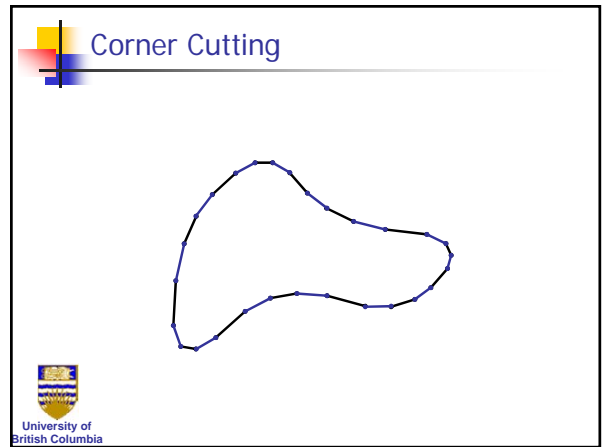
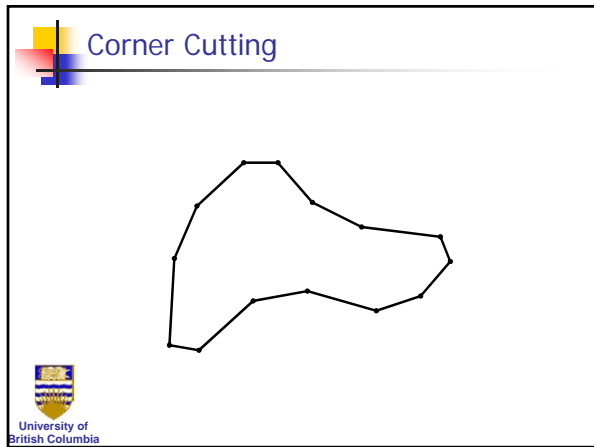
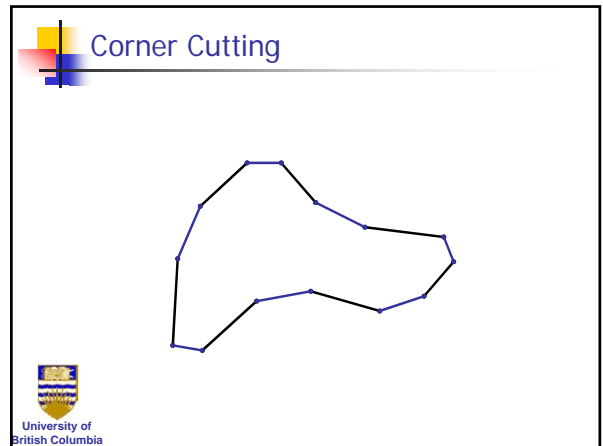
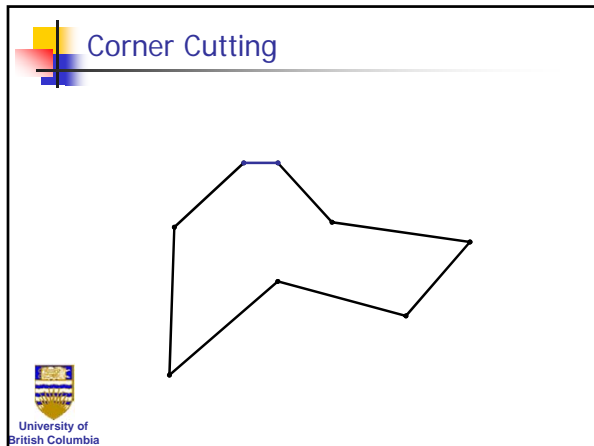


University of British Columbia

Corner Cutting



University of British Columbia



Corner Cutting

control point

limit curve

control polygon

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

δ

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

University of British Columbia

The 4-point scheme

control point

limit curve

control polygon

University of British Columbia

Subdivision curves

Non interpolatory subdivision schemes

- Corner Cutting

Interpolatory subdivision schemes

- The 4-point scheme

University of British Columbia

Subdivision curves

University of British Columbia

Basic concepts of Subdivision

- Subdivision curve generated by repeatedly applying subdivision operator to given polygon
- Each iteration
 - Increase number of vertices (approximately) * 2
- Initial polygon - control polygon
- Central questions:
 - Convergence: Given a subdivision operator and a control polygon, does the subdivision process converge?
 - Smoothness: Does subdivision converge to smooth curve?

University of British Columbia

Subdivision schemes for surfaces

- Each iteration
 - Subdivision refines *control net* (mesh)
 - Increase number of vertices (approximately) * 4
- Mesh vertices converge to limit surface
- Every subdivision method has:
 - Method to generate net topology
 - rules to calculate location of new vertices

University of British Columbia

Triangular subdivision

- Works only for triangular meshes (control nets)
- Every face replaced by 4 new triangular faces
- Two kinds of new vertices:
 - Green vertices are associated with old edges
 - Blue vertices are associated with old vertices

University of British Columbia

Loop's scheme

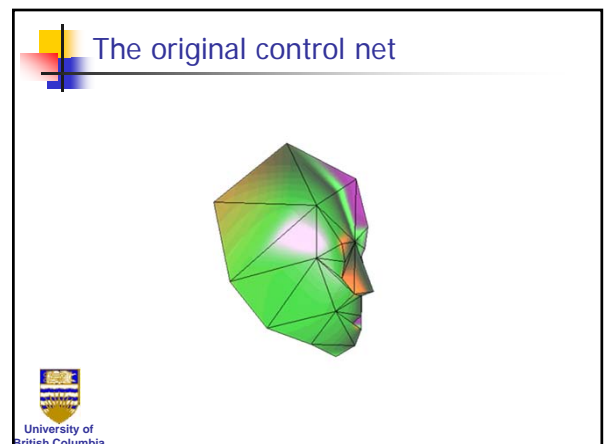
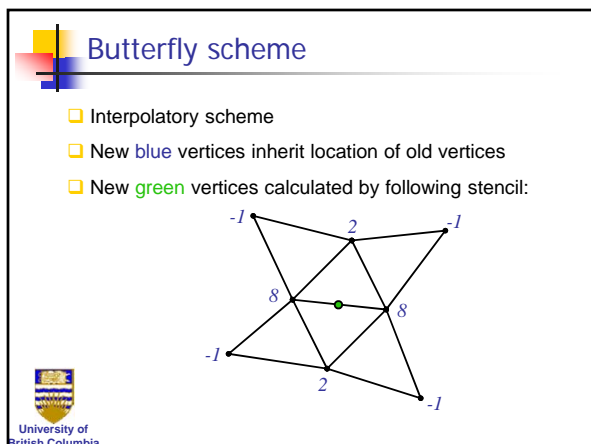
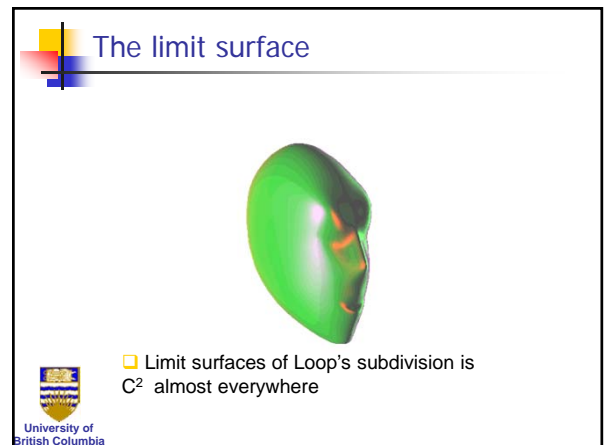
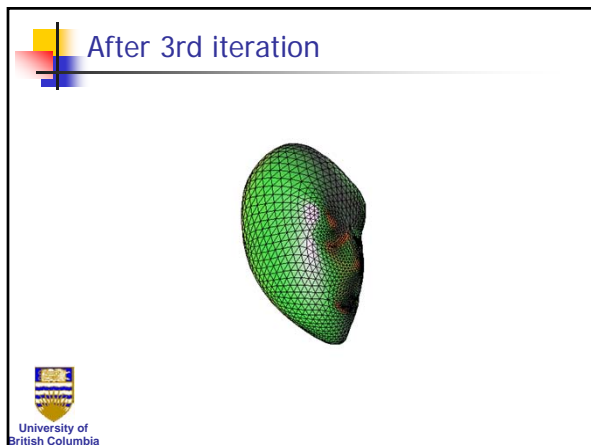
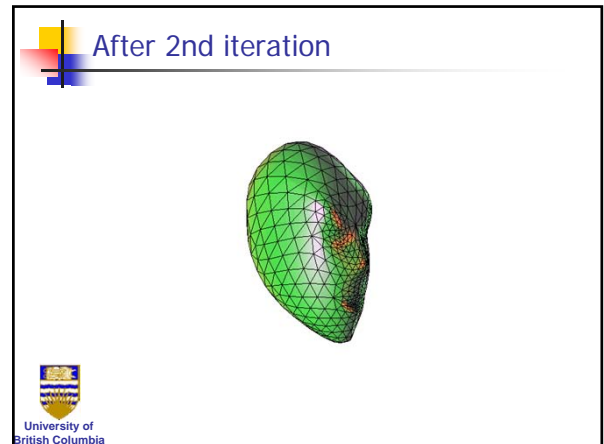
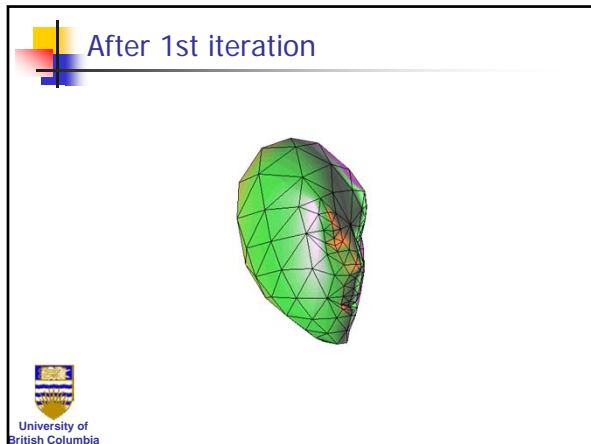
- New vertex = weighted average of old vertices
- List of weights - subdivision mask or stencil
 - Rule for new blue vertices (n - vertex valence)
 - Rule for new green vertices

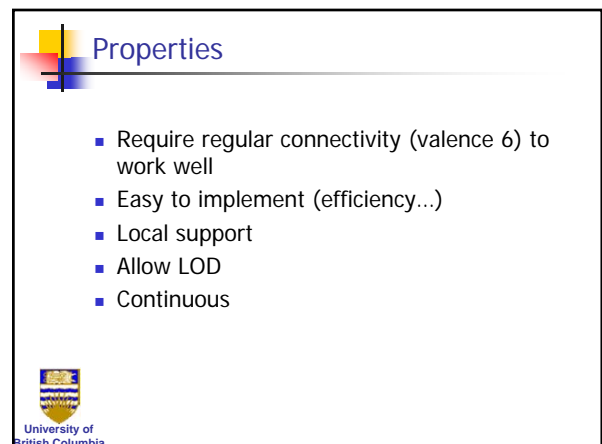
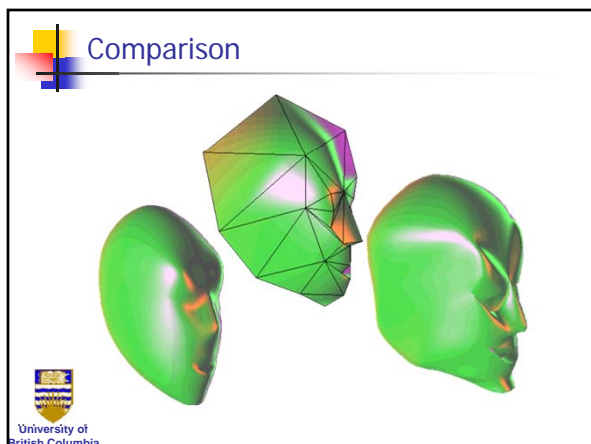
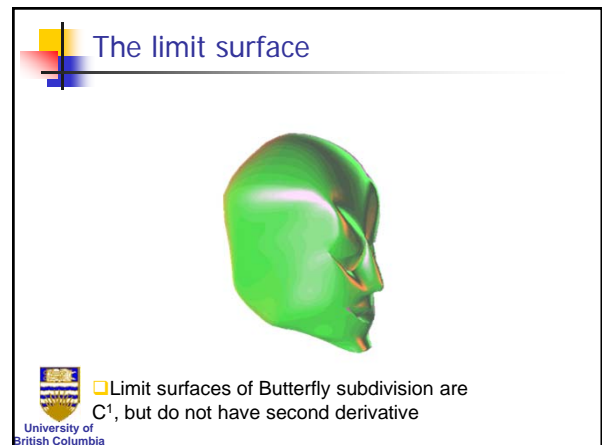
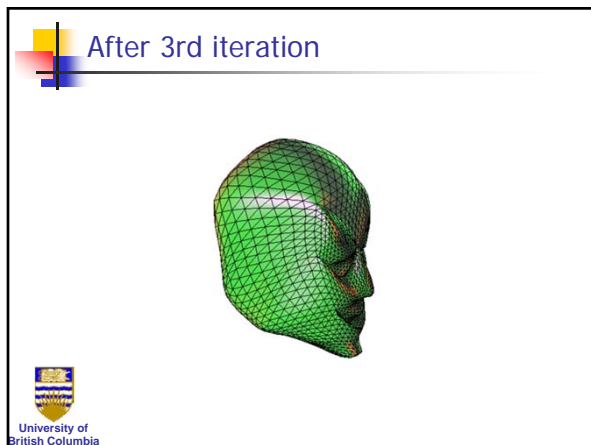
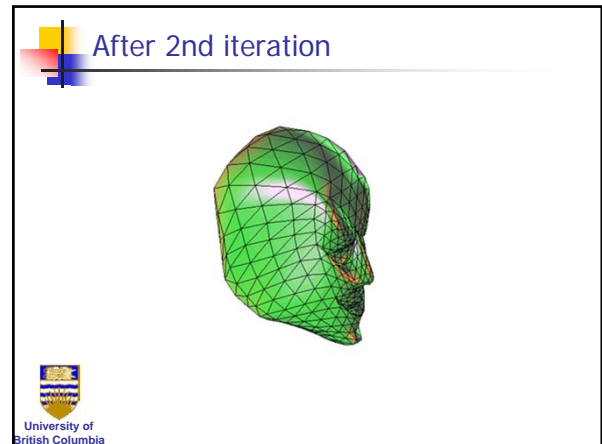
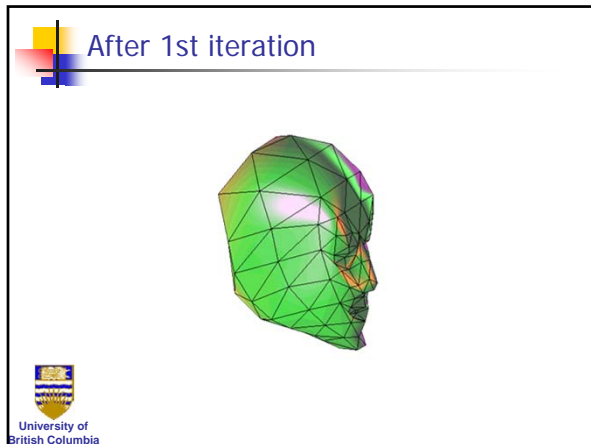
$$w_n = \frac{64n}{40 - (3 + 2\cos(2\pi/n))^2} - n$$

University of British Columbia

The original control net

University of British Columbia

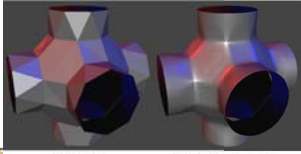






Drawbacks

- Not always intuitive
- Can have artifacts
- Hard to control



Initial mesh

Butterfly scheme interpolation

