




Lighting/Shading




- Goal
 - Model the interaction of light with surfaces to render realistic images
 - Generate per (pixel/vertex) color




Factors





- Light sources
 - Location, type & color
- Surface materials
 - How surfaces reflect light
- Transport of light
 - How light moves in a scene
- Viewer position




Illumination Models/Algorithms






- Local illumination - Fast
 - Ignore real physics, approximate the look
 - Interaction of each object with light
 - Compute on surface (light to viewer)
- Global illumination – Slow
 - Physically based
 - Interactions between objects

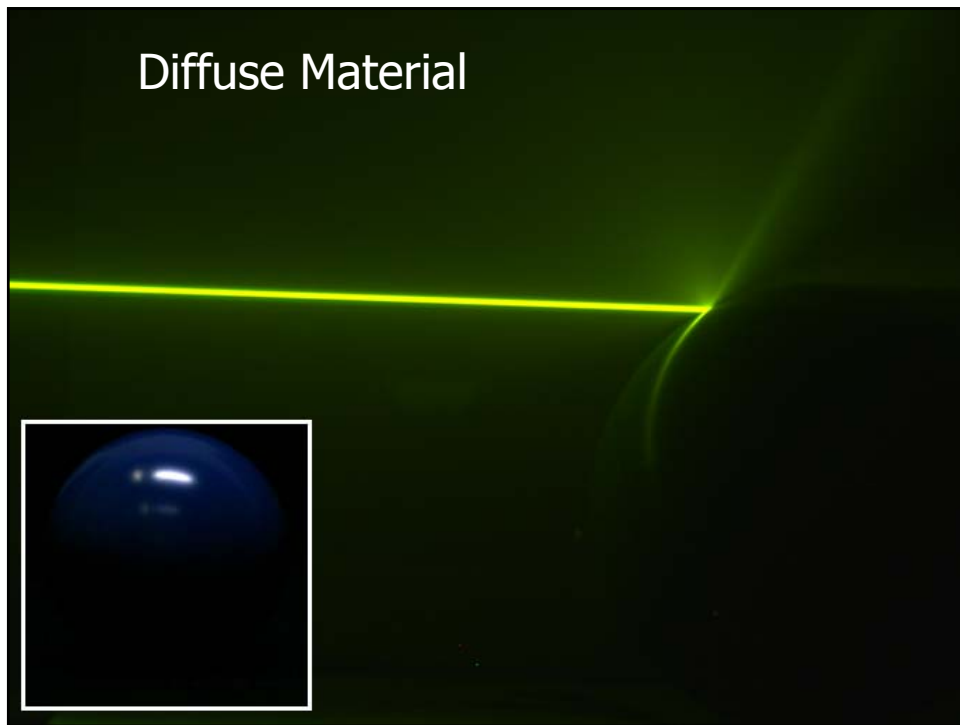
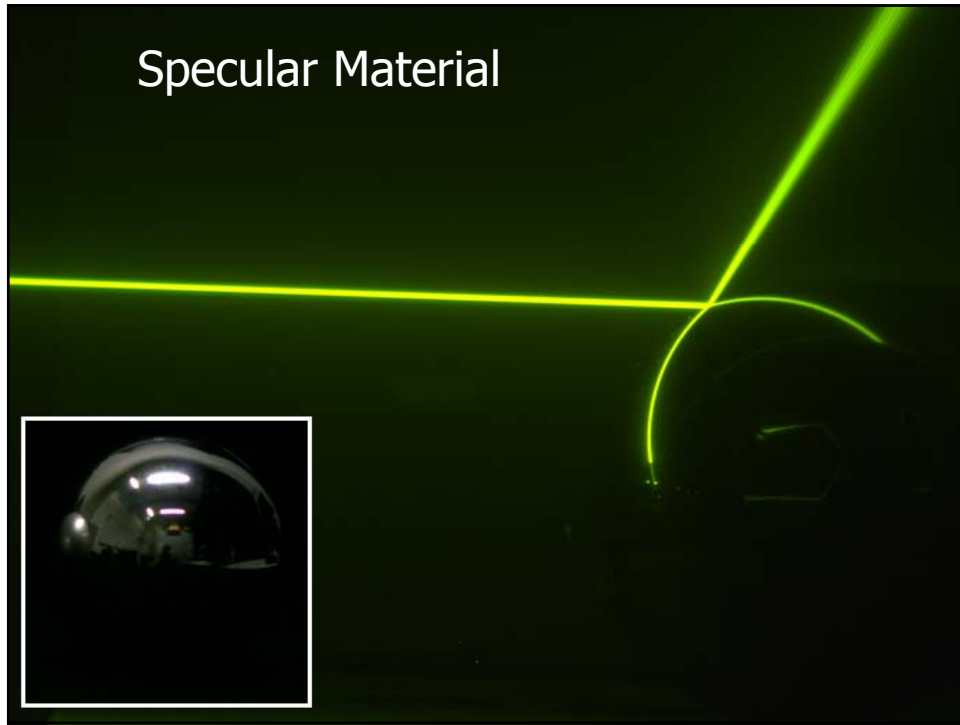


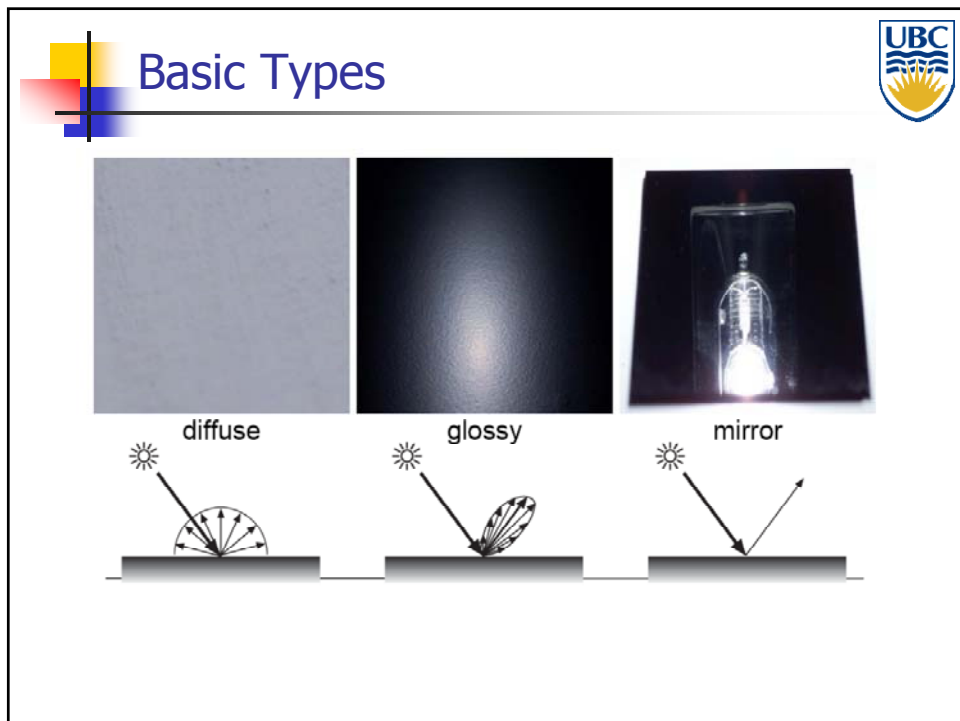
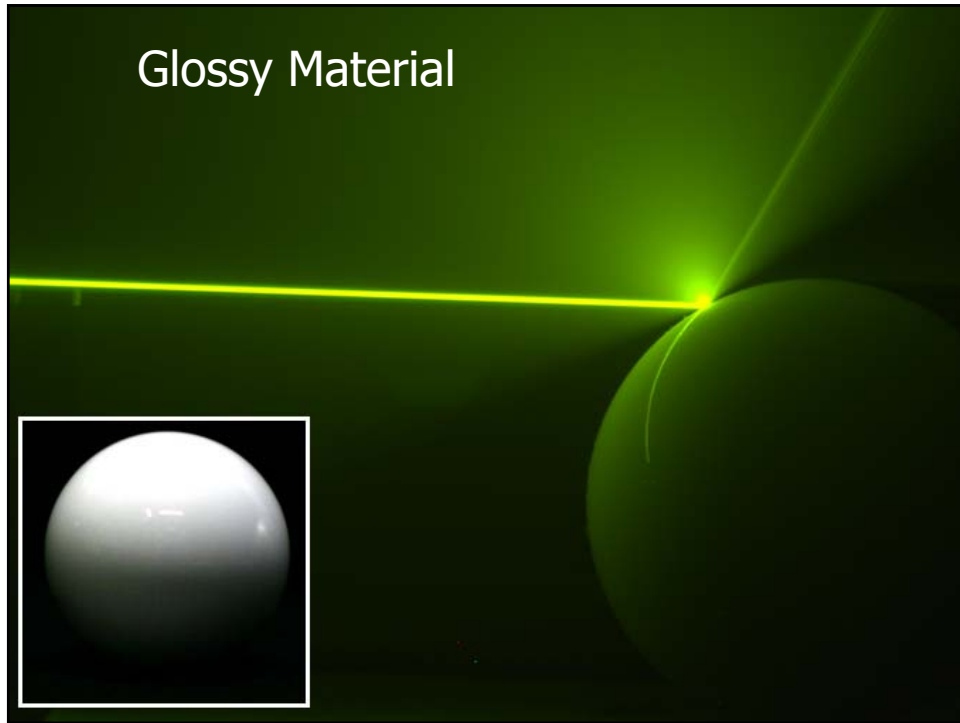
Materials




- Surface reflectance:
 - Illuminate surface point with a ray of light from different directions
 - How much light is reflected in each direction?






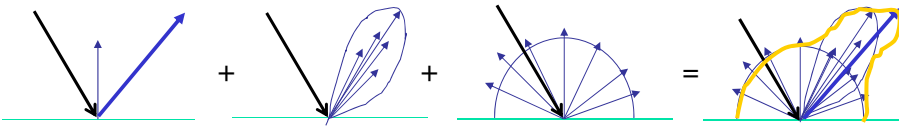





Reflectance Distribution Model




- Most surfaces exhibit complex reflectances
 - Vary with incident and reflected directions.
 - Model with combination – known as BRDF
 - BRDF: *Bidirectional Reflectance Distribution Function*

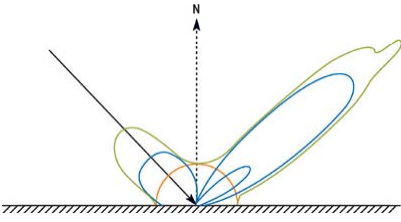


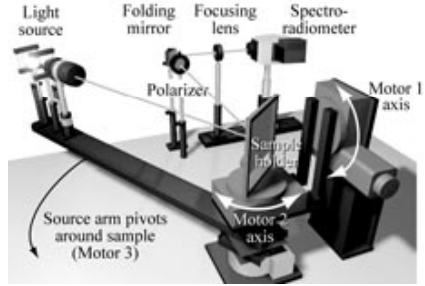



BRDF measurements/plots




■ 2D slice












Practical Considerations



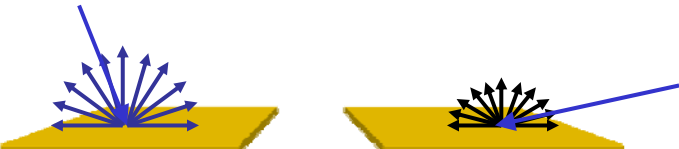
- In practice, often simplify (computational efficiency)
- Derive specific formulas that describe basic reflectance behaviors
 - diffuse, glossy, specular
 - OpenGL choice




Physics of Diffuse Reflection




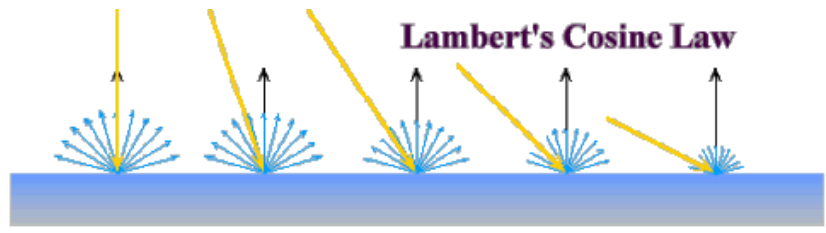
- Ideal diffuse reflection
 - Very rough surface at the microscopic level
 - Real-world example: chalk
 - Microscopic variations mean incoming ray of light equally likely to be reflected in any direction over the hemisphere
 - Reflected intensity only depends on light direction!





Lambert's "Law"

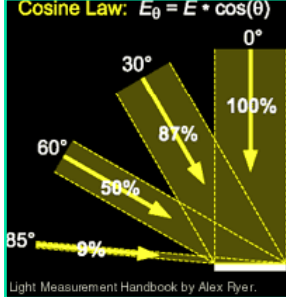





Lambert's Cosine Law

Intuitively: cross-sectional area of the "beam" intersecting an element of surface area is smaller for greater angles with the normal.


Cosine Law: $E_{\theta} = E \cdot \cos(\theta)$



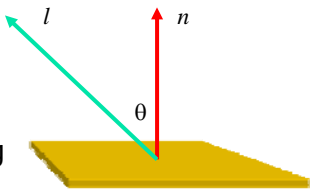
Light Measurement Handbook by Alex Fryer.




Computing Diffuse Reflection




- Depends on **angle of incidence**: angle between surface normal and incoming light
 - $I_{diffuse} = k_d I_{light} \cos \theta$
- In practice use vector arithmetic
 - $I_{diffuse} = k_d I_{light} (\mathbf{n} \cdot \mathbf{l})$
- Always normalize vectors used in lighting
 - \mathbf{n} , \mathbf{l} should be unit vectors
- Scalar (B/W intensity) or 3-tuple or 4-tuple (color)
 - k_d : diffuse coefficient, surface color
 - I_{light} : incoming light intensity
 - $I_{diffuse}$: outgoing light intensity (for diffuse reflection)






Diffuse Lighting Examples




- Lambertian sphere from several lighting angles:

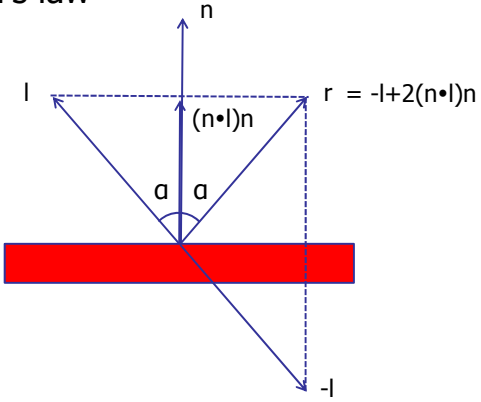


- need only consider angles from 0° to 90°
 - *Why?*


Physics of Specular Reflection




- Geometry of specular (perfect mirror) reflection
 - Snell's law




The diagram illustrates the geometry of specular reflection. A red horizontal bar represents the surface. A vertical blue arrow labeled n points upwards from the surface, representing the surface normal. An incident ray I is shown as a blue arrow pointing towards the surface. The angle between I and n is labeled α . A reflected ray r is shown as a blue arrow pointing away from the surface. The angle between r and n is also labeled α . A dashed blue line represents the projection of I onto the surface normal, labeled $(n \cdot I)n$. The reflected ray r is given by the equation $r = -I + 2(n \cdot I)n$. A dashed blue line also shows the projection of I onto the surface plane, labeled $-I$.




Empirical Approximation



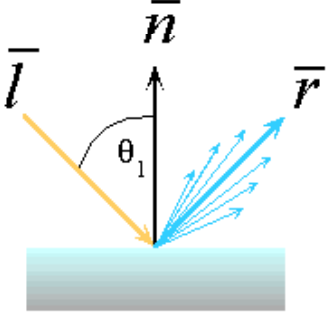
- Snell's law = perfect mirror-like surfaces
 - But ..
 - few surfaces exhibit perfect specular
 - Gaze and reflection directions never EXACTLY coincide
- Expect **most** reflected light to travel in direction predicted by Snell's Law
- But some light may be reflected in a direction slightly off the ideal reflected ray
- As angle from ideal reflected ray increases, we expect less light to be reflected




Empirical Approximation




- Angular falloff



- How to model this falloff?



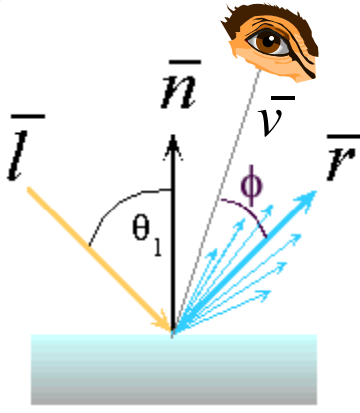
Phong Lighting




- Most common lighting model in computer graphics
 - (Phong Bui-Tuong, 1975)


$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\cos \phi)^{n_s}$$

ϕ : angle between \mathbf{r} and view direction \mathbf{v}
 n_s : purely empirical constant, varies rate of falloff
 k_s : specular coefficient, highlight color
 no physical basis, works ok in practice



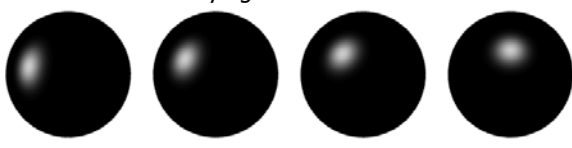


Phong Examples

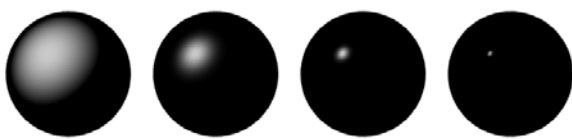
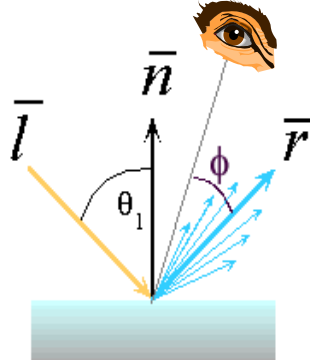



$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\cos \phi)^{n_s}$$

varying k_s




varying n_s



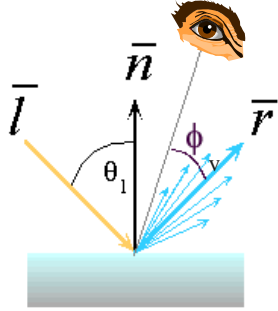
Calculating Phong Lighting





- compute cosine term of Phong lighting with vectors

$$\mathbf{I}_{\text{specular}} = k_s \mathbf{I}_{\text{light}} (\mathbf{v} \cdot \mathbf{r})^{n_s}$$


- \mathbf{v} : unit vector towards viewer/eye
- \mathbf{r} : ideal reflectance direction (unit vector)
- k_s : specular component = highlight color
- $\mathbf{I}_{\text{light}}$: incoming light intensity








Materials (last bit)




- Light is **linear**
 - If multiple rays illuminate the surface point the result is just the sum of the individual reflections for each ray

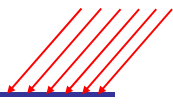
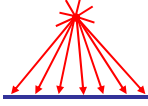
$$\sum_p I_p (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$




Light Sources




- Point source
 - light originates at a point
 - Rays hit planar surface at different angles
- Parallel source
 - light rays are parallel
 - Rays hit a planar surface at identical angles
 - Can model as point source at infinity
 - *Directional light*

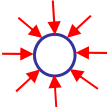
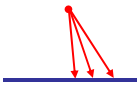
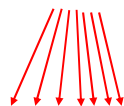




Light Sources




- Area source
 - Light originates at finite area in space.
 - In-between point and parallel sources
- Spotlights
 - position, direction, angle
- Ambient light (environment light)
 - Hack for replacing true global illumination
 - (light bouncing off from other objects)



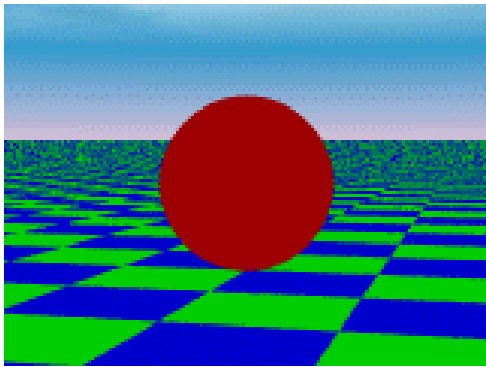
Ambient Light

- Non-directional light – environment light
- Object illuminated with same light everywhere
 - Looks like silhouette
- Illumination equation $I = I_a k_a$
 - I_a - ambient light intensity
 - k_a - fraction of this light reflected from surface




Ambient Light Sources


- Scene lit only with an ambient light source



- Light Position
Not Important
- Viewer Position
Not Important
- Surface Angle
Not Important

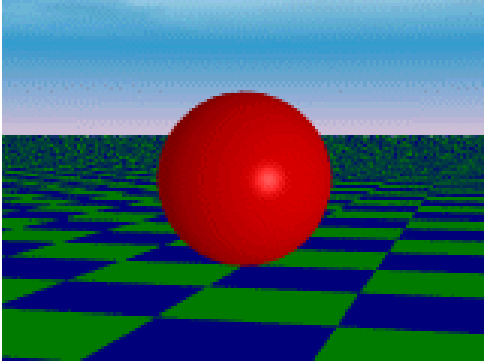


Directional Light Sources




- Scene lit with directional and ambient light

Surface Angle
Important




Light Position
Not Important

Viewer Position
Important

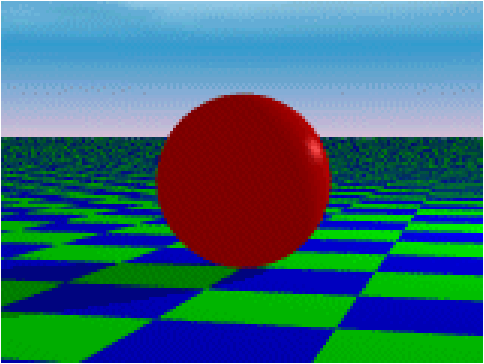


Point Light Sources




- Scene lit with ambient and point light source

Light Position
Important




Viewer Position
Important

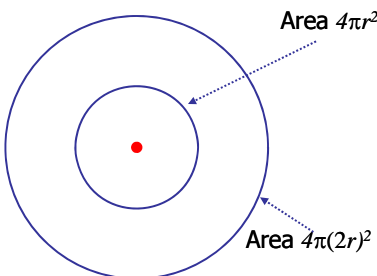
Surface Angle
Important




Light Source Falloff




- Quadratic falloff (point- and spot lights)
 - Brightness of objects depends on power per unit area that hits the object
 - The power per unit area for a point or spot light decreases quadratically with distance






Light Source Falloff




- Non-quadratic falloff
 - Many systems allow for other falloffs
 - Allows for faking effect of area light sources
 - OpenGL / graphics hardware
 - I_0 : intensity of light source
 - \mathbf{x} : object point
 - r : distance of light from \mathbf{x}

$$I_{in}(\mathbf{x}) = \frac{1}{ar^2 + br + c} \cdot I_0$$






Illumination Equation




- For multiple light sources:


$$I = I_a k_a + \sum_p \frac{I_p}{A(d_p)} (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$

- d_p - distance between surface and light source
+ distance between surface and viewer, A – attenuation function








shadingmodel



Light



- Light has color
- Interacts with object color (r,g,b)


$$I = I_a k_a$$


$$I_a = (I_{ar}, I_{ag}, I_{ab})$$

$$k_a = (k_{ar}, k_{ag}, k_{ab})$$


$$I = (I_r, I_g, I_b) = (I_{ar} k_{ar}, I_{ag} k_{ag}, I_{ab} k_{ab})$$

- Blue light on white surface?
- Blue light on red surface?







Lighting in OpenGL




- Light source: amount of RGB light emitted
 - value = percentage of full intensity, e.g., (1.0,0.5,0.5)
 - every light source emits ambient, diffuse, and specular light
- Materials: amount of RGB light reflected
 - value represents percentage reflected e.g., (0.0,1.0,0.5)
- Interaction: multiply components
 - Red light (1,0,0) x green surface (0,1,0) = black (0,0,0)




In OpenGL



- k_a, k_d, k_s - surface color (RGB)
- Modify by `glMaterialfv(GL_FRONT_AND_BACK, pname, RGB[])`
- `pname` - GL_AMBIENT, GL_DIFFUSE, GL_SPECULAR
- Light source properties (also RGB)
`glLightfv(GL_LIGHTi, pname, light[])`




Lighting in OpenGL




```
glLightfv(GL_LIGHT0, GL_AMBIENT, amb_light_rgba );
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif_light_rgba );
glLightfv(GL_LIGHT0, GL_SPECULAR, spec_light_rgba );
glLightfv(GL_LIGHT0, GL_POSITION, position);
glEnable(GL_LIGHT0);


glMaterialfv( GL_FRONT, GL_AMBIENT, ambient_rgba );
glMaterialfv( GL_FRONT, GL_DIFFUSE, diffuse_rgba );
glMaterialfv( GL_FRONT, GL_SPECULAR, specular_rgba );
glMaterialfv( GL_FRONT, GL_SHININESS, n );
```




Light Sources - OpenGL



- Specify parameters
`glLightfv(GL_LIGHTi, GL_POSITION, light[])`
i – between 0 & 8 (or more)
- Directional $[x \ y \ z \ 0]$
- Point source $[x \ y \ z \ 1]$
- Spotlight has extra parameters:
 - `GL_SPOT_DIRECTION`, `GL_SPOT_EXPONENT`,
`GL_SPOT_CUTOFF`
- Area source – too complex for projective pipeline (e.g. OpenGL)



Lighting in Rendering Pipeline



- Notes:
 - Lighting is applied to every **vertex**
 - i.e. the three vertices in a triangle
 - Per-vertex lighting
 - Will later see how the interior points of the triangle obtain their color
 - This process is called **shading**
 - Will discuss in the context of scan conversion