


Computer Graphics

Illumination Models

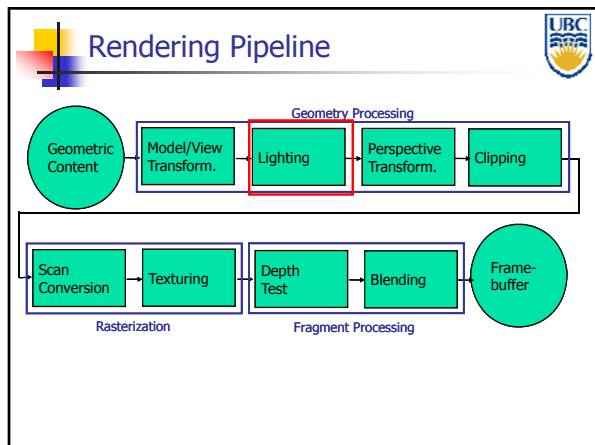
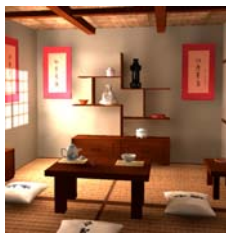
Chapter 6

Lighting





Factors

- Light sources
 - Location, type & color
- Surface materials
 - How surfaces reflect light
- Transport of light
 - How light moves in a scene
- Viewer position




Illumination Models/Algorithms

- Local illumination - Fast
 - Ignore real physics, approximate the look
 - Interaction of each object with light
 - Compute on surface (light to viewer)
- Global illumination – Slow
 - Physically based
 - Interactions between objects






Lighting/Shading

- Goal
 - Model the interaction of light with surfaces to render realistic images
 - Generate per (pixel/vertex) color



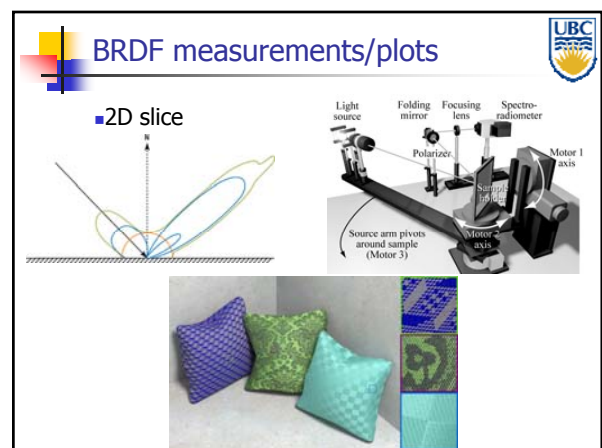
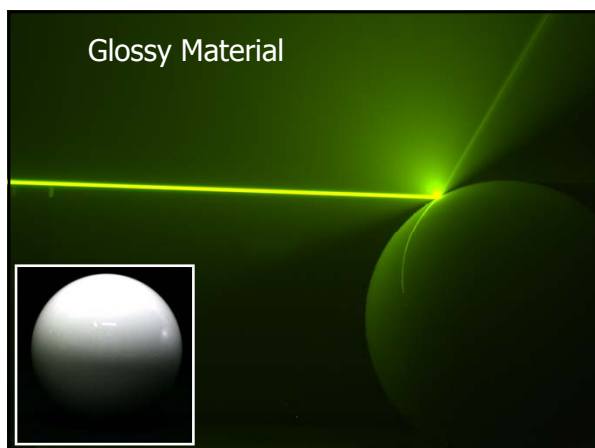
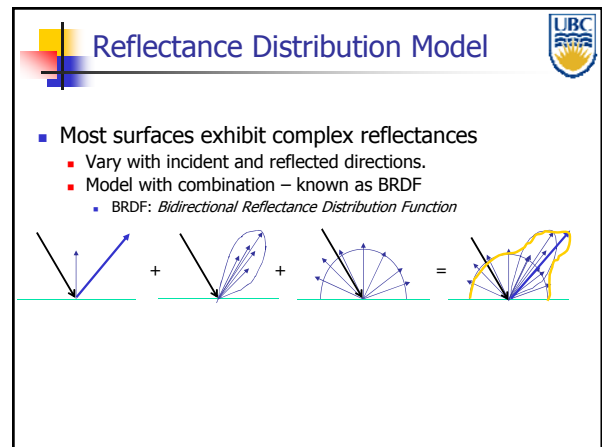
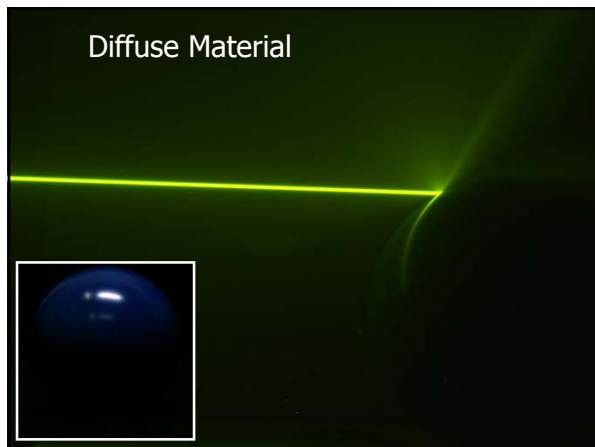
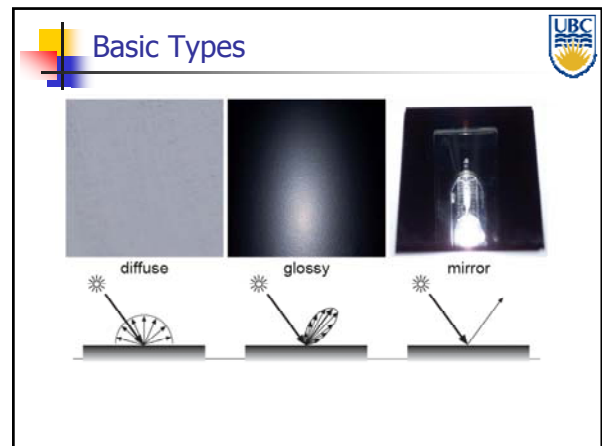
Materials

- Surface reflectance:
 - Illuminate surface point with a ray of light from different directions
 - How much light is reflected in each direction?



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Illumination Models



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Illumination Models

Practical Considerations

- In practice, often simplify (computational efficiency)
- Derive specific formulas that describe basic reflectance behaviors
 - diffuse, glossy, specular
 - OpenGL choice

Computing Diffuse Reflection

- Depends on **angle of incidence**: angle between surface normal and incoming light
 - $I_{diffuse} = k_d I_{light} \cos \theta$
- In practice use vector arithmetic
 - $I_{diffuse} = k_d I_{light} (\mathbf{n} \cdot \mathbf{l})$
- Always normalize vectors used in lighting
 - \mathbf{n} , \mathbf{l} should be unit vectors
- Scalar (B/W intensity) or 3-tuple or 4-tuple (color)
 - k_d : diffuse coefficient, surface color
 - I_{light} : incoming light intensity
 - $I_{diffuse}$: outgoing light intensity (for diffuse reflection)

Physics of Diffuse Reflection

- Ideal diffuse reflection
 - Very rough surface at the microscopic level
 - Real-world example: chalk
 - Microscopic variations mean incoming ray of light equally likely to be reflected in any direction over the hemisphere
 - Reflected intensity only depends on light direction!

Diffuse Lighting Examples

- Lambertian sphere from several lighting angles:
- need only consider angles from 0° to 90°
 - Why?

Lambert's "Law"

Lambert's Cosine Law

Intuitively: cross-sectional area of the "beam" intersecting an element of surface area is smaller for greater angles with the normal.

Cosine Law: $E_0 = E \cdot \cos(\theta)$

Angle (θ)	Percentage of Intensity
0°	100%
30°	87%
60°	50%
85°	12%

Light Measurement Handbook by Alex Payer

Physics of Specular Reflection

- Geometry of specular (perfect mirror) reflection
 - Snell's law

$r = -l + 2(\mathbf{n} \cdot \mathbf{n})$

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Illumination Models

Empirical Approximation

- Snell's law = perfect mirror-like surfaces
 - But ..
 - few surfaces exhibit perfect specularity
 - Gaze and reflection directions never EXACTLY coincide
- Expect **most** reflected light to travel in direction predicted by Snell's Law
- But some light may be reflected in a direction slightly off the ideal reflected ray
- As angle from ideal reflected ray increases, we expect less light to be reflected

Phong Examples

$$I_{\text{specular}} = k_s I_{\text{light}} (\cos \phi)^{n_s}$$

Empirical Approximation

- Angular falloff

- How to model this falloff?

Calculating Phong Lighting

- compute cosine term of Phong lighting with vectors

$$I_{\text{specular}} = k_s I_{\text{light}} (\mathbf{v} \cdot \mathbf{r})^{n_s}$$

- v: unit vector towards viewer/eye
- r: ideal reflectance direction (unit vector)
- k_s: specular component = highlight color
- I_{light}: incoming light intensity

Phong Lighting

- Most common lighting model in computer graphics
 - (Phong Bui-Tuong, 1975)

$$I_{\text{specular}} = k_s I_{\text{light}} (\cos \phi)^{n_s}$$

φ: angle between r and view direction v
 n_s: purely empirical constant, varies rate of falloff
 k_s: specular coefficient, highlight color
 no physical basis, works ok in practice

Materials (last bit)

- Light is **linear**
 - If multiple rays illuminate the surface point the result is just the sum of the individual reflections for each ray


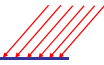
$$\sum_p I_p (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$

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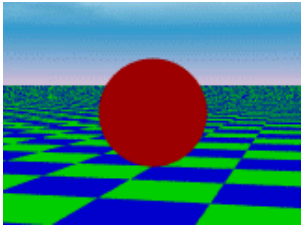
Light Sources

- Point source
 - light originates at a point
 - Rays hit planar surface at different angles
- Parallel source
 - light rays are parallel
 - Rays hit a planar surface at identical angles
 - Can model as point source at infinity
 - Directional light*

Ambient Light Sources




- Scene lit only with an ambient light source



- Light Position Not Important
- Viewer Position Not Important
- Surface Angle Not Important

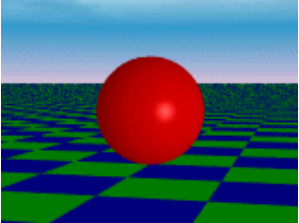
Light Sources

- Area source
 - Light originates at finite area in space.
 - In-between point and parallel sources
- Spotlights
 - position, direction, angle
- Ambient light (environment light)
 - Hack for replacing true global illumination
 - (light bouncing off from other objects)

Directional Light Sources


- Scene lit with directional and ambient light



- Surface Angle Important
- Viewer Position Important
- Light Position Not Important

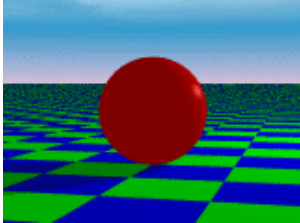
Ambient Light

- Non-directional light – environment light
- Object illuminated with same light everywhere
 - Looks like silhouette
- Illumination equation $I = I_a k_a$
 - I_a - ambient light intensity
 - k_a - fraction of this light reflected from surface



Point Light Sources

- Scene lit with ambient and point light source



- Light Position Important
- Viewer Position Important
- Surface Angle Important

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Illumination Models

Light Source Falloff

- Quadratic falloff (point- and spot lights)
- Brightness of objects depends on power per unit area that hits the object
- The power per unit area for a point or spot light decreases quadratically with distance

Light

- Light has color
- Interacts with object color (r,g,b)

$$I = I_a k_a$$

$$I_a = (I_{ar}, I_{ag}, I_{ab})$$

$$k_a = (k_{ar}, k_{ag}, k_{ab})$$

$$I = (I_r, I_g, I_b) = (I_{ar}k_{ar}, I_{ag}k_{ag}, I_{ab}k_{ab})$$

- Blue light on white surface?
- Blue light on red surface?

Light Source Falloff

- Non-quadratic falloff
- Many systems allow for other falloffs
- Allows for faking effect of area light sources
- OpenGL / graphics hardware
 - I_0 : intensity of light source
 - \mathbf{x} : object point
 - r : distance of light from \mathbf{x}

$$I_{in}(\mathbf{x}) = \frac{1}{ar^2 + br + c} \cdot I_0$$

Lighting in OpenGL

- Light source: amount of RGB light emitted
 - value = percentage of full intensity, e.g., (1.0,0.5,0.5)
 - every light source emits ambient, diffuse, and specular light
- Materials: amount of RGB light reflected
 - value represents percentage reflected e.g., (0.0,1.0,0.5)
- Interaction: multiply components
 - Red light (1,0,0) x green surface (0,1,0) = black (0,0,0)

Illumination Equation

- For multiple light sources:


$$I = I_a k_a + \sum_p \frac{I_p}{A(d_p)} (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$

- d_p - distance between surface and light source + distance between surface and viewer, A – attenuation function

In OpenGL

- k_a, k_d, k_s - surface color (RGB)
- Modify by `glMaterialfv(GL_FRONT_AND_BACK, pname, RGB[])`
- `pname` - GL_AMBIENT, GL_DIFFUSE, GL_SPECULAR
- Light source properties (also RGB) `glLightfv(GL_LIGHTi, pname, light[])`


Lighting in OpenGL



```
glLightfv(GL_LIGHT0, GL_AMBIENT, amb_light_rgba );
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif_light_rgba );
glLightfv(GL_LIGHT0, GL_SPECULAR, spec_light_rgba );
glLightfv(GL_LIGHT0, GL_POSITION, position);
glEnable(GL_LIGHT0);


glMaterialfv( GL_FRONT, GL_AMBIENT, ambient_rgba );
glMaterialfv( GL_FRONT, GL_DIFFUSE, diffuse_rgba );
glMaterialfv( GL_FRONT, GL_SPECULAR, specular_rgba );
glMaterialfv( GL_FRONT, GL_SHININESS, n );
```

Light Sources - OpenGL



- Specify parameters
`glLightfv(GL_LIGHTi, GL_POSITION, light[])`
i – between 0 & 8 (or more)
- Directional [x y z 0]
- Point source [x y z 1]
- Spotlight has extra parameters:
 - `GL_SPOT_DIRECTION`, `GL_SPOT_EXPONENT`, `GL_SPOT_CUTOFF`
- Area source – too complex for projective pipeline (e.g. OpenGL)

Lighting in Rendering Pipeline



- Notes:
 - Lighting is applied to every **vertex**
 - i.e. the three vertices in a triangle
 - Per-vertex lighting
 - Will later see how the interior points of the triangle obtain their color
 - This process is called **shading**
 - Will discuss in the context of scan conversion