

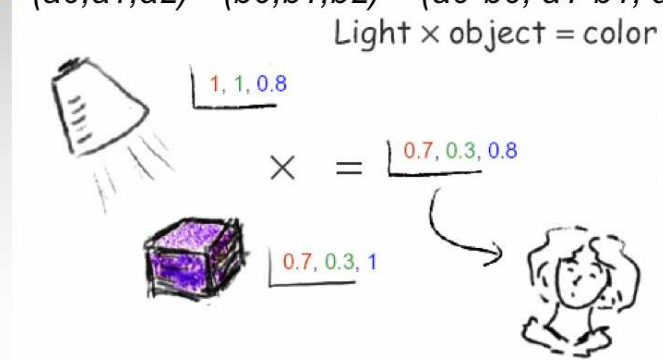
# Color

## CPSC 314

## So far in this Course: Simple Model of Color

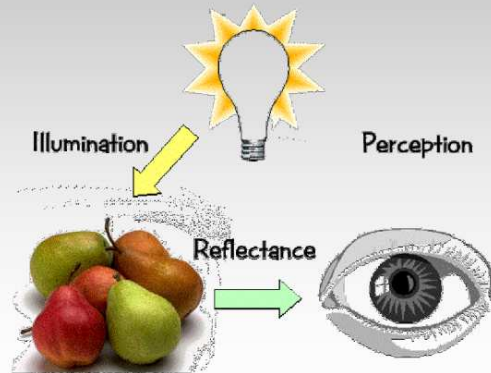
- Simple model based on RGB triples
- Component-wise multiplication of colors  
$$-(a_0, a_1, a_2) * (b_0, b_1, b_2) = (a_0 * b_0, a_1 * b_1, a_2 * b_2)$$

Light  $\times$  object = color



## Basics Of Color

### **Elements of color:**



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## Basics of Color

### **Physics**

- Illumination
  - *Electromagnetic spectra*
- Reflection
  - *Material properties*
  - *Surface geometry and microgeometry (i.e., polished versus matte versus brushed)*

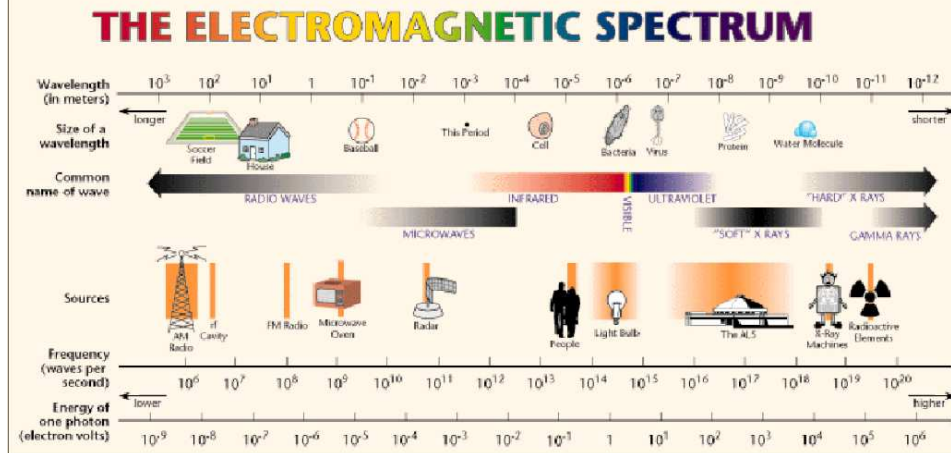
### **Perception**

- Physiology and neurophysiology
- Perceptual psychology

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# Electromagnetic Spectrum



# Light Sources

**Common light sources differ in the kind of spectrum they emit:**

- Continuous spectrum
  - Energy is emitted at all wavelengths
    - Blackbody radiation
    - Tungsten light bulbs
    - Certain fluorescent lights
    - Sunlight
    - Electrical arcs
- Line spectrum
  - Energy is emitted at certain discrete frequencies

## Blackbody Radiation

### **Black body**

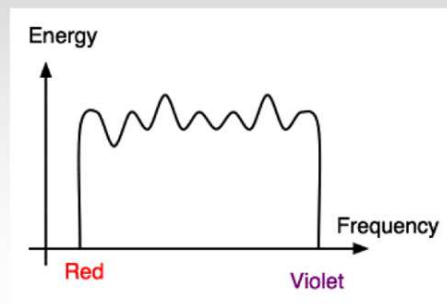
- Dark material, so that reflection can be neglected
- Spectrum of emitted light changes with temperature
  - *This is the origin of the term “color temperature”*
    - E.g. when setting a white point for your monitor
  - *Cold: mostly infrared*
  - *Hot: redish*
  - *Very hot: bluish*
- Demo:



<http://www.mhhe.com/physsci/astronomy/applets/Blackbody/frame.html>

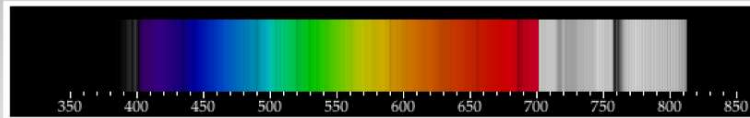
## White Light

- Sun or light bulbs emit all frequencies within the visible range to produce what we perceive as the "white light"
- But the exact tone depends on the emitted spectrum

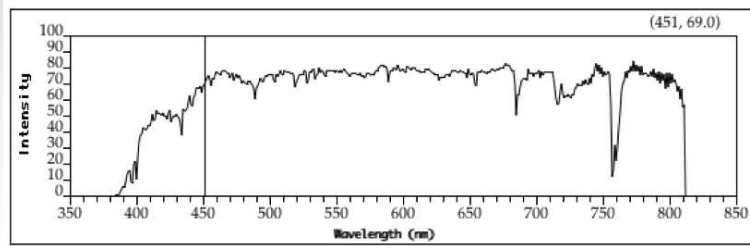




# Sunlight Spectrum



Emission Graph



Electromagnetic Spectrum

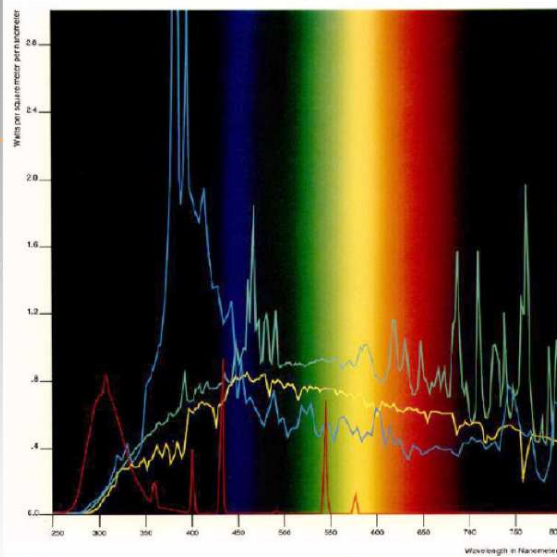
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# Continuous Spectrum

## Example:

- Sunlight
- Various "daylight" lamps

A Comparison of Relative Spectral Energy Distribution



**Sunlight**  
Data: "Sunlight" (1000 W/m², 1000 nm, 1000 nm)  
Measured at 1000 nm

**Sunlight Carbon LED**  
Measured at 1000 nm

**Xenon Arc Lamp**  
Measured at 1000 nm

**FS-40 Fluorescent Sun Lamp**  
Measured at 1000 nm

Accelerated weathering devices simulate the effects of sunlight on various substrates. This graph illustrates the spectral energy distribution as a function of wavelength produced by a number of artificial light sources. The letter (L) in the wavelength appears on the graph (i.e., shorter wavelengths) the higher the energy output generated. The graph compares the energy output to terrestrial sunlight. The above frequency distribution is just light, the more reliable and accurate the results of the experiment. Accelerated weathering

Devices that emit larger amounts of shorter wavelengths (i.e., ultraviolet) cause shorter periods of time, and often complete less work than those that emit light with longer wavelengths closer to the distribution of terrestrial sunlight.

**CIBA-GEIGY**

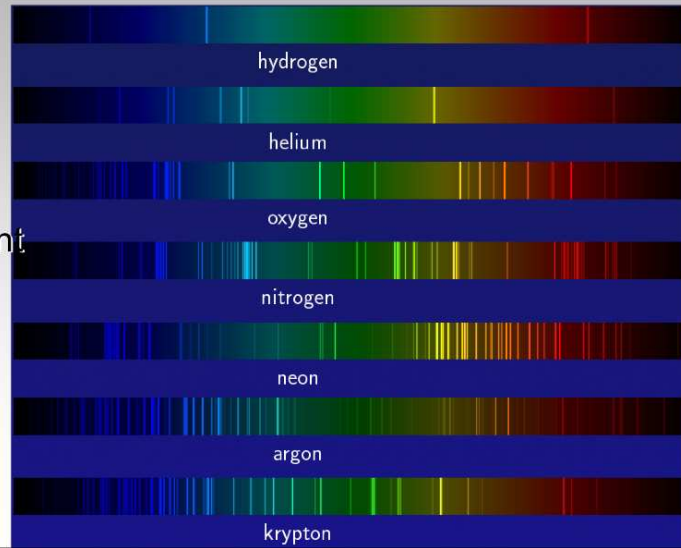
CIBA-GEIGY Corporation  
P.O. Box 4000  
Tarrytown, New York 10590  
(914) 631-1000



## Line Spectrum

### Examples:

- Ionized gases
- Lasers
- Some fluorescent lamps



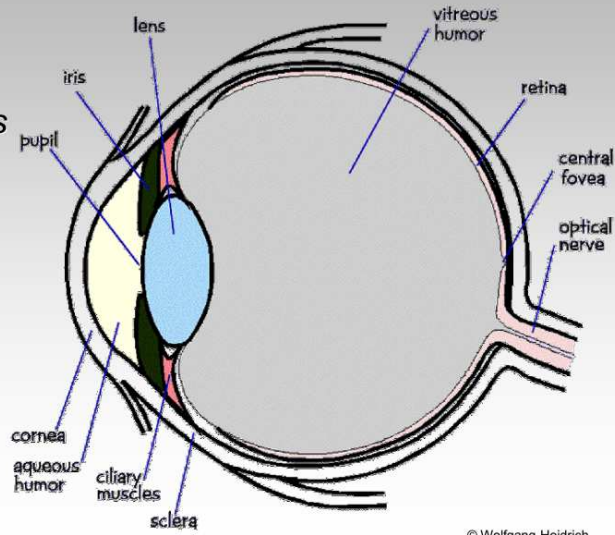
## White Light and Color

- When white light is incident upon an object, some frequencies are reflected and some are absorbed by the object
  - *But generally, the wavelength of reflected photons remains the same*
  - *Exceptions: fluorescence, phosphorescence...*
- Combination of frequencies present in the reflected light that determines what we perceive as the color of the object

# Physiology of Vision

## The retina

- Rods
  - B/w, edges
- Cones
  - Color!

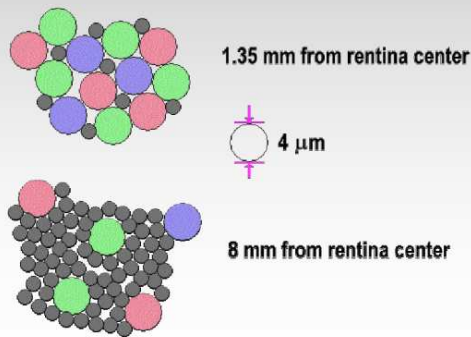


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# Physiology of Vision

## Center of retina is densely packed region called the fovea.

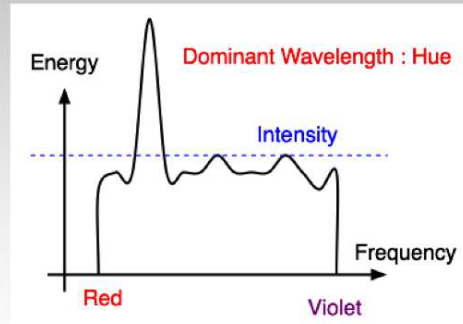
- Cones much denser here than the *periphery*



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# Hue

**Hue (or simply, "color") is dominant wavelength/frequency**

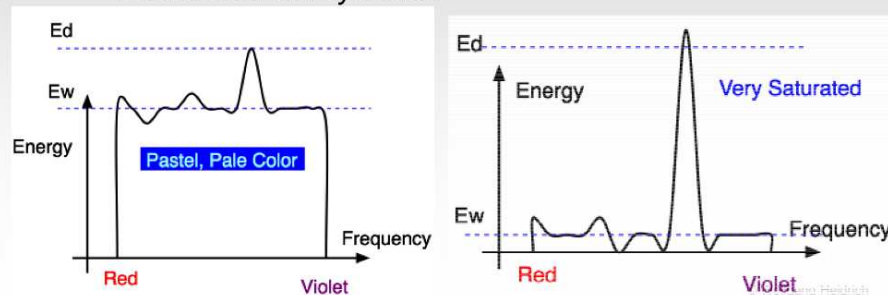


- Integration of energy for all visible wavelengths is proportional to intensity of color

# Saturation or Purity of Light

**How washed out or how pure the color of the light appears**

- Contribution of dominant light vs. other frequencies producing white light
- Saturation: how far is color from grey
  - *Pink is less saturated than red, sky blue is less saturated than royal blue*







## Intensity vs. Brightness

### **Intensity : physical term**

- **Measured** radiant energy emitted per unit of time, per unit solid angle, and per unit projected area of the source (related to the luminance of the source)

### **Lightness/brightness: perceived intensity of light**

- Nonlinear

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## Perceptual vs. Colorimetric Terms

### **Perceptual**

- Hue
- Saturation
- Lightness
  - *Reflecting objects*
- Brightness
  - *Light sources*

### **Colorimetric**

- Dominant wavelength
- Excitation purity
- Luminance
- Luminance

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## Color/Lightness Constancy

### **Color perception also depends on surrounding**

- Colors in close proximity
- Illumination under which the scene is viewed

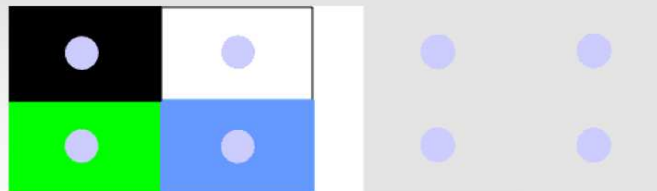
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## Adaptation, Surrounding Color

### **Color perception is also affected by**

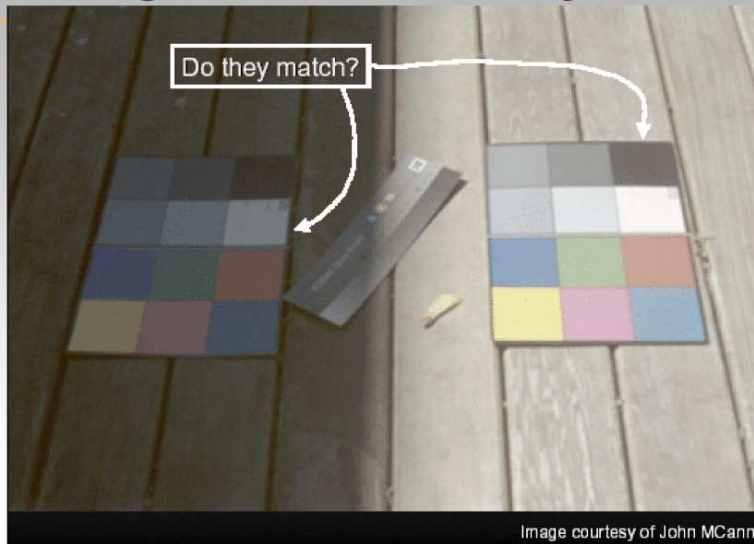
- Adaptation (move from sunlight to dark room)
- Surrounding color/intensity:
  - *Simultaneous contrast effect*



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## Color/Lightness Constancy



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## Color/Lightness Constancy



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## Color/Lightness Constancy



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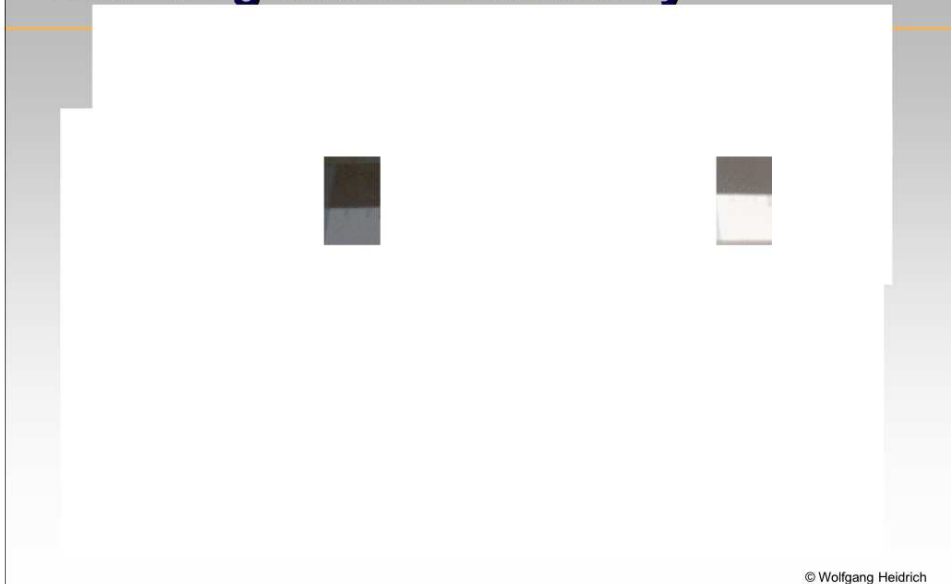
## Color/Lightness Constancy



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## Color/Lightness Constancy



## Color/Lightness Constancy



## Color Constancy

- Automatic “white balance” from change in illumination
- Vast amount of processing behind the scenes!
- Colorimetry vs. perception



## Tristimulus Theory of Color Vision

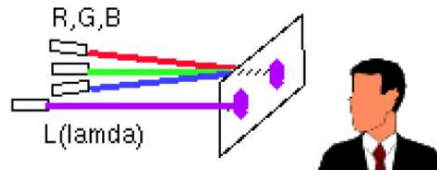


- Although light sources can have extremely complex spectra, it was empirically determined that colors could be described by only 3 **primaries**
- Colors that look the same but have different spectra are called **metamers**
- Metamer demo:

[http://www.cs.brown.edu/exploratories/freeSoftware/catalogs/color\\_theory.html](http://www.cs.brown.edu/exploratories/freeSoftware/catalogs/color_theory.html)

## Color Matching Experiments

**Performed  
in the 1930s**



**Idea: perceptually based measurement**

- shine given wavelength ( $\lambda$ ) on a screen
- User must control three pure lights producing three other wavelengths (say  $R=700$  nm,  $G=546$  nm, and  $B=438$  nm)
- Adjust intensity of RGB until colors are identical

## Color Matching Experiment

**Results**

- It was found that any color  $S(\lambda)$  could be matched with three suitable primaries  $A(\lambda)$ ,  $B(\lambda)$ , and  $C(\lambda)$ 
  - Used monochromatic light at 438, 546, and 700 nanometers

- Also found the space is linear, i.e. if

$$R(\lambda) \equiv S(\lambda)$$

then

$$R(\lambda) + M(\lambda) \equiv S(\lambda) + M(\lambda)$$

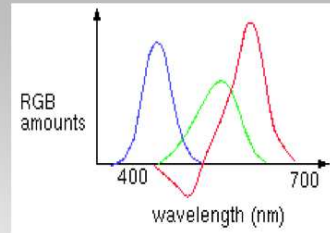
and

$$k \cdot R(\lambda) \equiv k \cdot S(\lambda)$$

## Negative Lobes

### Actually:

- Exact target match possible sometimes requires “negative light”



- Some red has to be added to target color to permit exact match using “knobs” on RGB intensity output
- Equivalent mathematically to removing red from RGB output

## Notation

### Don't confuse:

- Primaries: the spectra of the three different light sources: **R, G, B**
  - For the matching experiments, these were **monochromatic** (i.e. single wavelength) light!
  - Primaries for displays usually have a wider spectrum
- Coefficients  $R, G, B$ 
  - Specify how much of **R, G, B** is in a given color
- Color matching functions:  $r(\lambda), g(\lambda), b(\lambda)$ 
  - Specify how much of **R, G, B** is needed to produce a color that is a metamer for pure monochromatic light of wavelength  $\lambda$





## Negative Lobes

### So:

- Can't generate **all** other wavelengths with **any** set of three **positive** monochromatic lights!

### Solution:

- Convert to new synthetic "primaries" to make the color matching easy

$$\begin{pmatrix} \mathbf{X} \\ \mathbf{Y} \\ \mathbf{Z} \end{pmatrix} = \begin{pmatrix} 2.36460 & -0.51515 & 0.00520 \\ -0.89653 & 1.42640 & -0.01441 \\ -0.46807 & 0.08875 & 1.00921 \end{pmatrix} \begin{pmatrix} \mathbf{R} \\ \mathbf{G} \\ \mathbf{B} \end{pmatrix}$$

### Note:

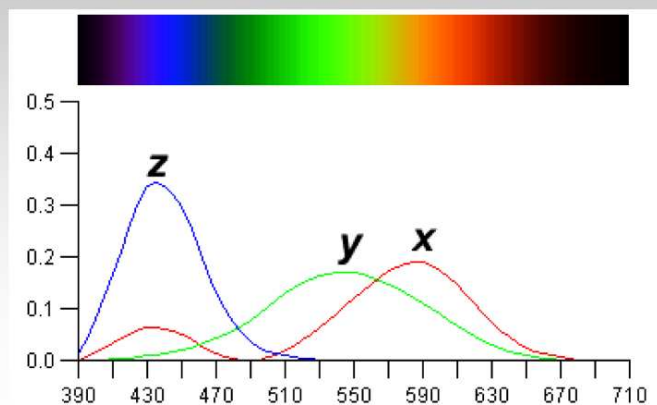
- **R, G, B** are the same monochromatic primaries as before
- The corresponding matching functions  $x(\lambda)$ ,  $y(\lambda)$ ,  $z(\lambda)$  are now positive everywhere
- But the primaries contain "negative" light contributions, and are therefore not physically realizable

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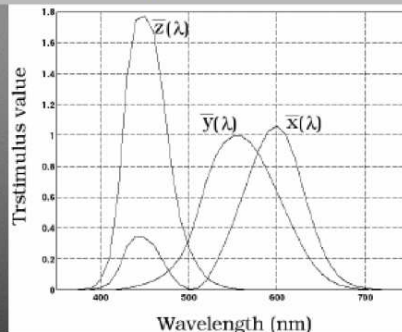
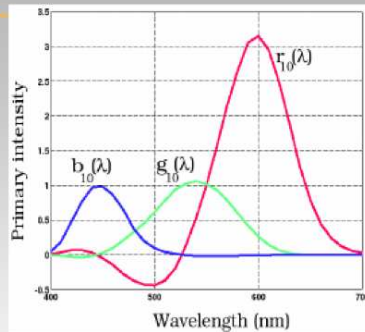
## Matching Functions - CIE Color Space

- CIE defined three "imaginary" lights X, Y, and Z, any wavelength  $\lambda$  can be matched perceptually by positive combinations



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# Matching Functions - Measured vs. CIE Color Spaces



## Measured basis

- Monochromatic lights
- Physical observations
- Negative lobes

## Transformed basis

- “imaginary” lights
- All positive, unit area matching functions
- Y is luminance, no hue
- X,Z no luminance

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# Notation



## Don't confuse:

- Synthetic primaries **X, Y, Z**
  - Contain negative frequencies
  - Do not correspond to visible colors
- Color matching functions  $x(\lambda), y(\lambda), z(\lambda)$ 
  - Are non-negative everywhere
- Coefficients X, Y, Z
- Normalized **chromaticity values**

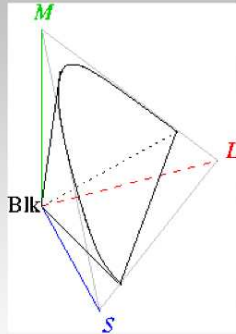
$$x = \frac{X}{X+Y+Z}, y = \frac{Y}{X+Y+Z}, z = \frac{Z}{X+Y+Z}$$

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# CIE Gamut and $\lambda$ Chromaticity Diagram

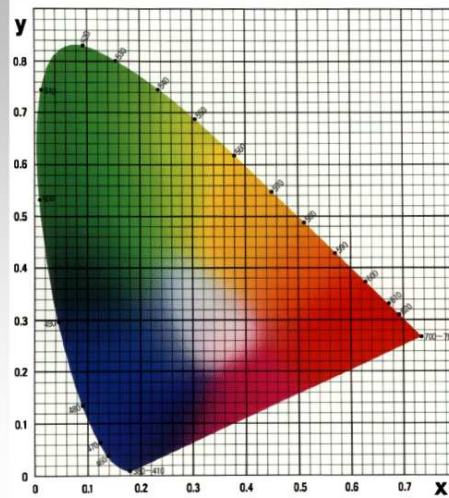


## 3D gamut



## Chromaticity diagram

- Hue only, no intensity



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# Facts about the CIE “Horseshoe” Diagram

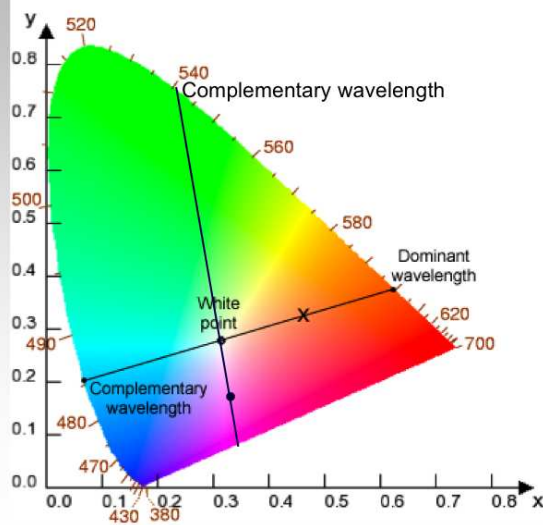


- All visible colors lie inside the horseshoe
  - Result from color matching experiments
- Spectral (monochromatic) colors lie around the border
  - The straight line between blue and red contains the purple tones
- Colors combine linearly (i.e. along lines), since the xy-plane is a plane from a linear space

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# Color Interpolation, Dominant & Opponent Wavelength



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# RGB Color Space (Color Cube)



**Define colors with (r, g, b) amounts of red, green, and blue**

- Used by OpenGL
- Hardware-centric
- Describes the colors that can be generated with specific RGB light sources

**RGB color cube sits within CIE color space**

- Subset of perceivable colors
- Scaled, rotated, sheared cube

