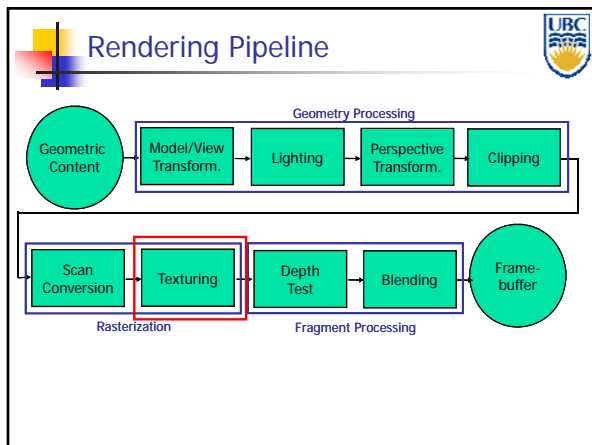


UBC

Chapter 12

Texture Mapping

- UBC
- ### Texture Mapping
- Introduced to increase realism
 - Lighting/shading models not enough
 - Hide geometric simplicity
 - Images convey illusion of geometry
 - Map a brick wall texture on a flat polygon
 - Create bumpy effect on surface
 - Associate 2D information with 3D surface
 - Point on surface corresponds to a point in texture
 - "Paint" image onto polygon



- UBC
- ### Color Texture Mapping
- Define color (RGB) for each point on object surface
 - Two approaches
 - Surface texture map
 - Volumetric texture
-

- UBC
- ### Texture Mapping
- Real life objects non uniform in terms of color & normal
 - To generate realistic objects - reproduce coloring & normal variations = **Texture**
 - Can often replace complex geometric details
-

- UBC
- ### Surface texture
- Define texture pattern over (u,v) domain (Image)
 - Image – 2D array of "texels"
 - Assign (u,v) coordinates to each point on object surface
 - How: depends on surface type
 - For polygons (triangle)
 - Inside – use barycentric coordinates
 - For vertices need mapping function (artist/programmer)
-

Texture Mapping

`glTexCoord2f(s, t)`
`glVertexf(x, y, z, w)`

(u_0, v_0) , (u_1, v_1) , (u_2, v_2)

(u, v) parameterization in OpenGL

Example Texture Map

`glTexCoord2d(1,1);`
`glVertex3d(-x, y, z);`

`glTexCoord2d(0,0);`
`glVertex3d(-x, -y, -z);`

Texture + Object = Mapped Texture

Texture Mapping Example

Hand + Striped Texture = Striped Hand

Hand → Wireframe Hand

Fractional Texture Coordinates

texture image

$(0,0)$, $(1,0)$, $(0,1)$, $(1,1)$

$(0,0.5)$, $(0.25,0.5)$

Texture Coordinates

- Every polygon has object coordinates and texture coordinates
 - object coordinates describe where polygon vertices are on the screen
 - texture coordinates describe texel coordinates of each vertex
 - texture coordinates are interpolated across triangle (like R,G,B,Z)
 - (well, not quite...)
- `glTexCoord2f(TYPE coords)`
 - Other versions for different texture dimensions

Texture Lookup: Tiling and Clamping

- What if s or t is outside the interval $[0...1]$?
- Multiple choices
 - Use fractional part of texture coordinates
 - Cyclic repetition of texture to tile whole surface
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_REPEAT, GL_TEXTURE_WRAP_T, GL_REPEAT, ...)`
 - Clamp every component to range $[0...1]$
 - Re-use color values from texture image border
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_CLAMP, GL_TEXTURE_WRAP_T, GL_CLAMP, ...)`

Tiled Texture Map

Code examples:

```
glTexCoord2d(1, 1);
glVertex3d(x, y, z);
```

```
glTexCoord2d(4, 4);
glVertex3d(x, y, z);
```

Interpolation: Screen vs. World Space

- Screen space (perspective) interpolation incorrect
 - Problem ignored with shading, but artifacts more visible with texturing

OpenGL Details

- How to mix texture & color (replace, blend, etc...)
- Transformations: Change scale, orientation of texture on an object
- Storage: data structure + read format
 - Rule: size always power of 2
- Binding: which image to use

Perspective - Reminder

$$T \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & a & b \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} \quad z_{NDC} = \frac{a \cdot z_{eye} + b}{z_{eye}} = a + \frac{b}{z_{eye}}$$

- Preserves order
 - BUT distorts distances

Texture Mapping

- Texture coordinate interpolation
 - Perspective foreshortening problem
 - Also problematic for color interpolation, etc.

Texture Coordinate Interpolation

- Perspective Correct Interpolation
 - α, β, γ : Barycentric coordinates (2D) of point P
 - s_0, s_1, s_2 : texture coordinates of vertices
 - w_0, w_1, w_2 : homogenous coordinate of vertices

$$s = \frac{\alpha \cdot s_0 / w_0 + \beta \cdot s_1 / w_1 + \gamma \cdot s_2 / w_2}{\alpha / w_0 + \beta / w_1 + \gamma / w_2}$$

- Similarly for t

Texture: Sampling & Reconstruction

Related: Upsampling pixel images

Reconstruction

- How to deal with:
 - pixels that are much larger than texels? (apply filtering, "averaging")
 - pixels that are much smaller than texels? (interpolate)

MIP-mapping

Use "image pyramid" to precompute averaged versions of the texture

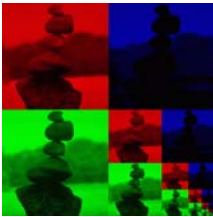
Magnification: Interpolating Textures

- Nearest neighbor
- Bilinear
- Hermite (cubic)

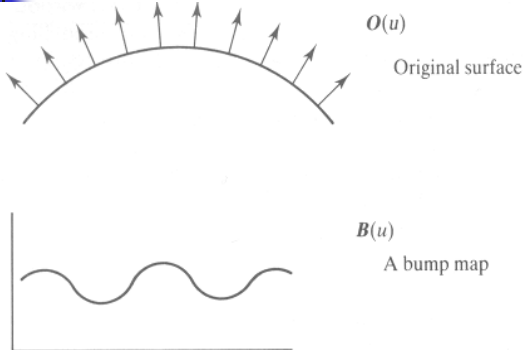
MIP-mapping

MIPmap storage

- Only 1/3 more space required



Bump Mapping




$O(u)$
Original surface

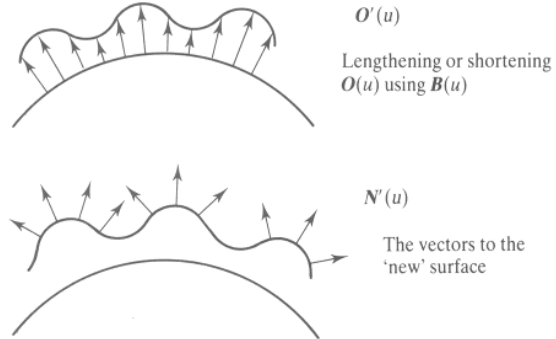
$B(u)$
A bump map

Texture Parameters

- In addition to color can control other material/object properties
 - Reflectance (either diffuse or specular)
 - Surface normal (bump mapping)
 - Transparency
 - Reflected color (environment mapping)



Bump Mapping

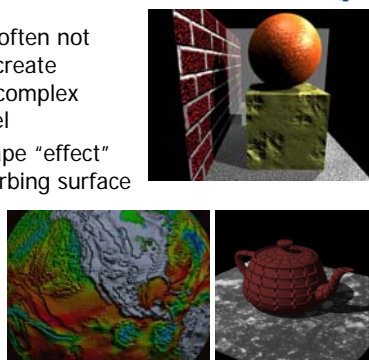


$O'(u)$
Lengthening or shortening $O(u)$ using $B(u)$

$N'(u)$
The vectors to the 'new' surface

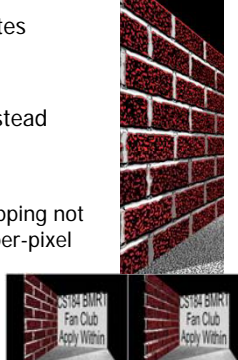
Bump Mapping: Normals As Texture

- Object surface often not smooth – to recreate correctly need complex geometry model
- Can control shape “effect” by locally perturbing surface normal
 - Random
 - Directional




Displacement Mapping

- Bump mapping gets silhouettes wrong
 - Shadows wrong too
- Change surface geometry instead
 - Need to subdivide surface
- GPU support
 - Bump and displacement mapping not directly supported: require per-pixel lighting
 - Modern GPUs allow for programming both yourself

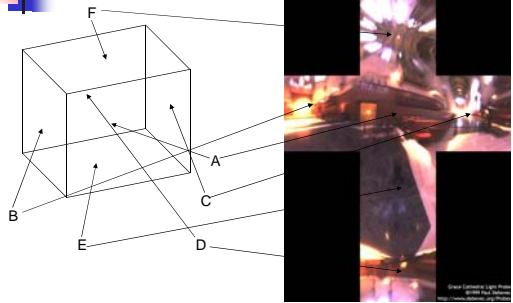


Environment Mapping

- cheap way to achieve reflective effect
 - generate image of surrounding
 - map to object as texture



Cube Mapping




Environment Mapping

- used to model object that reflects surrounding textures to the eye
 - movie example: cyborg in Terminator 2
- different approaches
 - sphere, cube most popular
 - OpenGL support
 - `GL_SPHERE_MAP`, `GL_CUBE_MAP`
 - others possible too


Sphere Mapping

- texture is distorted fish-eye view
 - point camera at mirrored sphere
 - spherical texture mapping creates texture coordinates that correctly index into this texture map



Cube Mapping

- 6 planar textures, sides of cube
 - point camera in 6 different directions, facing out from origin



Volumetric Texture

- Define texture pattern over 3D domain - 3D space containing the object
 - Texture function can be digitized or procedural
 - For each point on object compute texture from point location in space
- Common for natural material/irregular textures (stone, wood, etc...)

