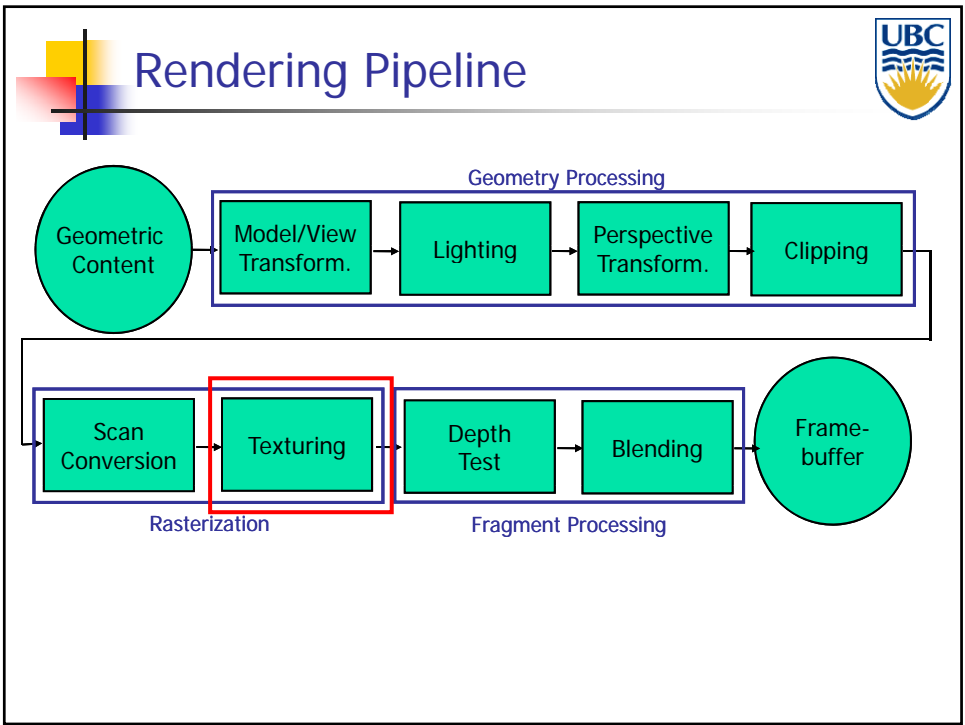





Chapter 12



Texture Mapping




Texture Mapping



- Real life objects non uniform in terms of color & normal
- To generate realistic objects - reproduce coloring & normal variations = **Texture**
- Can often replace complex geometric details




Texture Mapping

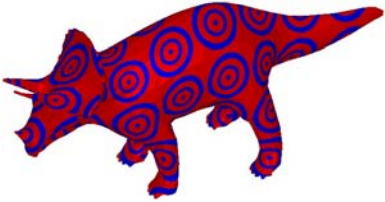
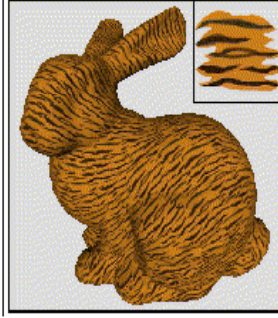



- Introduced to increase realism
 - Lighting/shading models not enough
- Hide geometric simplicity
 - Images convey illusion of geometry
 - Map a brick wall texture on a flat polygon
 - Create bumpy effect on surface
- Associate 2D information with 3D surface
 - Point on surface corresponds to a point in texture
 - "Paint" image onto polygon


Color Texture Mapping



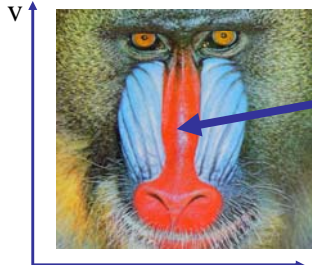
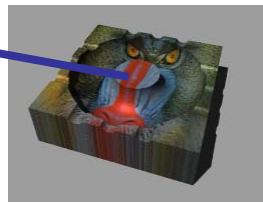
- Define color (RGB) for each point on object surface
- Two approaches
 - Surface texture map
 - Volumetric texture







Surface texture

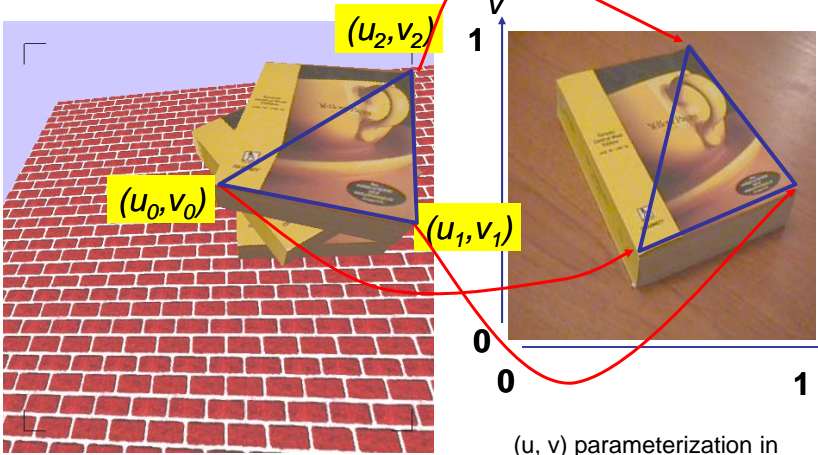


- Define texture pattern over (u,v) domain (Image)
 - Image – 2D array of “texels”
- Assign (u,v) coordinates to each point on object surface
 - How: depends on surface type
- For polygons (triangle)
 - Inside – use barycentric coordinates
 - For vertices need mapping function (artist/programmer)






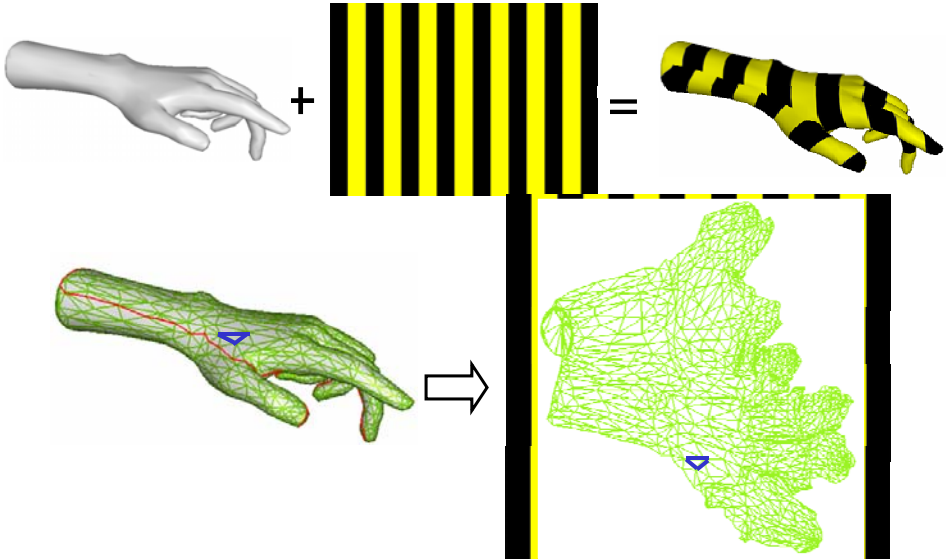
 **Texture Mapping** 



`glTexCoord2f(s, t)`
`glVertexf(x, y, z, w)`



(u, v) parameterization in OpenGL



 **Texture Mapping Example** 



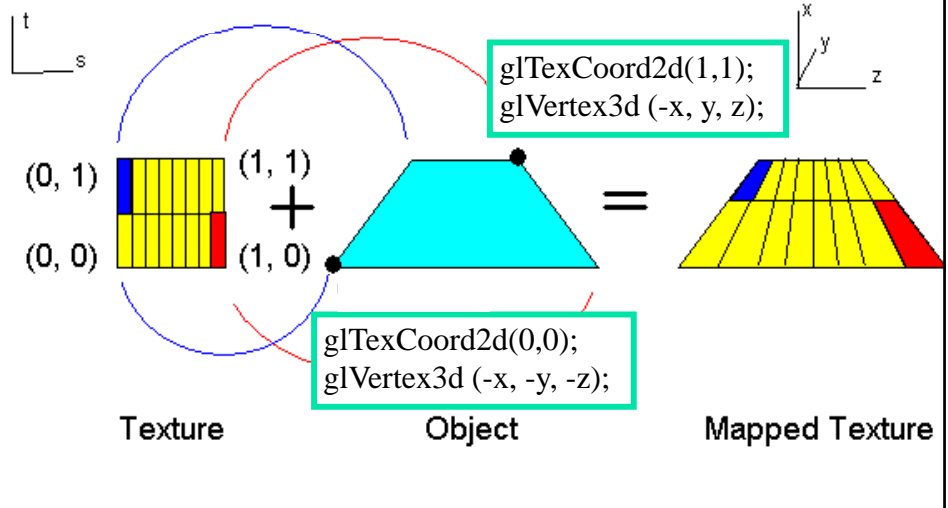



Texture Coordinates

- Every polygon has object coordinates and texture coordinates
 - object coordinates describe where polygon vertices are on the screen
 - texture coordinates describe texel coordinates of each vertex
 - texture coordinates are interpolated across triangle (like R,G,B,Z)
 - (well, not quite...)
- `glTexCoord2f(TYPE coords)`
 - Other versions for different texture dimensions





Example Texture Map




`glTexCoord2d(1,1);
glVertex3d(-x, y, z);`
`glTexCoord2d(0,0);
glVertex3d(-x, -y, -z);`

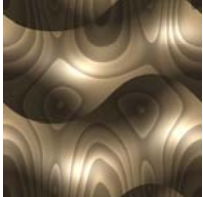
Texture
Object
Mapped Texture



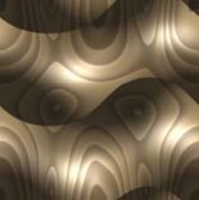
Fractional Texture Coordinates



texture image




(0,1) (1,1)




(0,0) (1,0)


(0,.5) (.25,.5)



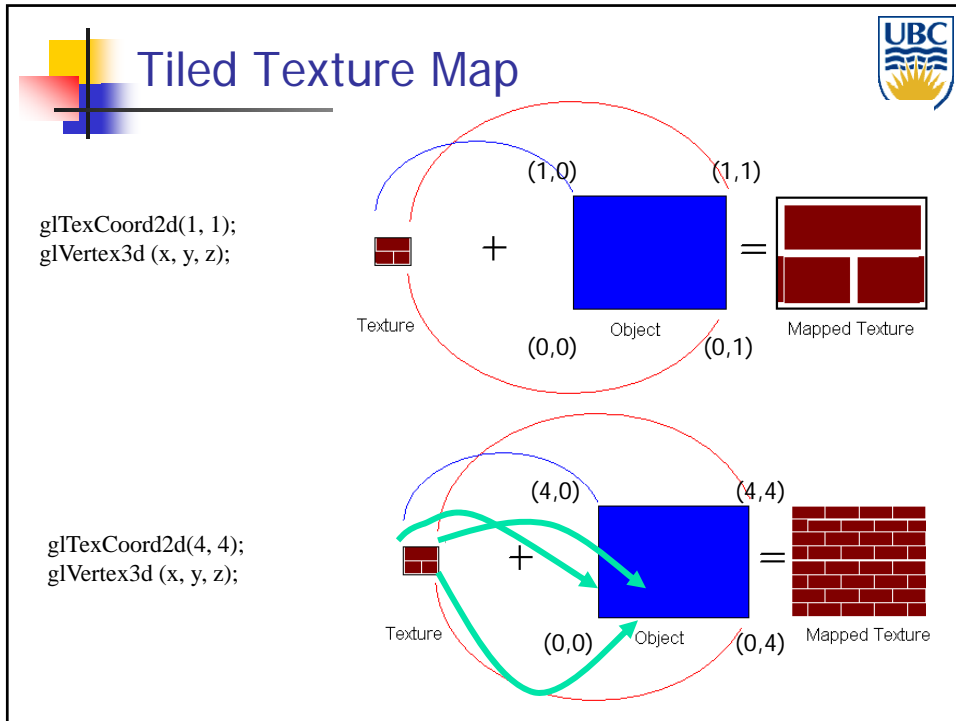
(0,0) (.25,0)



Texture Lookup: Tiling and Clamping



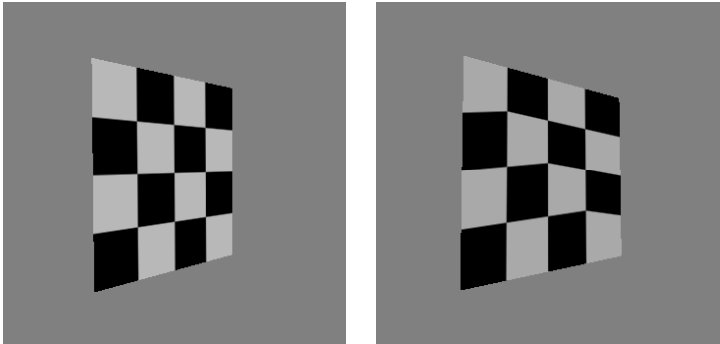
- What if s or t is outside the interval [0...1]?
- Multiple choices
 - Use fractional part of texture coordinates
 - Cyclic repetition of texture to tile whole surface
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_REPEAT, GL_TEXTURE_WRAP_T, GL_REPEAT, ...)`
 - Clamp every component to range [0...1]
 - Re-use color values from texture image border
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_CLAMP, GL_TEXTURE_WRAP_T, GL_CLAMP, ...)`



-
- ## OpenGL Details
- How to mix texture & color (replace, blend, etc...)
 - Transformations: Change scale, orientation of texture on an object
 - Storage: data structure + read format
 - Rule: size always power of 2
 - Binding: which image to use

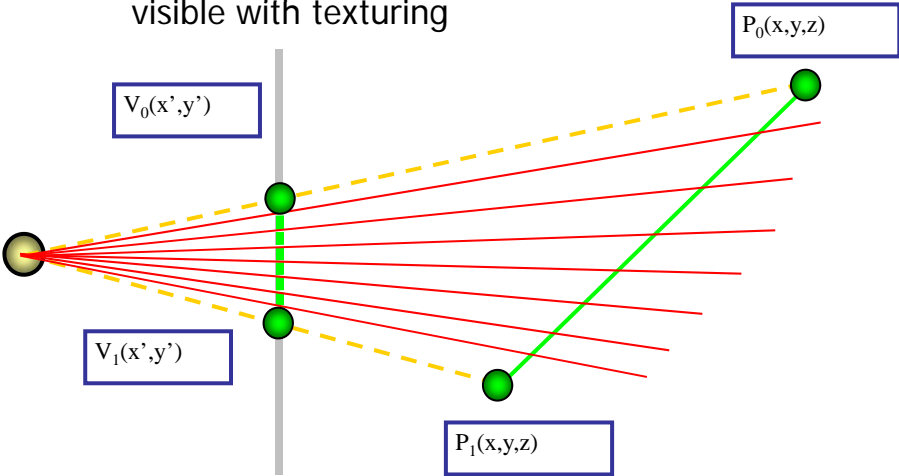
Texture Mapping


- Texture coordinate interpolation
 - Perspective foreshortening problem
 - Also problematic for color interpolation, etc.




Interpolation: Screen vs. World Space

- Screen space (perspective) interpolation incorrect
 - Problem ignored with shading, but artifacts more visible with texturing






Perspective - Reminder




$$T \begin{pmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & a & b \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$z_{NDC} = \frac{a \cdot z_{eye} + b}{z_{eye}} = a + \frac{b}{z_{eye}}$$

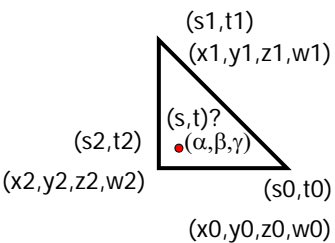
- Preserves order
 - BUT distorts distances



Texture Coordinate Interpolation





- Perspective Correct Interpolation
 - α, β, γ : Barycentric coordinates (2D) of point **P**
 - s_0, s_1, s_2 : texture coordinates of vertices
 - w_0, w_1, w_2 : homogenous coordinate of vertices

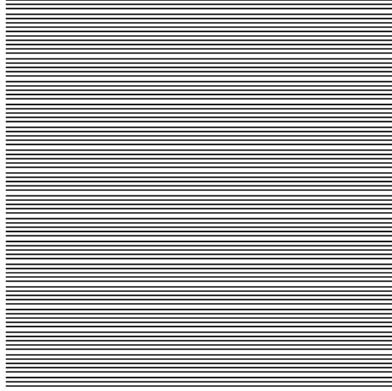


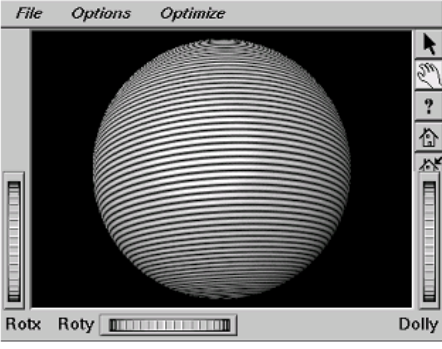
$$s = \frac{\alpha \cdot s_0 / w_0 + \beta \cdot s_1 / w_1 + \gamma \cdot s_2 / w_2}{\alpha / w_0 + \beta / w_1 + \gamma / w_2}$$



- Similarly for t

Texture: Sampling & Reconstruction

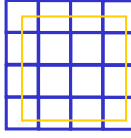


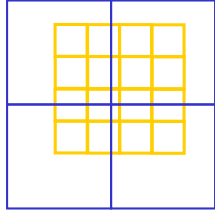


Reconstruction

- How to deal with:
 - pixels that are much larger than texels ?
 (apply filtering, "averaging")

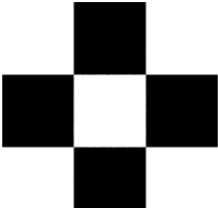
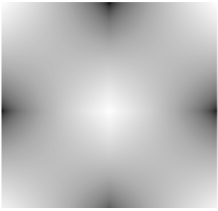
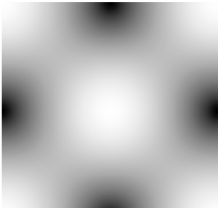

 - pixels that are much smaller than texels ?
 (interpolate)




Magnification: Interpolating Textures


- Nearest neighbor
- Bilinear
- Hermite (cubic)

1	0	1
0	1	0
1	0	1

Related: Upsampling pixel images



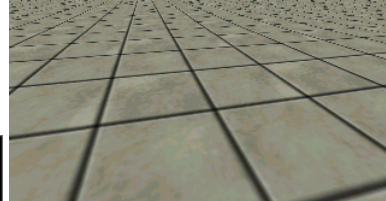
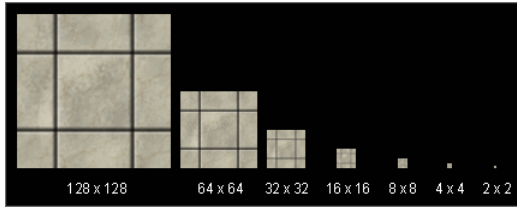




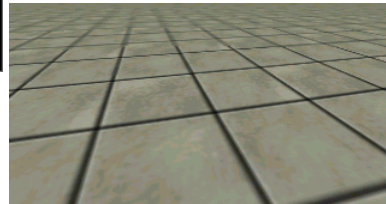
MIP-mapping



Use "image pyramid" to precompute averaged versions of the texture



Without MIP-mapping



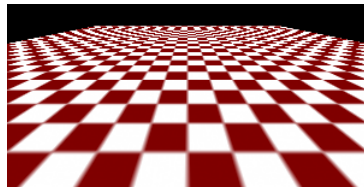
With MIP-mapping



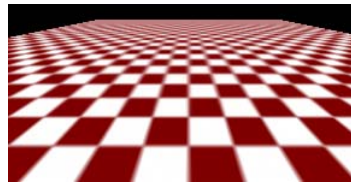
MIP-mapping



without




with




MIPmap storage

- Only 1/3 more space required




Texture Parameters

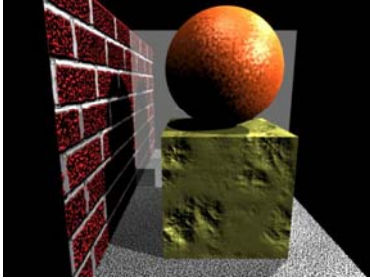
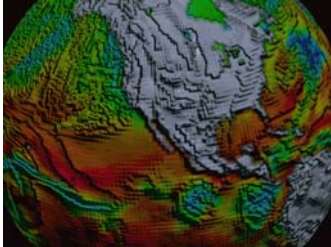
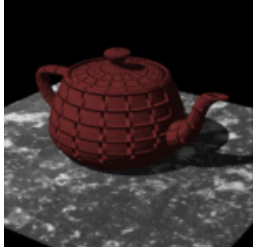
- In addition to color can control other material/object properties
 - Reflectance (either diffuse or specular)
 - Surface normal (bump mapping)
 - Transparency
 - Reflected color (environment mapping)




Bump Mapping: Normals As Texture

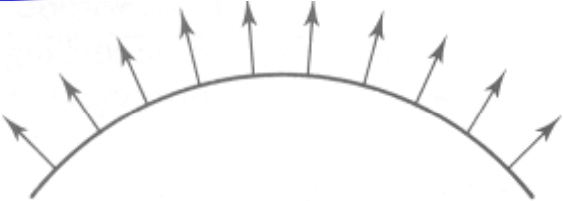


- Object surface often not smooth – to recreate correctly need complex geometry model
- Can control shape “effect” by locally perturbing surface normal
 - Random
 - Directional

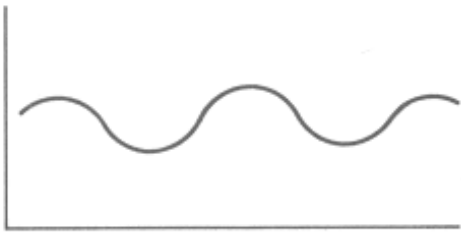




Bump Mapping







$O(u)$
Original surface



$B(u)$
A bump map

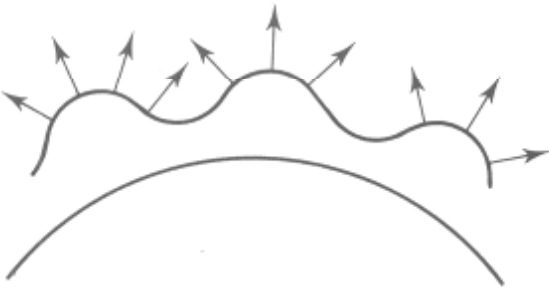
Bump Mapping





$O'(u)$


Lengthening or shortening $O(u)$ using $B(u)$




$N'(u)$



The vectors to the 'new' surface

Displacement Mapping




- Bump mapping gets silhouettes wrong
 - Shadows wrong too
- Change surface geometry instead
 - Need to subdivide surface
- GPU support
 - Bump and displacement mapping not directly supported: require per-pixel lighting
 - Modern GPUs allow for programming both yourself





Environment Mapping



- cheap way to achieve reflective effect
 - generate image of surrounding
 - map to object as texture




Environment Mapping

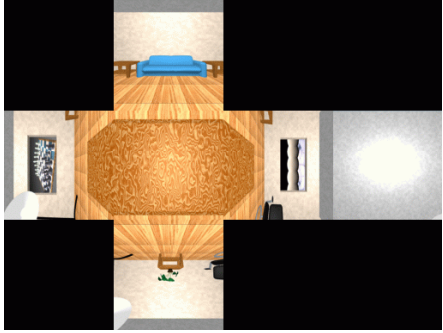



- used to model object that reflects surrounding textures to the eye
 - movie example: cyborg in Terminator 2
- different approaches
 - sphere, cube most popular
 - OpenGL support
 - `GL_SPHERE_MAP`, `GL_CUBE_MAP`
 - others possible too


Cube Mapping

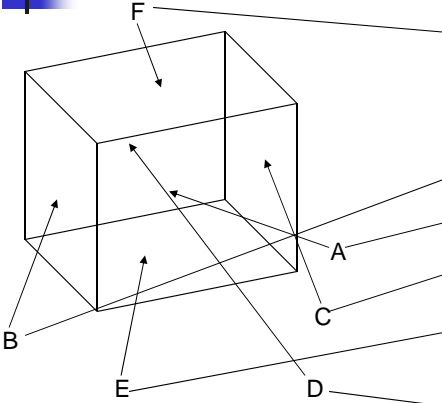


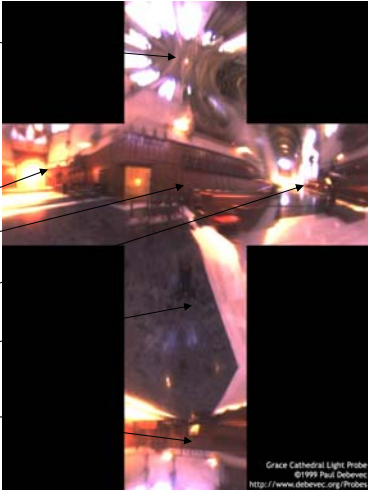
- 6 planar textures, sides of cube
- point camera in 6 different directions, facing out from origin

Cube Mapping







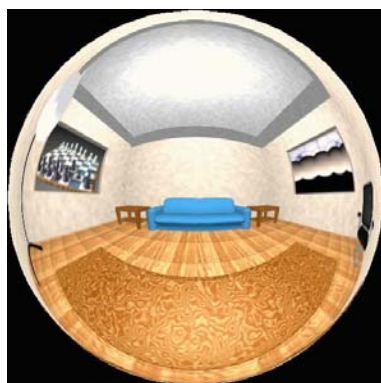
Grace Cathedral Light Probe
 ©1999 Paul Debevec
<http://www.sbbvcs.org/Probe/>



Sphere Mapping



- texture is distorted fish-eye view
 - point camera at mirrored sphere
 - spherical texture mapping creates texture coordinates that correctly index into this texture map



Volumetric Texture



- Define texture pattern over 3D domain - 3D space containing the object
 - Texture function can be digitized or **procedural**
 - For each point on object compute texture from point location in space
- Common for natural material/irregular textures (stone, wood, etc...)

