



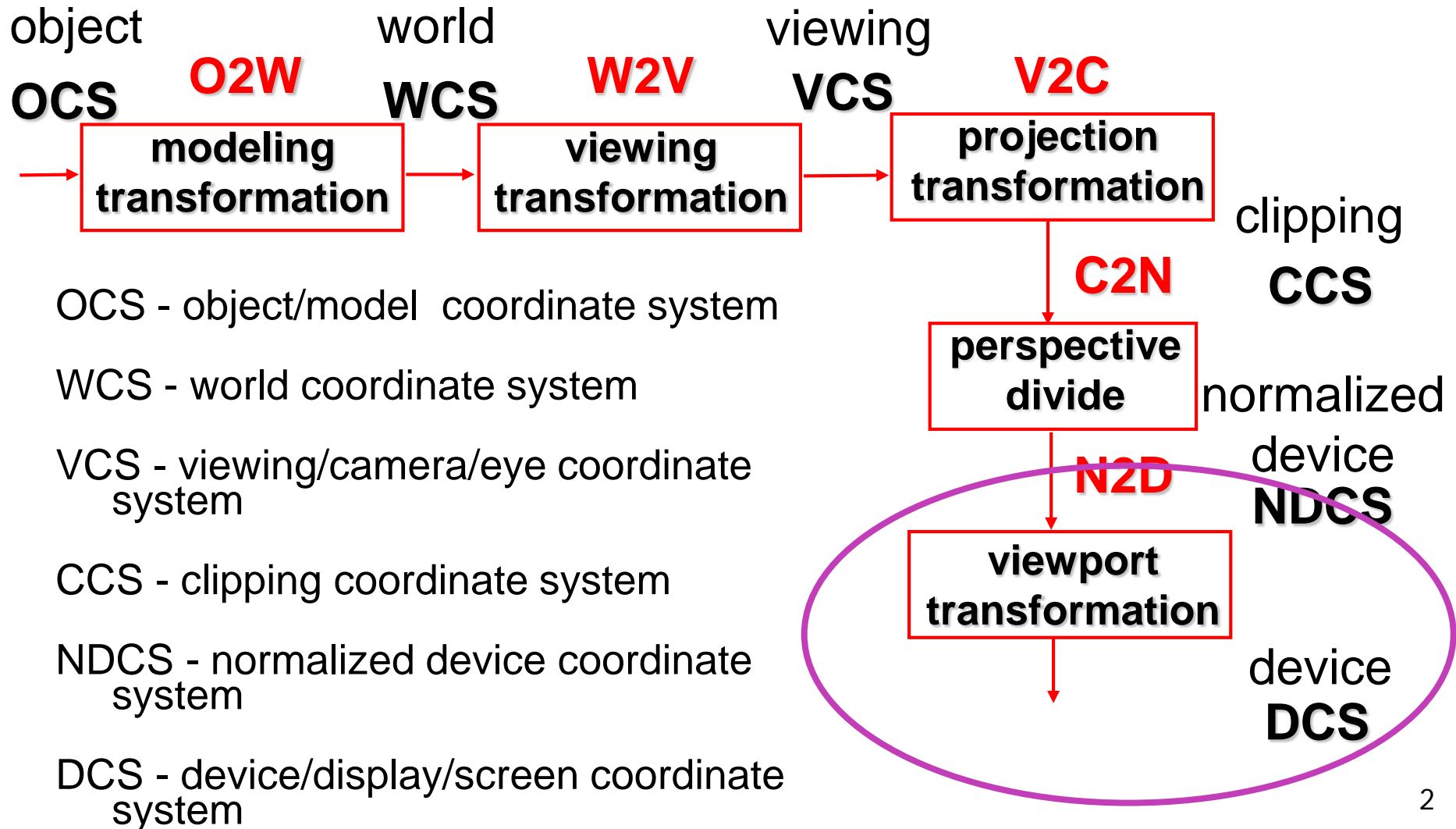
University of British Columbia
CPSC 314 Computer Graphics
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Viewing 4

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2016>

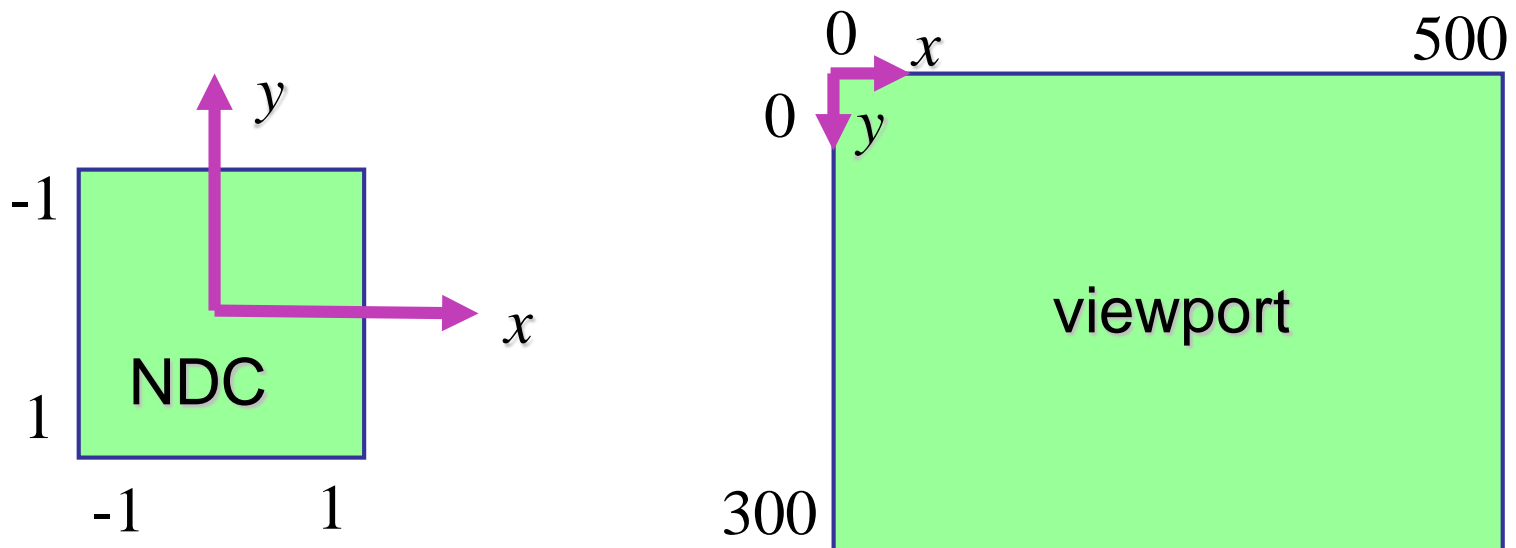
Projective Rendering Pipeline



NDC to Device Transformation

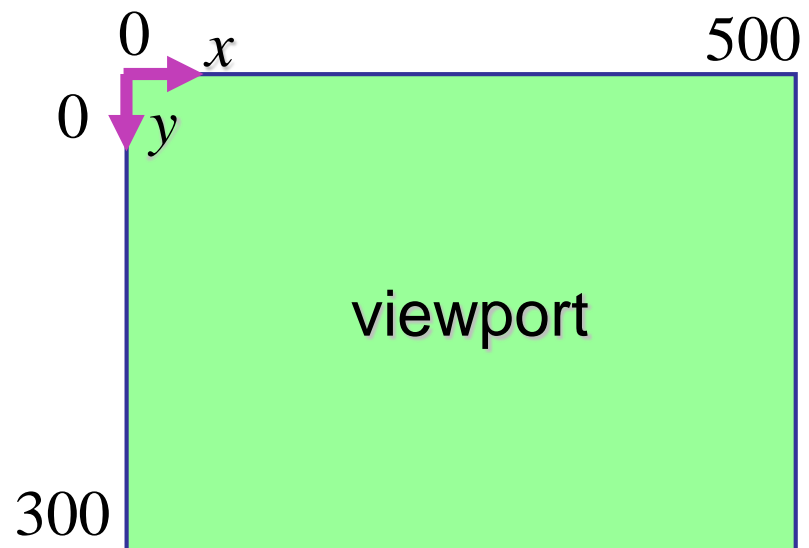
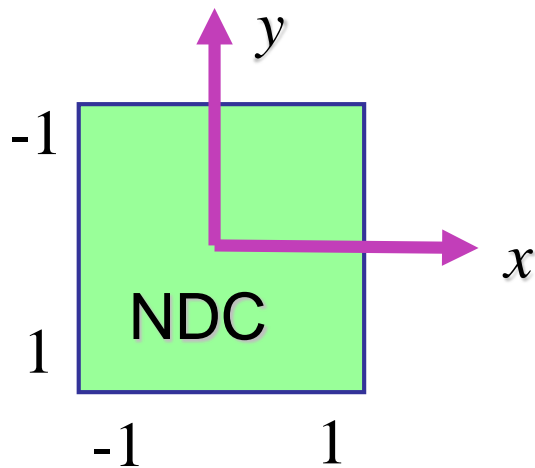
- map from NDC to pixel coordinates on display
 - NDC range is $x = -1 \dots 1$, $y = -1 \dots 1$, $z = -1 \dots 1$
 - typical display range: $x = 0 \dots 500$, $y = 0 \dots 300$
 - maximum is size of actual screen
 - z range max and default is (0, 1), use later for visibility

```
gl.viewport(0,0,w,h);  
gl.depthRange(0,1); // depth = 1 by default
```



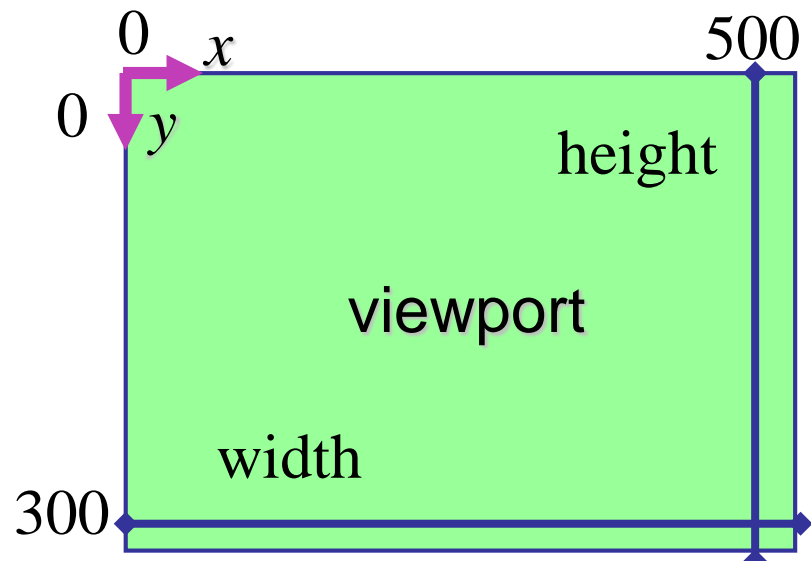
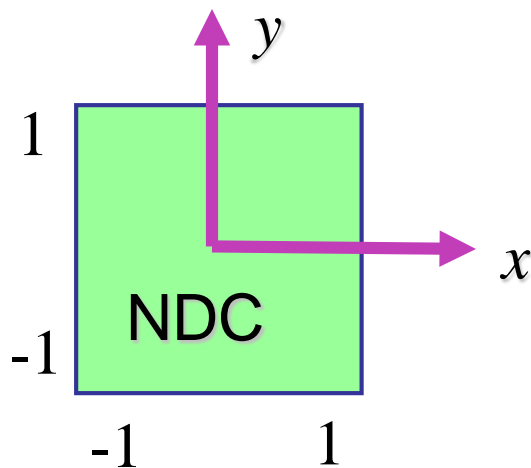
Origin Location

- yet more (possibly confusing) conventions
 - GL origin: lower left
 - most window systems origin: upper left
- then must reflect in y
- when interpreting mouse position, have to flip your y coordinates



N2D Transformation

- general formulation
 - reflect in y for upper vs. lower left origin
 - scale by width, height, depth
 - translate by $\text{width}/2$, $\text{height}/2$, $\text{depth}/2$
 - FCG includes additional translation for pixel centers at $(.5, .5)$ instead of $(0,0)$

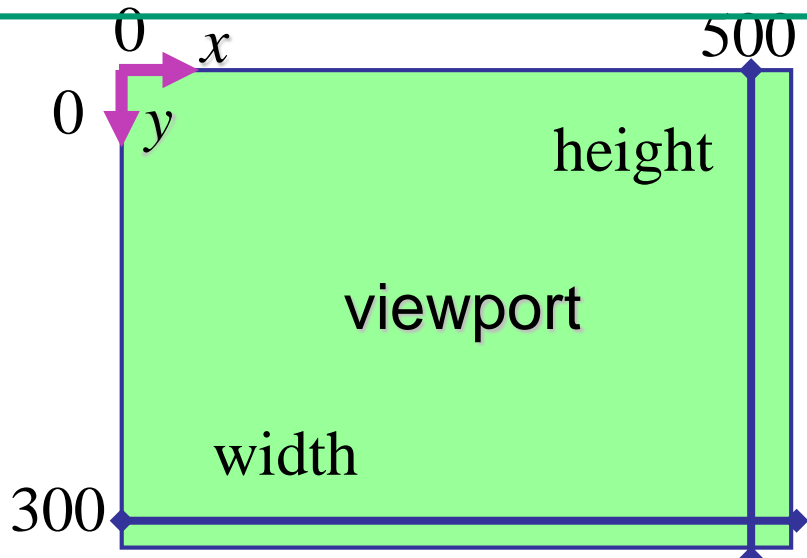
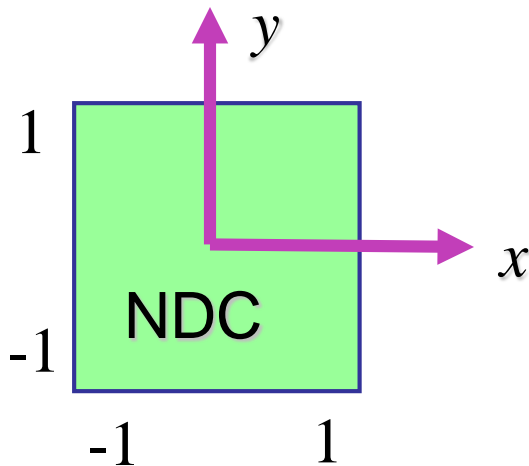


N2D Transformation

$$\begin{bmatrix} x_D \\ y_D \\ z_D \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & \frac{width}{2} - \frac{1}{2} \\ 0 & 1 & 0 & \frac{height}{2} - \frac{1}{2} \\ 0 & 0 & 1 & \frac{depth}{2} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} width \\ height \\ depth \\ 1 \end{bmatrix} = \begin{bmatrix} width & 0 & 0 & 0 \\ 0 & height & 0 & 0 \\ 0 & 0 & depth & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_N \\ y_N \\ z_N \\ 1 \end{bmatrix} = \begin{bmatrix} \frac{width(x_N + 1) - 1}{2} \\ \frac{height(-y_N + 1) - 1}{2} \\ \frac{depth(z_N + 1)}{2} \\ 1 \end{bmatrix}$$

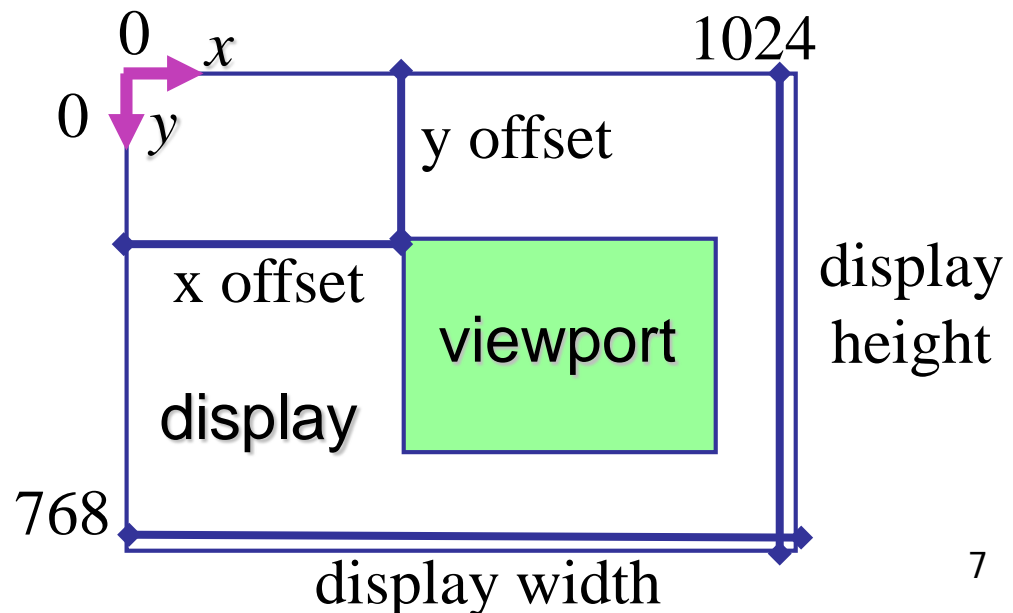
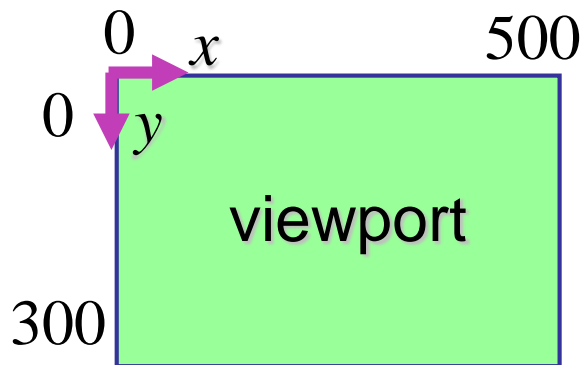
reminder:
NDC z range is -1 to 1

Display z range is 0 to 1.
gl.depthRange(n,f) can
constrain further, but *depth = 1*
is both max and default

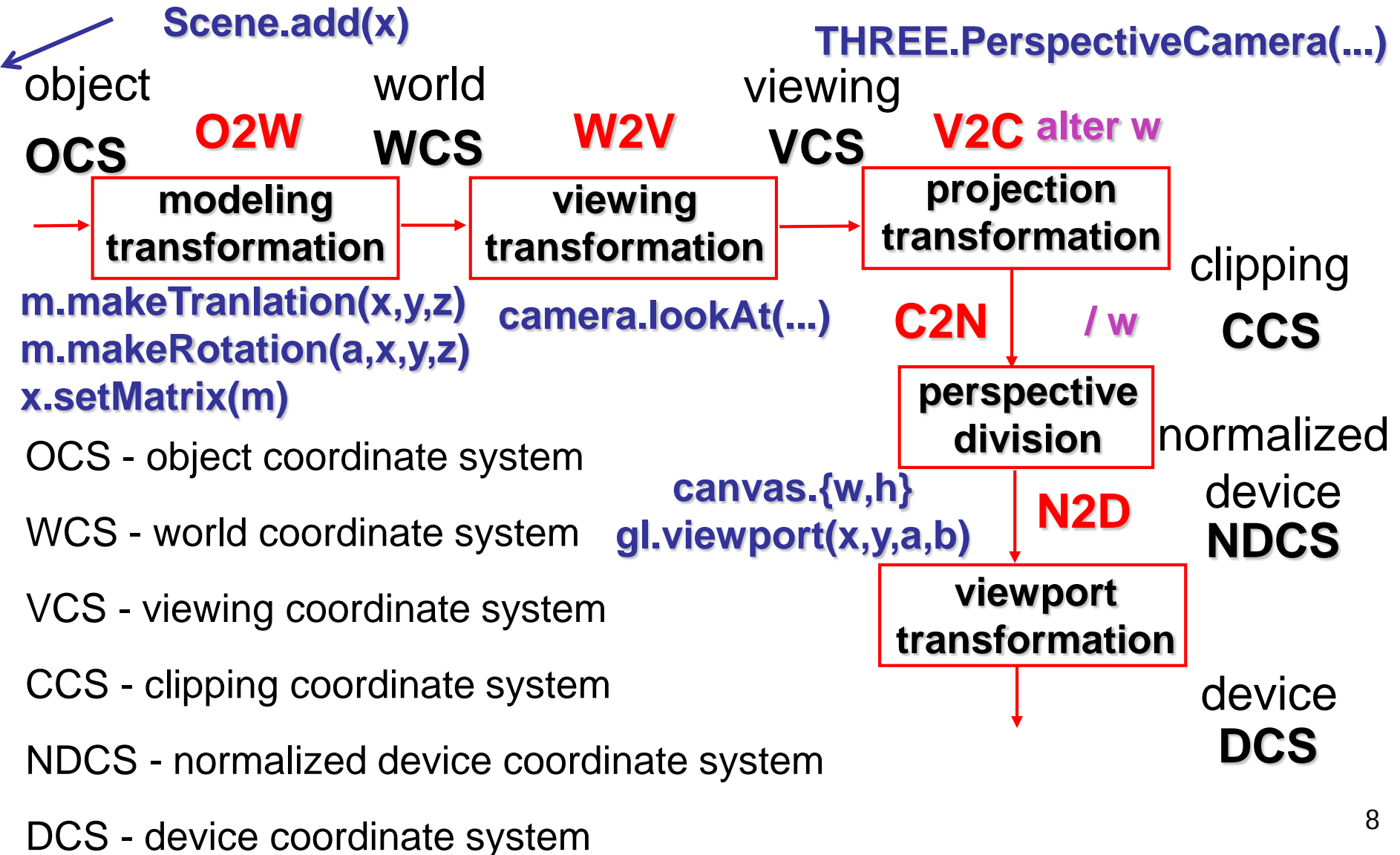


Device vs. Screen Coordinates

- viewport/window location wrt actual display not available within GL
 - usually don't care
 - use relative information when handling mouse events, not absolute coordinates
 - could get actual display height/width, window offsets from OS
- loose use of terms: device, display, window, screen...

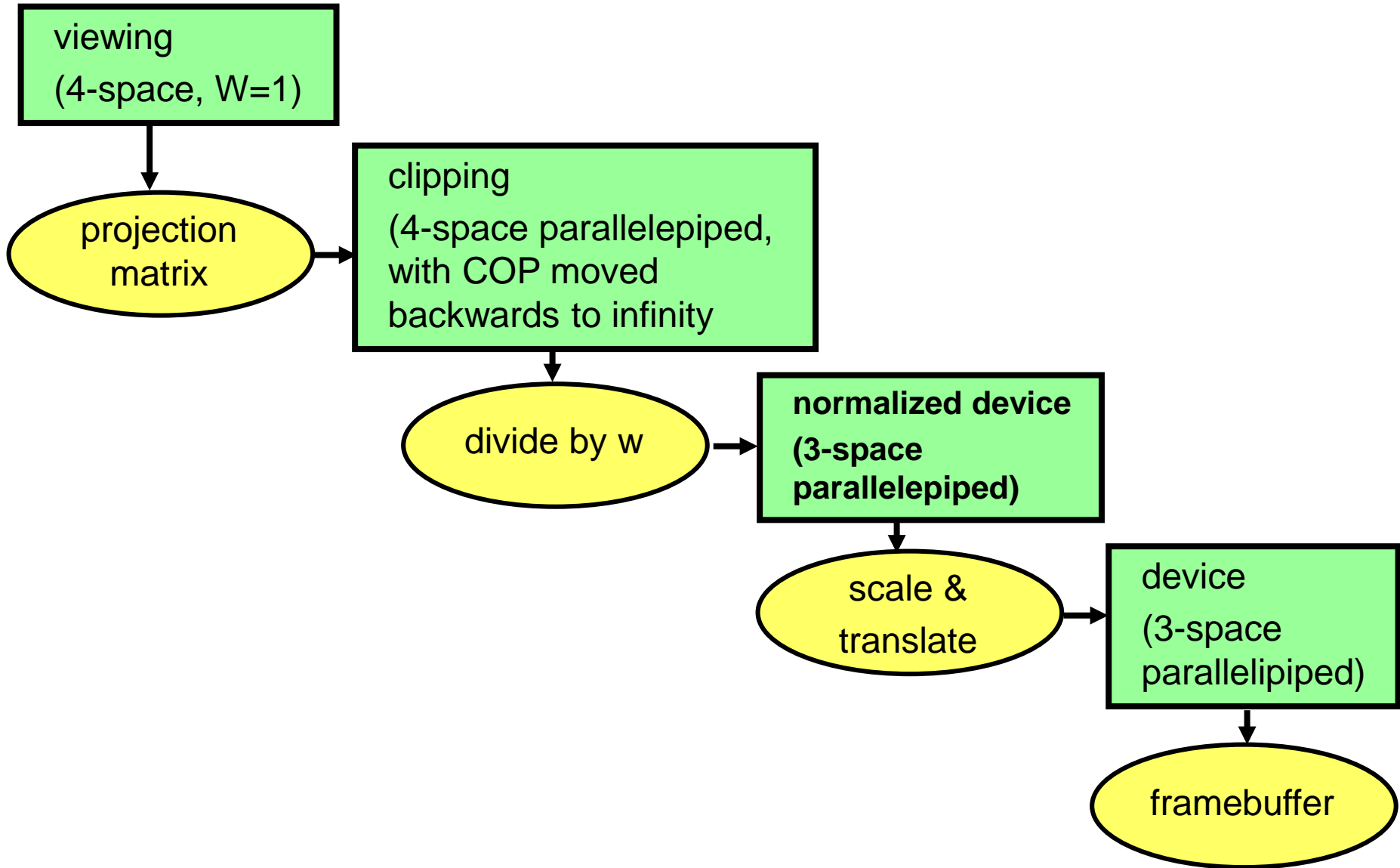


Projective Rendering Pipeline



Questions?

Coordinate Systems



Perspective Example

tracks in VCS:

left $x=-1, y=-1$

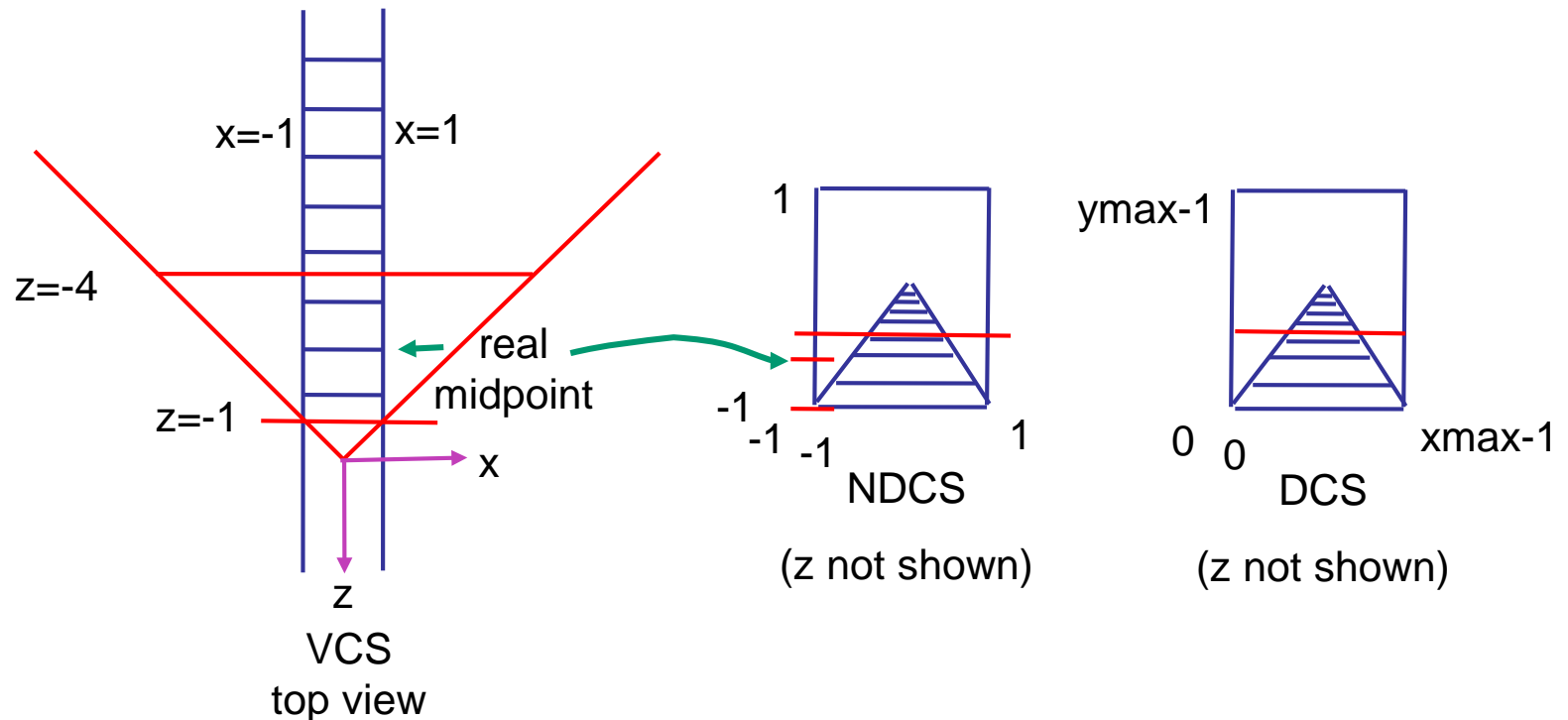
right $x=1, y=-1$

view volume

left = -1, right = 1

bot = -1, top = 1

near = 1, far = 4



Perspective Example

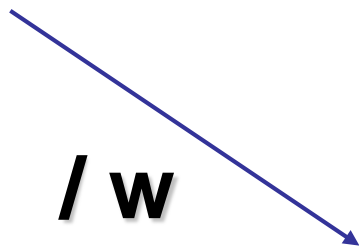
view volume

- left = -1, right = 1
- bot = -1, top = 1
- near = 1, far = 4

$$\begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & \frac{-(f+n)}{f-n} & \frac{-2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -5/3 & -8/3 \\ 0 & 0 & -1 & 0 \end{bmatrix}$$

Perspective Example

$$\left[\begin{array}{c|c} 1 & 1 \\ -1 & 1 \\ -5z_{VCS}/3 - 8/3 & -5/3 \quad -8/3 \\ -z_{VCS} & -1 \end{array} \right] = \left[\begin{array}{c|c} 1 & 1 \\ 1 & -1 \\ -5/3 & -8/3 \\ -1 & 1 \end{array} \right] z_{VCS}$$

/ w 

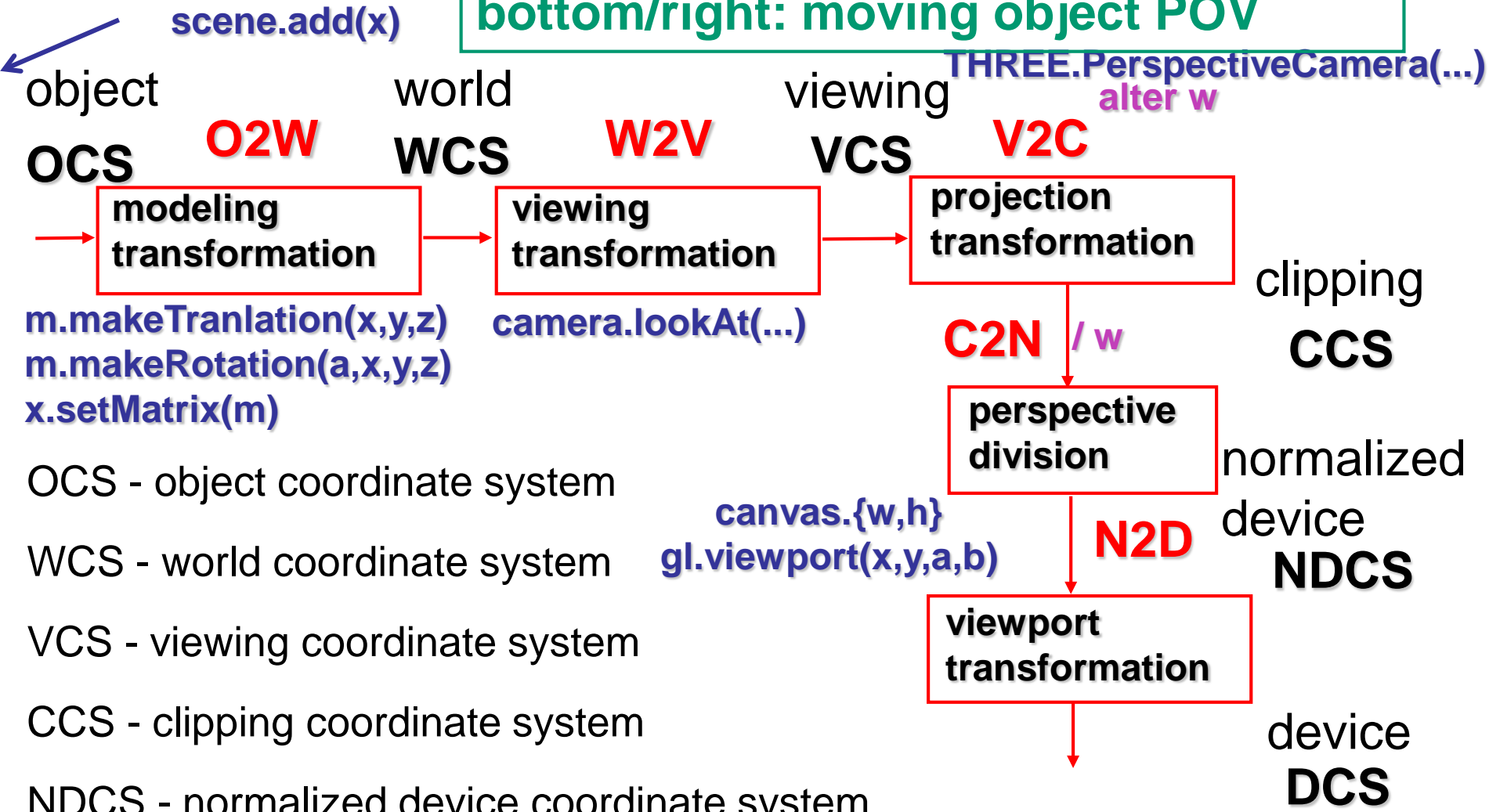
$$x_{NDCS} = -1/z_{VCS}$$

$$y_{NDCS} = 1/z_{VCS}$$

$$z_{NDCS} = \frac{5}{3} + \frac{8}{3z_{VCS}}$$

Projective Rendering Pipeline

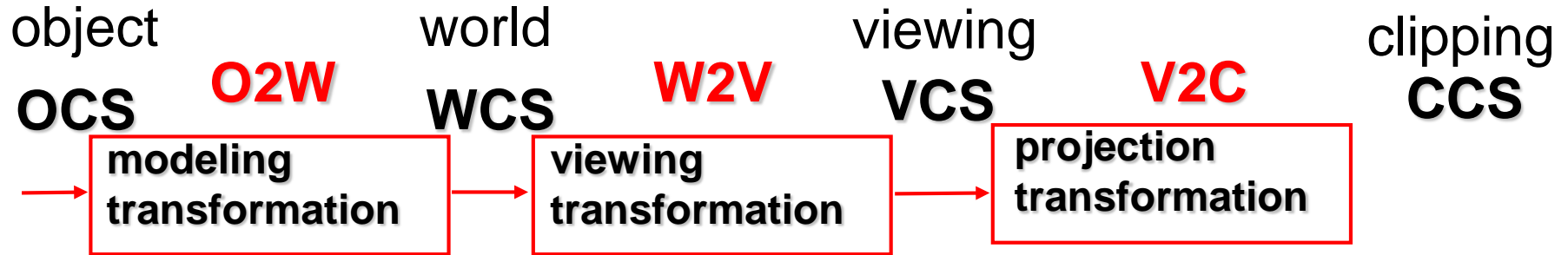
following pipeline from top/left to bottom/right: moving object POV



- OCS - object coordinate system
- WCS - world coordinate system
- VCS - viewing coordinate system
- CCS - clipping coordinate system
- NDCS - normalized device coordinate system
- DCS - device coordinate system

OpenGL Example

go back from end of pipeline to beginning: coord frame POV!



CCS

```
gl.viewport(0,0,w,h);
```

VCS

```
THREE.PerspectiveCamera(view angle, aspect, near, far)
```

WCS

```
u_xformMatrix = Identity()  
gl.uniformMatrix4fv(u_xformMatrix, false, xformMatrix);
```

OCS1

```
torsoGeometry.applyMatrix(u_xformMatrix );  
var torso = new THREE.Mesh(torsoGeometry,normalMaterial);  
scene.add(torso);
```

Coord Sys: Frame vs Point

read down: transforming between coordinate frames, from frame A to frame B

read up: transforming points, up from frame B coords to frame A coords

OpenGL command order

D2N

DCS display

`gl.viewport(x,y,a,b)`

N2D

N2V

NDCS normalized device

`THREE.PerspectiveCamera(...)`

V2N

V2W

VCS viewing

`camera.lookAt(...)`

W2V

W2O

WCS world

`m.makeRotationX(...)`

O2W

OCS object

`scene.add(object)`

pipeline interpretation¹⁶

Questions?