## Computer Graphics

 Ray Tracing

## Midterm 2



## Computer Graphics

 Ray TracingRayTrace(r,scene)
obj := FirstIntersection(r,scene)
if (no obj) return BackgroundColor; else begin
if ( $\operatorname{Reflect}\left(\mathrm{obj}_{\mathrm{j}}\right)$ ) then
reflect_color := RayTrace(ReflectRay(r,obj)); else
reflect_color := Black;
if ( Transparent(obj) ) then
refract_color := RayTrace(RefractRay(r,obj));
else
refract_color := Black;
return Shade(reflect_color,refract_color,obj); end;

## More About Ray-Tracing

- Algorithm above has a BUG....
- Does not terminate
- Termination Criteria
- No intersection
- Contribution of secondary ray attenuated below threshold - each reflection/refraction attenuates ray
- Maximal depth is reached



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## Ray Tracing

## Ray-Tracing: Practicalities

- Generation of rays
- Intersection of rays with geometric primitives
- Geometric transformations
- Lighting and shading
- Speed: Reducing number of intersection tests
- E.g. use BSP trees or other types of space partitioning



## Ray-Tracing: Generation of Rays

- Camera Coordinate System
- Origin: C (camera position)
- Viewing direction: w
- Up vector: v
- u direction: $\mathbf{u}=\mathbf{w} \times \mathbf{v}$
- Note:



## Ray-Tracing: Practicalities

## $\overline{\text { UBC }}$

- Generation of rays
- Intersection of rays with geometric primitives
- Geometric transformations
- Lighting and shading
- Speed: Reducing number of intersection tests
- E.g. use BSP trees or other types of space partitioning
transformation in rendering pipeline!
- See gluLookAt...


## Ray-Tracing: Generation of Rays

- Other parameters:
- Distance to image plane: $d$
- Image resolution (in pixels): $x, h$
- Left, right, top, bottom boundaries in image plane: $l, r, t, b$

- Then:
- Lower left corner of image: $O=C+d \cdot w+l \cdot u+b \cdot v$
- Pixel at position $i, j(i=0 . . x-1, j=0 . . h-1)$ :
$P_{i, j}=O+i \cdot \frac{r-l}{x-1} \cdot \mathrm{u}-j \cdot \frac{t-b}{h-1} \cdot \mathrm{v}$
$=O+i \cdot \Delta u \cdot \mathrm{u}-j \cdot \Delta v \cdot \mathrm{v}$


## Ray-Object Intersections

- Kernel of ray-tracing $\Rightarrow$ must be extremely efficient
- Usually involves solving a set of equations - Using implicit formulas for primitives

Example: Ray-Sphere intersection

$$
\begin{aligned}
& \text { ray: } x(t)=p_{x}+v_{x} t, y(t)=p_{y}+v_{y} t, z(t)=p_{z}+v_{z} t \\
& \text { (unit) sphere: } x^{2}+y^{2}+z^{2}=1 \\
& \text { quadratic equation in } t \text { : } \\
& 0=\left(p_{x}+v_{x} t\right)^{2}+\left(p_{y}+v_{y} t\right)^{2}+\left(p_{z}+v_{z} t\right)^{2}-1 \\
& =t^{2}\left(v_{x}^{2}+v_{y}^{2}+v_{z}^{2}\right)+2 t\left(p_{x} v_{x}+p_{y} v_{y}+p_{z} v_{z}\right) \\
& \quad+\left(p_{x}^{2}+p_{y}^{2}+p_{z}^{2}\right)-1
\end{aligned}
$$

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. But roople the same
But root-finding difficult

- Net to resolve to numerical methods
- Other Primitives:
- Implicit functions:
- Spheres at arbitrary positions - Same thing

Conic sections (hyperboloids, ellipsoids, paraboloids, cones, cylinders)

- Same thing (all are quadratic functions!)
- Higher order functions (e.g. tori and other quartic functions)
- 

$\qquad$

## Ray-Tracing: Transformations

- Note: rays replace perspective transformation
- Geometric Transformations:
- Similar goal as in rendering pipeline:
- Modeling scenes convenient using different coordinate systems for individual objects
- Problem:
- Not all object representations are easy to transform
- This problem is fixed in rendering pipeline by restriction to polygons (affine invariance!)


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## Ray Tracing

## Ray-Tracing: Local Lighting

## - Light sources:

- For the moment: point and directional lights
- More complex lights are possible
- Area lights
- Global illumination
- Other objects in the scene reflect light
- Everything is a light source!
- Talk about this on Monday


## Ray-Tracing: Local Lighting

- Local surface information (normal...)
- For implicit surfaces $F(x, y, z)=0$ : normal $\mathbf{n}(x, y, z)$ can be easily computed at every intersection point using the gradient

$$
\mathbf{n}(x, y, z)=\left(\begin{array}{l}
\partial F(x, y, z) / \partial x \\
\partial F(x, y, z) / \partial y \\
\partial F(x, y, z) / \partial z
\end{array}\right)
$$

- Example:

$$
\begin{aligned}
F(x, y, z)=x^{2} & +y^{2}+z^{2}-r^{2} \\
\mathbf{n}(x, y, z) & =\left(\begin{array}{l}
2 x \\
2 y \\
2 z
\end{array}\right) \quad \text { Needs to be normalized }
\end{aligned}
$$

## Ray-Tracing: Local Lighting

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- Local surface information
- Alternatively: can interpolate per-vertex information for triangles/meshes as in rendering pipeline
- Phong shading!
- Same as discussed for rendering pipeline
- Difference to rendering pipeline:
- Have to compute Barycentric coordinates for every intersection point (e.g plane equation for triangles)


## Ray Tracing

- Data Structures
- Goal: reduce number of intersection tests per ray
- Lots of different approaches:
- (Hierarchical) bounding volumes
- Hierarchical space subdivision
- Octree, k-D tree, BSP tree


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## Spatial Subdivision Data Structures UBC

- Bounding Volumes:
- Find simple object completely enclosing complicated objects
- Boxes, spheres
- Hierarchically combine into larger bounding volumes
- Spatial subdivision data structure:
- Partition the whole space into cells - Grids, octrees, (BSP trees)
- Simplifies and accelerates traversal
- Performance less dependent on order in which objects are inserted


## Soft Shadows: Area Light Sources

- So far:
- All lights were either point-shaped or directional
- Both for ray-tracing and the rendering pipeline
- Thus, at every point, we only need to compute lighting formula and shadowing for ONE direction per light
- In reality:
- All lights have a finite area
- Instead of just dealing with one direction, we now have to integrate over all directions that go to the light source



## Are Light Sources

- Area Lights:
- Infinitely many light rays
- Need to integrate over all of them:


| light |
| :---: |
| directions |

- Lighting model visibility and light intensity can now be different for every ray!



## Integrating over Light Source

- Rewrite the integration
- Instead of integrating over directions

$I_{\text {refecced }}=\int \rho(\omega) \cdot V(\omega) \cdot I_{\text {light }}(\omega) \cdot d \omega$ | light |
| :---: |
| directions |

integrate over points on the light source
$I_{\text {refleced }}(q)=\int_{s, t} \rho(p-q) \cdot V(p-q) I_{\text {light }}(p) \cdot d s \cdot d t$

- q point on reflecting surface
- $p=F(s, t)$ point on the area light
- We are integrating over $p$


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## Integration

## - Problem:

- Except for basic case not solvable analytically!
- Largely due to the visibility term
- So:
- Use numerical integration = approximate light with lots of point lights


