
A decorative graphic consisting of a blue square, a red square, and a yellow square, with a black crosshair overlaid on them.


## Chapter 4: Transformations- Transforming Normals, Hierarchies and OpenGL, Assignment 2

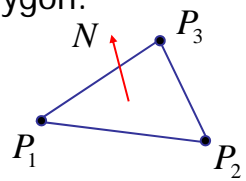
A decorative graphic consisting of a blue square, a red square, and a yellow square, with a black crosshair overlaid on them.

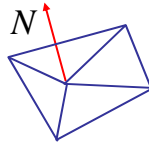
## Transforming Normals




## Computing Normals




- polygon:  

$$N = (P_2 - P_1) \times (P_3 - P_1)$$
- assume vertices ordered CCW when viewed from visible side of polygon
- normal for a vertex
  - used for lighting
  - supplied by model (i.e., sphere), or computed from neighboring polygons







## Transforming Normals



- What is a normal?
  - **Vector**
    - Orthogonal (perpendicular) to plane/surface
  - Do standard transformations preserve orthogonality?



## Planes and Normals




- Plane - all points where  $N \cdot P = 0$


$$P = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}, N = \begin{bmatrix} A \\ B \\ C \\ 0 \end{bmatrix}$$

- Implicit form

$$\text{Plane} = A \cdot x + B \cdot y + C \cdot z + D$$



## Finding Correct Normal Transform



- transform a plane

$$\begin{matrix} P \\ N \end{matrix} \longrightarrow \begin{matrix} P' = MP \\ N' = QN \end{matrix} \quad \begin{matrix} \text{Given } M, \\ \text{find } Q \end{matrix}$$

$N'^T P' = 0$  stay perpendicular

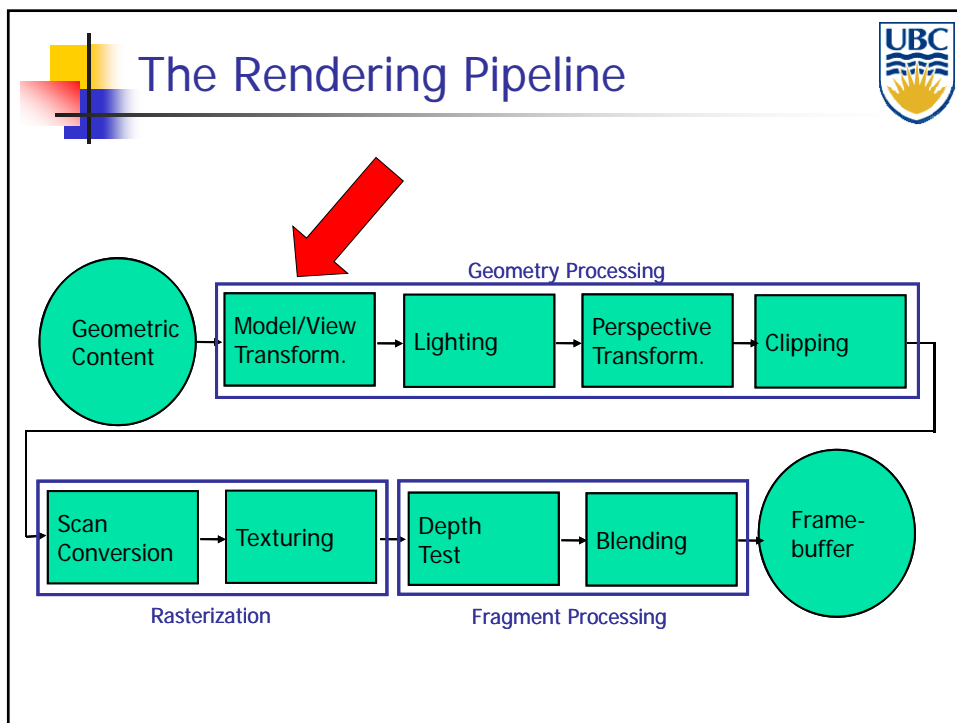
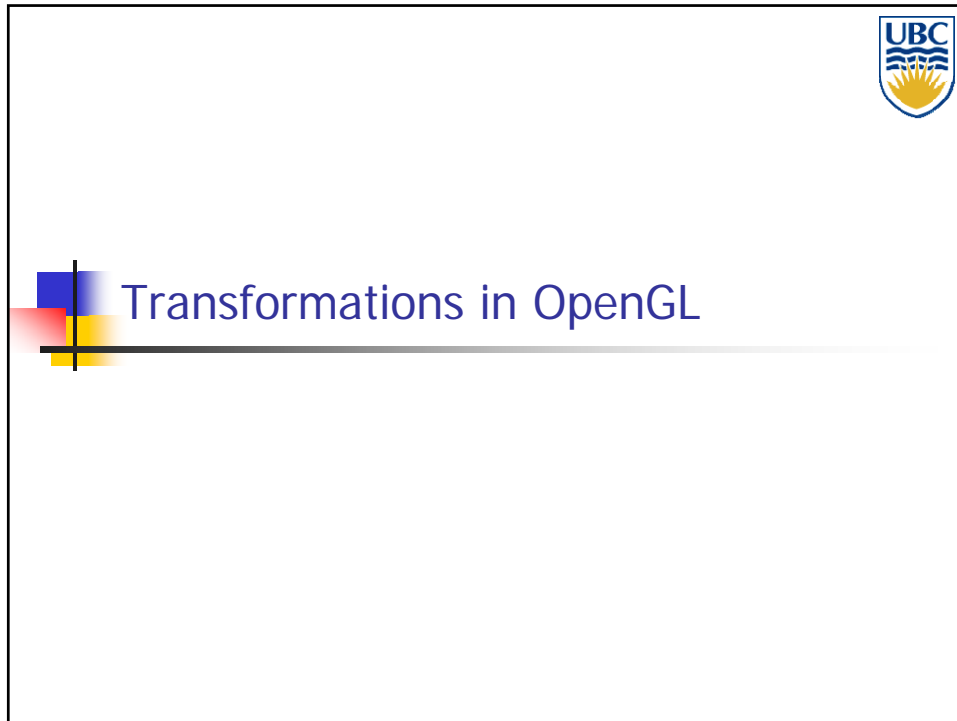
$(QN)^T (MP) = 0$  substitute from above


$N^T Q^T MP = 0$   $(AB)^T = B^T A^T$

$Q^T M = I$   $N^T P = 0$


$$Q = (M^{-1})^T$$

Normal transformed by  
*transpose of the inverse* of the  
modeling transformation







## Modeling Transformation



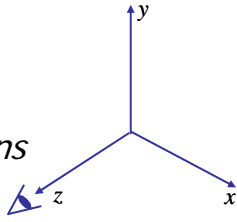
- Purpose:
  - Map geometry from local object coordinate system into a global world coordinate system
  - Same as placing objects
- Transformations:
  - Arbitrary affine transformations are possible
    - More complex transformations may be desirable
      - Freeform deformations
    - Not available in hardware




## Viewing Transformation




- Purpose:
  - Map geometry from *world coordinate system* into *camera coordinate system*
  - Camera coordinate system is **right-handed**, viewing direction is *negative z-axis*
  - Same as placing camera
- Transformations:
  - Usually only *rigid body transformations*
    - Rotations and translations
  - Objects have same size and shape in camera and world coordinates







## Model/View Transformation



- Combine modeling and viewing transform
  - Combine into single matrix
  - Saves computation time
    - if many points are to be transformed
  - Possible because viewing transformation directly follows modeling transformation without intermediate operations



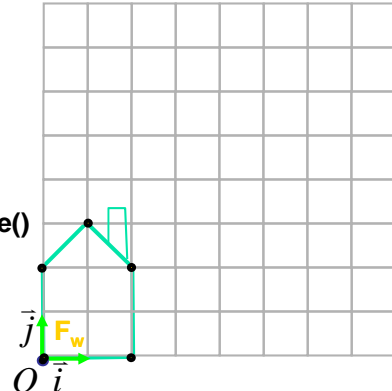
## Transformations in OpenGL




```
glMatrixMode(GL_MODELVIEW);
glLoadIdentity();


glBegin(GL_LINE_LOOP);
glVertex2f(0,0);
glVertex2f(2,0);
glVertex2f(2,2);
glVertex2f(1,3);
glVertex2f(0,2);
glEnd();
```

} DrawHouse()





## Transformations in OpenGL



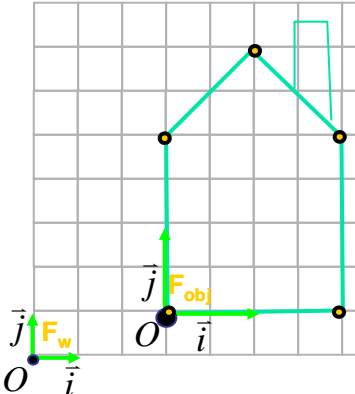
$$\begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}_w = \begin{bmatrix} 2 & 0 & 0 & 3 \\ 0 & 2 & 0 & 1 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}_{obj}$$


```

GLfloat T[16] = { 2,0,0,0, 0,2,0,0,
                  0,0,2,0 3,1,0,1};


glMatrixMode(GL_MODELVIEW);
glLoadMatrixf(T);

DrawHouse();
    
```





## Transformations in OpenGL



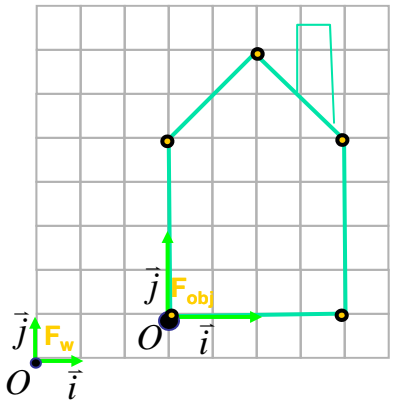
- An easier way to do the same thing....


```

glMatrixMode(GL_MODELVIEW);
glLoadIdentity();


glTranslatef(3,1,0);
glScale(2,2,2);

DrawHouse();
    
```






## Matrix Operations in OpenGL




- 2 Matrices:
  - Model/view matrix M
  - Projective matrix P
- Example:
 

```

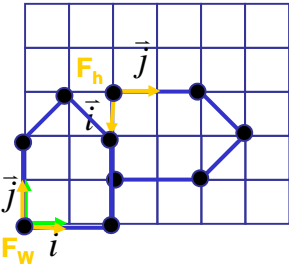
glMatrixMode( GL_MODELVIEW );
glLoadIdentity(); // M=Id
glRotatef( angle, x, y, z ); // M= R(α)*Id
glTranslatef( x, y, z ); // M= T(x,y,z)*R(α)*Id
glMatrixMode( GL_PROJECTION );
glRotatef( ... ); // P= ...
            
```



## Composing Transformations

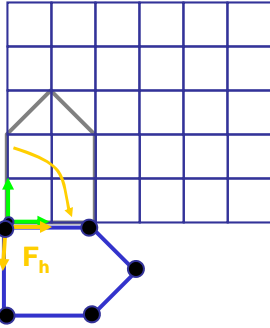


suppose we want



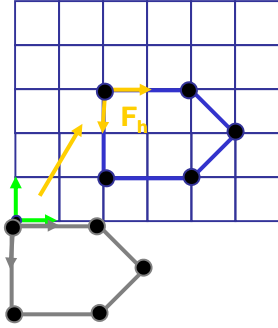
$F_h$

Rotate(z,-90)



$P_A = Rot(z,-90) P_h$


Translate(2,3,0)




$P_W = Trans(2,3,0) P_A$

$P_W = Trans(2,3,0) Rot(z,-90) P_h$





## Composing Transformations



$$P_w = \text{Trans}(2,3,0)\text{Rot}(z,-90)P_h$$


- R-to-L: interpret operations wrt fixed coords
  - moving object
- L-to-R: interpret operations wrt local coords
  - changing coordinate system
- OpenGL (L-to-R, local coords)

```
glTranslatef(2,3,0);
glRotatef(-90,0,0,1);
DrawHouse();
```


$$M_{MV} = \text{Trans}(2,3,0) \cdot M_{MV}$$

$$M_{MV} = \text{Rot}(z,-90)M_{MV}$$


**updates current transformation matrix  
by postmultiplying**




## Post Multiplication



- Composite transformation is now just the product of a few matrixes
- Rather than multiply each point sequentially with 3 matrices, first multiply the matrices, then multiply each point with only one (composite) matrix
  - Much faster for large # of points!
  - Same reason to use homogeneous coordinates



## Interpreting Composite OpenGL Transformations



- Example from earlier lectures:
  - Rotation around arbitrary center
  - In OpenGL:


```
// initialization of matrix
glMatrixMode( GL_MODELVIEW );
glLoadIdentity();

glTranslatef( 4, 3 );
glRotatef( 30, 0.0, 0.0, 1.0 );
glTranslatef( -4, -3 );


glBegin( GL_TRIANGLES );
// specify object geometry...
```

Top-to-bottom:  
transf. of  
coordinate frame

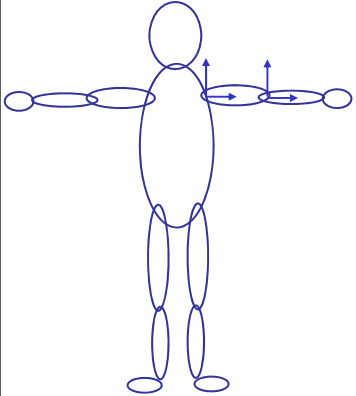
Bottom-to-top:  
transf. of  
object



## Transformation Hierarchies

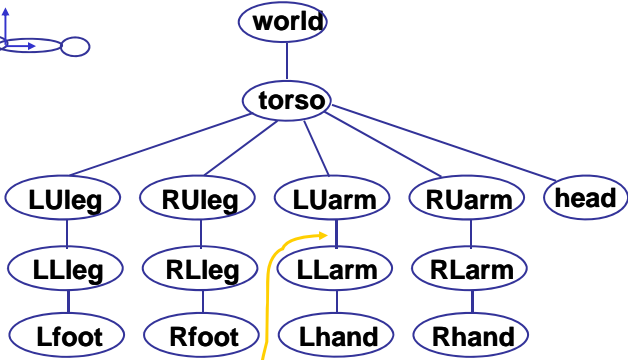
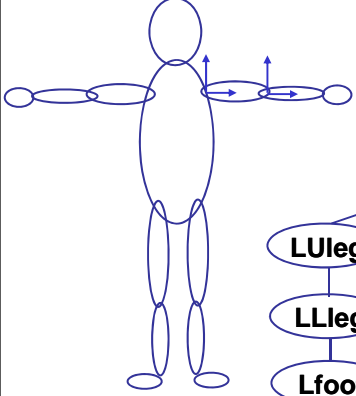


## Transformation Hierarchies




- scene may have a hierarchy of coordinate systems
  - Multiple objects, multiple joint links, ...
  - stores matrix at each level with incremental transform from parent's coordinate system

## Transformation Hierarchies




```
graph TD; world((world)) --- torso((torso)); torso --- LUleg((LUleg)); torso --- RUleg((RUleg)); torso --- LUarm((LUarm)); torso --- RUarm((RUarm)); torso --- head((head)); LUleg --- LLleg((LLleg)); RUleg --- RLleg((RLleg)); LUarm --- LLarm((LLarm)); RUarm --- RLarm((RLarm)); LLleg --- Lfoot((Lfoot)); RLleg --- Rfoot((Rfoot)); LLarm --- Lhand((Lhand)); RLarm --- Rhand((Rhand));
```

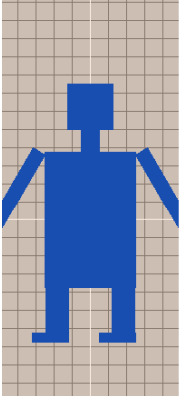
$\text{rot}(z, \theta) \text{ trans}(0.30, 0, 0)$



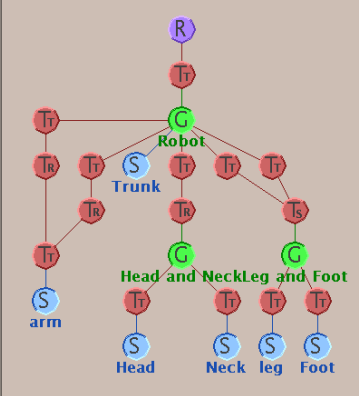
## Check out: Brown Applets




<http://www.cs.brown.edu/exploratories/freeSoftware/catalogs/scenegraphs.html>




Have a look later

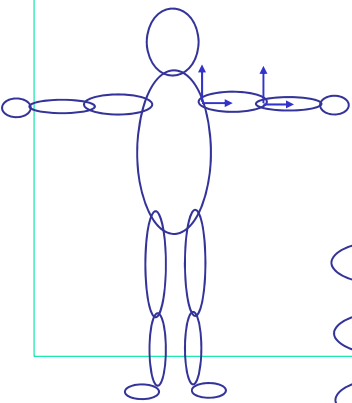


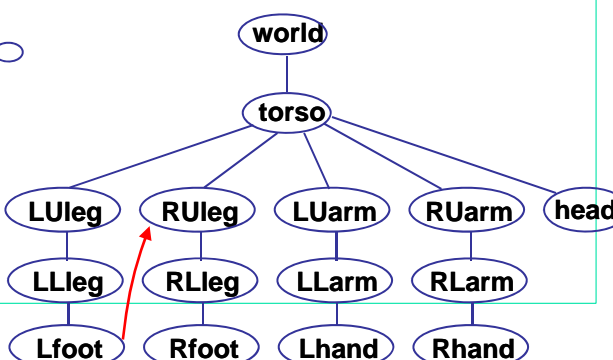



## Matrix Stacks




- Avoiding unnecessary computation when incremental processing makes no sense
  - Using inverse to return to origin..





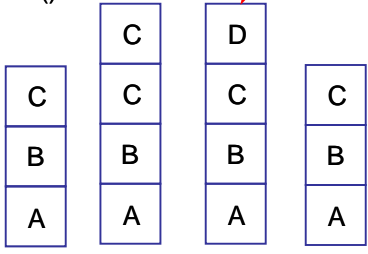


## Matrix Stacks




`glPushMatrix()`  
`glPopMatrix()`


$D = C \text{ scale}(2,2,2) \text{ trans}(1,0,0)$



```
DrawSquare()
glPushMatrix()
glScale3f(2,2,2)
glTranslate3f(1,0,0)
DrawSquare()
glPopMatrix()
```



## Modularization

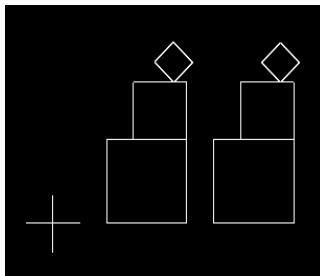



- Drawing a scaled square
  - Push/pop ensures no coord system change

```
void drawBlock(float k) {
    glPushMatrix();


    glScalef(k,k,k);
    glBegin(GL_LINE_LOOP);
    glVertex3f(0,0,0);
    glVertex3f(1,0,0);
    glVertex3f(1,1,0);
    glVertex3f(0,1,0);
    glEnd();

    glPopMatrix();
}
```






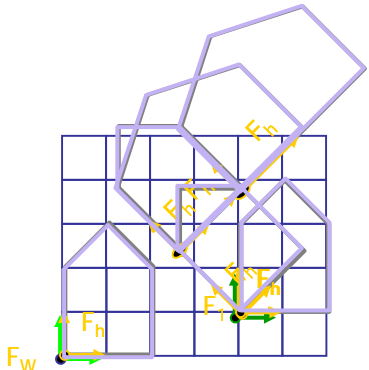

## Matrix Stacks




- Advantages
  - No need to compute inverse matrices all the time
  - Modularize changes to pipeline state
  - Avoids incremental changes to coordinate systems
    - Accumulation of numerical errors
- Practical issues
  - In graphics hardware, depth of matrix stacks is limited
    - Typically 16 for model/view and ~4 for projective matrix




## Transformation Hierarchy Examples

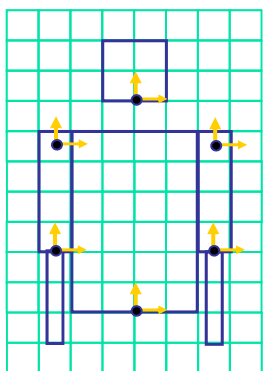


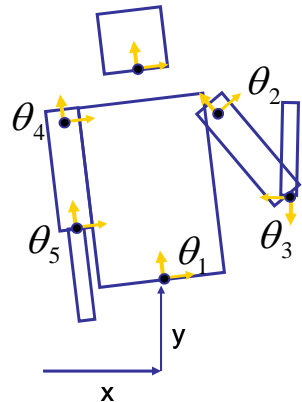
```
glLoadIdentity();  
glTranslatef(4,1,0);  
glPushMatrix();  
glRotatef(45,0,0,1);  
glTranslatef(0,2,0);  
glScalef(2,1,1);  
glTranslate(1,0,0);  
glPopMatrix();
```



## Transformation Hierarchy Examples









```

glTranslate3f(x,y,0);
glRotatef(  $\theta_1$ ,0,0,1);
DrawBody();
glPushMatrix();
  glTranslate3f(0,7,0);
  DrawHead();
glPopMatrix();
glPushMatrix();
  glTranslate(2.5,5.5,0);
  glRotatef(  $\theta_2$ ,0,0,1);
  DrawUArm();
  glTranslate(0,-3.5,0);
  glRotatef(  $\theta_3$ ,0,0,1);
  DrawLArm();
glPopMatrix();
... (draw other arm)

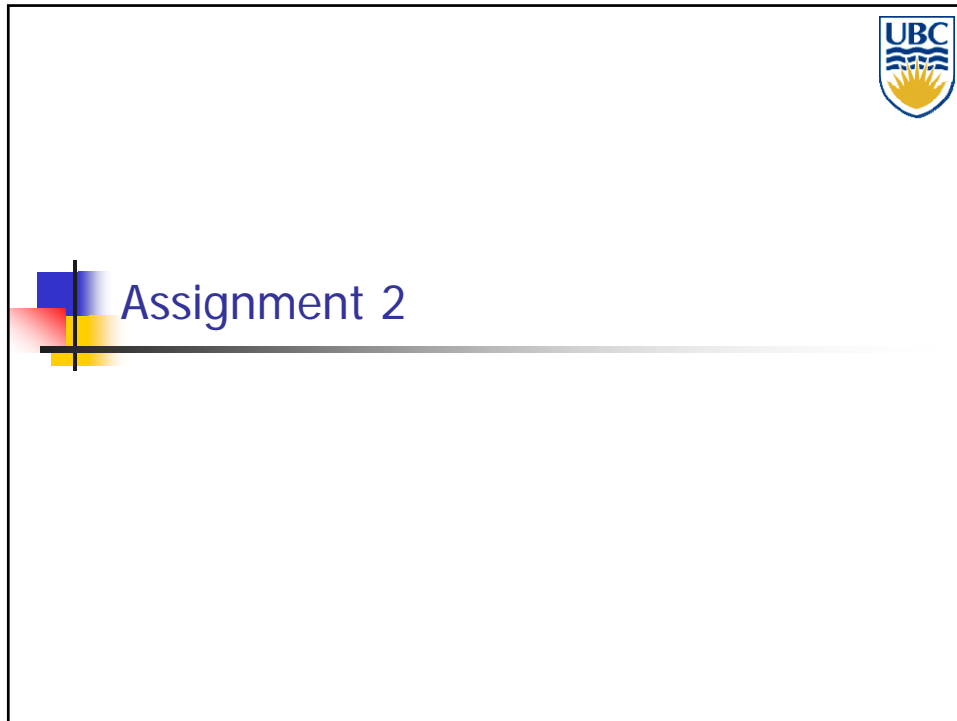
```



## Hierarchical Modeling



- Advantages
  - Define object once, instantiate multiple copies
  - Transformation parameters often good control knobs
  - Maintain structural constraints if well-designed
- Limitations
  - Expressivity: not always the best controls
  - Can't do closed kinematic chains
    - Keep hand on hip




Assignment 2


- Out last week, due **4pm Fri Oct 14, 2011**
  - [http://www.ugrad.cs.ubc.ca/~cs314/Vsep2011/a2/programming\\_a2.pdf](http://www.ugrad.cs.ubc.ca/~cs314/Vsep2011/a2/programming_a2.pdf)
  - Start very soon!
  - Build and animate a giraffe made out of spheres and 4x4 matrices
    - think cartoon, not beauty
  - Template code - program shell, Makefile
    - <http://www.ugrad.cs.ubc.ca/~cs314/Vsep2011/a2/a2.tar.gz>

The slide features a decorative graphic on the left side consisting of overlapping colored squares (yellow, red, blue) and a black crosshair. The UBC logo is positioned in the top right corner.






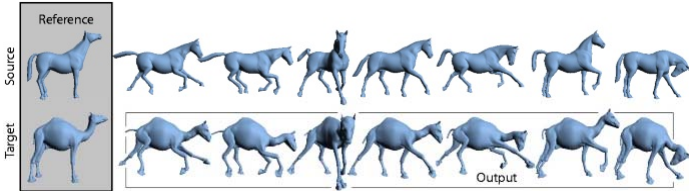

## Advice



- **Draw one section at a time**
  - Ensure you're constructing hierarchy correctly
  - Use body as scene graph root
  - Continue with attached parts
- Finish all required parts before...
  - ...Adding extra links or DOFs
  - ...Going for extra credit
- Visual debugging
  - Draw the current coord system



## Advanced transformations example



- **Deformation Transfer [Sumner'05]**
  - Use transformation gradients (transformation without translation) as per-triangle encoding of motion

Advanced transformations example 

- Deformation Transfer

