


Computer Graphics

Illumination Models

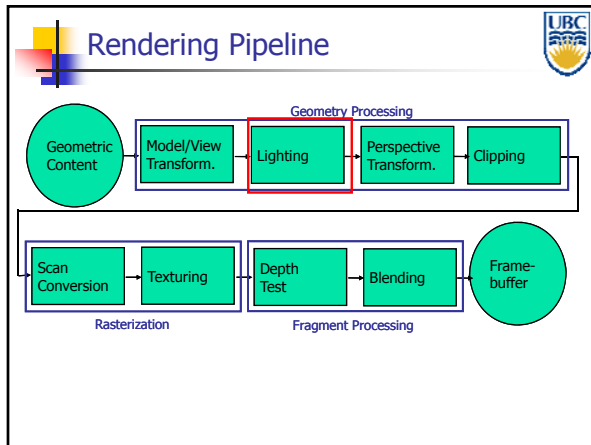
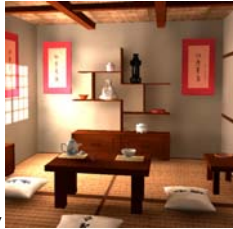
Chapter 6

Lighting




Lighting

- Appearance depends on
 - Light sources, locations, properties
 - Material (surface) properties
 - Viewer position
- Algorithms:
 - Local illumination - Fast
 - "Fake" - Ignore real physics, approximate the look
 - Compute at material, from light to viewer
 - Global illumination - Slow
 - Physically based




Local vs. Global Illumination Models

- Local model - interaction of each object with light
- Global model: interactions between objects




Lighting

- Goal
 - Model the interaction of light with surfaces to render realistic images
- Contributing Factors
 - Light sources
 - Shape and color
 - Surface materials
 - How surfaces reflect light
 - Transport of light
 - How light moves in a scene



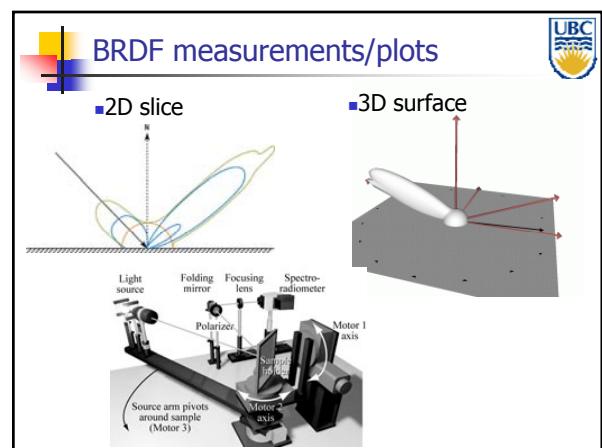
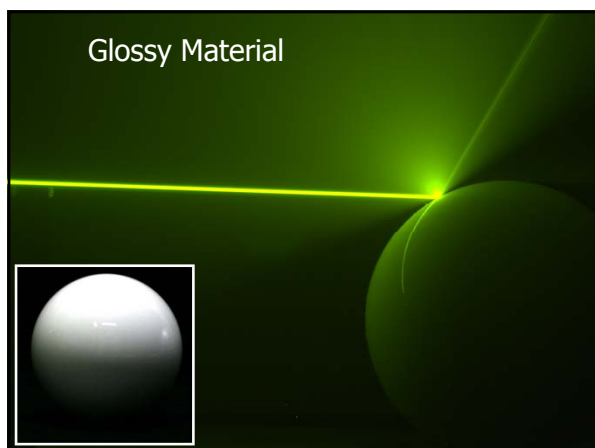
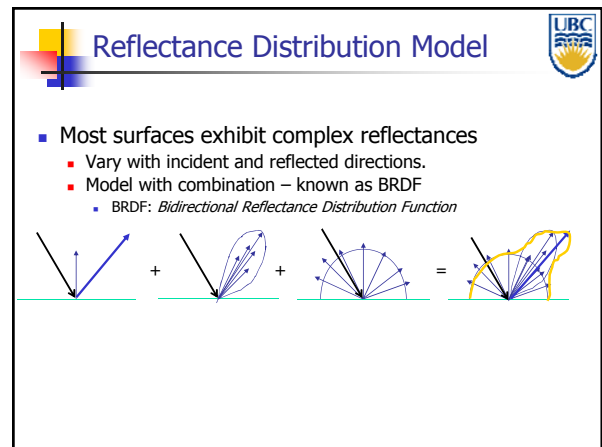
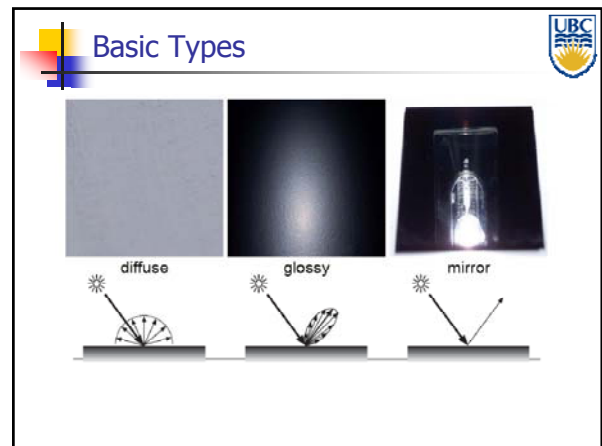
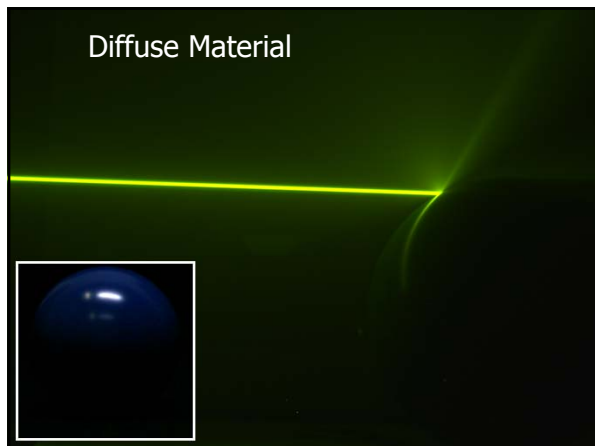
Materials

- Surface reflectance:
 - Illuminate surface point with a ray of light from different directions
 - How much light is reflected in each direction?



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Materials

- Practical Considerations
 - In practice, often simplify (computational efficiency)
 - Derive specific formulas that describe basic reflectance behaviors
 - diffuse, glossy, specular
 - OpenGL choice

Computing Diffuse Reflection

- Depends on **angle of incidence**: angle between surface normal and incoming light
 - $I_{diffuse} = k_d I_{light} \cos \theta$
- In practice use vector arithmetic
 - $I_{diffuse} = k_d I_{light} (\mathbf{n} \cdot \mathbf{l})$
- Always normalize vectors used in lighting
 - \mathbf{n} , \mathbf{l} should be unit vectors
- Scalar (B/W intensity) or 3-tuple or 4-tuple (color)
 - k_d : diffuse coefficient, surface color
 - I_{light} : incoming light intensity
 - $I_{diffuse}$: outgoing light intensity (for diffuse reflection)

Physics of Diffuse Reflection

- Ideal diffuse reflection
 - Very rough surface at the microscopic level
 - Real-world example: chalk
 - Microscopic variations mean incoming ray of light equally likely to be reflected in any direction over the hemisphere
 - Reflected intensity only depends on light direction!

Diffuse Lighting Examples

- Lambertian sphere from several lighting angles:
 - need only consider angles from 0° to 90°

Lambert's "Law"

Lambert's Cosine Law

Intuitively: cross-sectional area of the "beam" intersecting an element of surface area is smaller for greater angles with the normal.

Cosine Law: $E_0 = E \cdot \cos(\theta)$

Angle (θ)	Percentage of Intensity
0°	100%
30°	87%
60°	50%
85°	12%

Light Measurement Handbook by Alex Payer

Physics of Specular Reflection

- Geometry of specular (perfect mirror) reflection
 - Snell's law

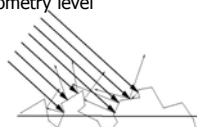
$r = -l + 2(\mathbf{n} \cdot \mathbf{n})$

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Glossy Reflectance

- Snell's law applies to perfect mirror-like surfaces, but aside from mirrors (and chrome) few surfaces exhibit perfect specularity
- How can we capture the "softer" reflections of surface that are glossy, not mirror-like?
- One option: model exact physics
 - Multiple reflections on microgeometry level
- or...

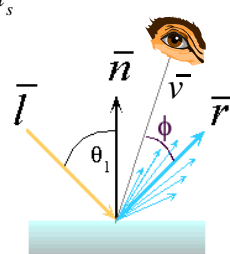


Phong Lighting

- Most common lighting model in computer graphics
 - (Phong Bui-Tuong, 1975)

$$I_{\text{specular}} = k_s I_{\text{light}} (\cos \phi)^{n_s}$$

ϕ : angle between r and view direction v
 n_s : purely empirical constant, varies rate of falloff
 k_s : specular coefficient, highlight color
 no physical basis, works ok in practice

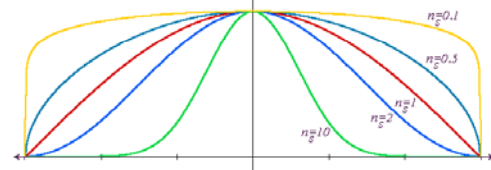


Empirical Approximation

- Expect most reflected light to travel in direction predicted by Snell's Law
- But (because of microscopic surface variations) some light may be reflected in a direction slightly off the ideal reflected ray
- As angle from ideal reflected ray increases, we expect less light to be reflected

Phong Lighting: The n_s Term

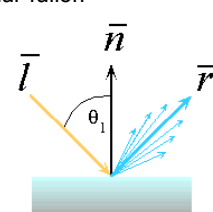
- Phong reflectance term drops off with divergence of viewing angle from ideal reflected ray



Viewing angle - reflected angle

Empirical Approximation

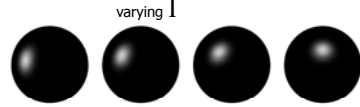
- Angular falloff



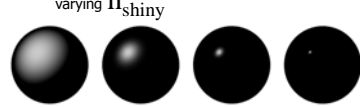
- How might we model this falloff?

Phong Examples

varying l



varying n_{shiny}



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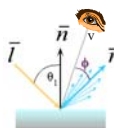
Illumination Models

Calculating Phong Lighting

- compute cosine term of Phong lighting with vectors

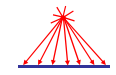
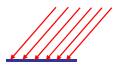
$$I_{\text{specular}} = k_s I_{\text{light}} (\mathbf{v} \cdot \mathbf{r})^{n_s}$$

- \mathbf{v} : unit vector towards viewer/eye
- \mathbf{r} : ideal reflectance direction (unit vector)
- k_s : specular component
 - highlight color
- I_{light} : incoming light intensity



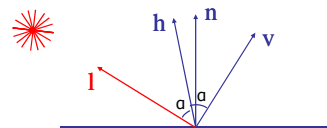
Light Sources

- Point source
 - light originates at a point
 - Rays hit planar surface at different angles
- Parallel source
 - light rays are parallel
 - Rays hit a planar surface at identical angles
 - May be modeled as point source at infinity
 - Directional light*

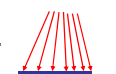


Alternative Model

- Blinn-Phong model (Jim Blinn, 1977)
 - Variation with better physical interpretation
 - \mathbf{h} : halfway vector; r : roughness

$$I_{\text{specular}} = k_s \cdot (\mathbf{h} \cdot \mathbf{n})^{1/r} \cdot I_{\text{light}}; \text{ with } \mathbf{h} = (\mathbf{l} + \mathbf{v}) / 2$$


Light Sources

- Area source
 - Light originates at finite area in space.
 - In-between point and parallel sources
- Spotlights
 - position, direction, angle
- Ambient light (environment light)
 - Hack for replacing true global illumination
 - (light bouncing off from other objects)

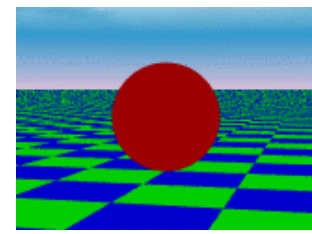




Materials (last bit)

- Light is linear
 - If multiple rays illuminate the surface point the result is just the sum of the individual reflections for each ray

Ambient Light Sources

- Scene lit only with an ambient light source



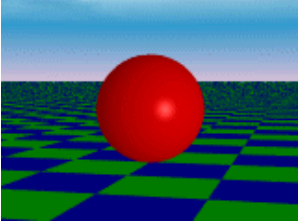
- Light Position Not Important
- Viewer Position Not Important
- Surface Angle Not Important

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Directional Light Sources

- Scene lit with directional and ambient light



Surface Angle Important

Light Position Not Important

Viewer Position Not Important

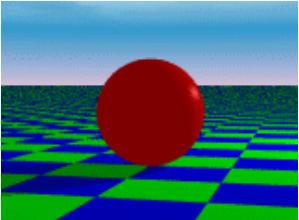
Light Source Falloff

- Non-quadratic falloff
- Many systems allow for other falloffs
- Allows for faking effect of area light sources
- OpenGL / graphics hardware
 - I_0 : intensity of light source
 - x : object point
 - r : distance of light from x

$$I_m(x) = \frac{1}{ar^2 + br + c} \cdot I_0$$

Point Light Sources

- Scene lit with ambient and point light source




Light Position Important

Viewer Position Important

Surface Angle Important

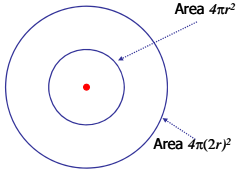
Ambient Light

- non-directional light – environment light
- Object illuminated with same light everywhere
 - Looks like silhouette
- Illumination equation $I = I_a k_a$
 - I_a - ambient light intensity
 - k_a - fraction of this light reflected from surface
 - Defines object color



Light Source Falloff

- Quadratic falloff (point- and spot lights)
- Brightness of objects depends on power per unit area that hits the object
- The power per unit area for a point or spot light decreases quadratically with distance




Illumination Equation

- For multiple light sources:

$$I = I_a k_a + \sum_p \frac{I_p}{A(d_p)} (k_d (n \cdot l_p) + k_s (r_p \cdot v)^n)$$

- d_p - distance between surface and light source + distance between surface and viewer, A – attenuation function




Computer Graphics

Illumination Models

Light

- Light has color
- Interacts with object color (r,g,b)
 $I = I_a k_a$
 $I_a = (I_{ar}, I_{ag}, I_{ab})$
 $k_a = (k_{ar}, k_{ag}, k_{ab})$
 $I = (I_r, I_g, I_b) = (I_{ar}k_{ar}, I_{ag}k_{ag}, I_{ab}k_{ab})$

- Blue light on white surface?
- Blue light on red surface?



Lighting in OpenGL

```
glLightfv(GL_LIGHT0, GL_AMBIENT, amb_light_rgba );  
glLightfv(GL_LIGHT0, GL_DIFFUSE, dif_light_rgba );  
glLightfv(GL_LIGHT0, GL_SPECULAR, spec_light_rgba );  
glLightfv(GL_LIGHT0, GL_POSITION, position);  
glEnable(GL_LIGHT0);  
  
glMaterialfv( GL_FRONT, GL_AMBIENT, ambient_rgba );  
glMaterialfv( GL_FRONT, GL_DIFFUSE, diffuse_rgba );  
glMaterialfv( GL_FRONT, GL_SPECULAR, specular_rgba );  
glMaterialfv( GL_FRONT, GL_SHININESS, n );
```

Lighting in OpenGL

- Light source: amount of RGB light emitted
 - value represents percentage of full intensity, e.g., (1.0,0.5,0.5)
 - every light source emits ambient, diffuse, and specular light
- Materials: amount of RGB light reflected
 - value represents percentage reflected e.g., (0.0,1.0,0.5)
- Interaction: multiply components
 - Red light (1,0,0) x green surface (0,1,0) = black (0,0,0)

Light Sources - OpenGL

- Specify parameters
`glLightfv(GL_LIGHTi, GL_POSITION, light[])`
i – between 0 & 8 (or more)
- Directional [x y z 0]
- Point source [x y z 1]
- Spotlight has extra parameters:
 - `GL_SPOT_DIRECTION`, `GL_SPOT_EXPONENT`, `GL_SPOT_CUTOFF`
- Area source – too complex for projective pipeline (e.g. OpenGL)

In OpenGL

- k_a, k_d, k_s - surface color (RGB)
- Modify by `glMaterialfv(GL_FRONT_AND_BACK, pname, RGB[])`
`pname` - `GL_AMBIENT`, `GL_DIFFUSE`, `GL_SPECULAR`
- Light source properties (also RGB)
`glLightfv(GL_LIGHTi, pname, light[])`

Lighting in Rendering Pipeline

- Notes:
 - Lighting is applied to every **vertex**
 - i.e. the three vertices in a triangle
 - Per-vertex lighting
 - Will later see how the interior points of the triangle obtain their color
 - This process is called **shading**
 - Will discuss in the context of scan conversion