# University of British Columbia CPSC 314 Computer Graphics Jan-Apr 2016 

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## Transformations 5

http://www.ugrad.cs.ubc.ca/~cs314/Vjan2016

## Assignments

- project 1
- out today, due 11:59pm sharp Tue Feb 2
- projects will go out before we've covered all the material
- so you can think about it before diving in
- build star-nosed mole out of cubes and $4 \times 4$ matrices
- think cartoon, not beauty
- http://www.ugrad.cs.ubc.ca/~cs314/Vjan2016/p1.pdf
- template code gives you program shell http://www.ugrad.cs.ubc.ca/~cs314/Vjan2016/p1.zip
- theory homework 1
- out today, due 2pm sharp Wed Jan 27 (start of class)
- theoretical side of material
- http://www.ugrad.cs.ubc.ca/~cs314/Vjan2016/h1.pdf


## Real Star-Nosed Moles


http://aninfopage.blogspot.ca/2011/12/star-nose-mole.html

http://animals.howstuffworks.com/mammals/ mole-info.htm

http://www.rsba.ca/recherche_espece/ fiche_espece.php?recordID=334

http://www.biokids.umich.edu/critters/ Condylura_cristata/

## Star-Nosed Moles!

. out of boxes and matrices


## Cartoon motion: armadillo jumpcut



## Cartoon motion: armadillo jumpcut



## Project 1 Advice

- do not model everything first and only then worry about animating
- interleave modelling, animation
- for each body part: add it, then jumpcut animate, then smooth animate
- discover if on wrong track sooner
- dependencies: can't get anim credit if no model
- use body as scene graph root
- check from multiple camera angles


## Project 1 Advice

- finish all required parts before
- going for extra credit
- playing with lighting or viewing
- construct your $4 \times 4$ matrix by hand
- without rotate(), translate(), scale() commands in Three.js
- do not interpolate numbers within matrix
- even though it's safe to linearly interpolate parameters you use to create matrix


## Project 1 Advice

- smooth transition
- change happens gradually over X frames
- key click triggers animation
- one way: redraw happens X times
- linear interpolation:
each time, param += (new-old)/30
- or redraw happens over $X$ seconds
- even better, but not required


## Style

- you can lose up to $15 \%$ for poor style
- most critical: reasonable structure
- yes: parametrized functions
- no: cut-and-paste with slight changes
- reasonable names (variables, functions)
- adequate commenting
- rule of thumb: what if you had to fix a bug two years from now?
- global variables are indeed acceptable


## Version Control

- bad idea: just keep changing same file
- save off versions often
- after got one thing to work, before you try starting next
- just before you do something drastic
- use version control software
- strongly recommended: easy to browse previous work, revert
- use meaningful comments to describe what you did
- "started on tail", "fixed head breakoff bug", "leg code compiles but doesn't run"
- useful when you're working alone, critical when working together


## General Rotation

## Rotation About a Point: Moving Object



## Rotation: Changing Coordinate Systems

- same example: rotation around arbitrary center



$$
\boldsymbol{\Gamma}\left(x_{,} y, z\right) \boldsymbol{P}(z, \theta) \boldsymbol{\Gamma}\left(-\mathcal{X}_{,}-\mathscr{Y},-z\right)
$$

## Rotation: Changing Coordinate Systems

- rotation around arbitrary center
- step 1: translate coordinate system to rotation center

$$
\mathbf{T}(x, y, z) \mathbf{R}(z, \theta) \mathbf{T}(-x,-y,-z)
$$

## Rotation: Changing Coordinate Systems

- rotation around arbitrary center
- step 2: perform rotation


$$
\mathbf{T}(x, y, z) \mathbf{R}(z, \theta) \mathbf{T}(-x,-y,-z)
$$

## Rotation: Changing Coordinate Systems

- rotation around arbitrary center
- step 3: back to original coordinate system


$$
\mathbf{T}(x, y, z) \mathbf{R}(z, \theta) \mathbf{T}(-x,-y,-z)
$$

## General Transform Composition

- transformation of geometry into coordinate system where operation becomes simpler
- typically translate to origin
- perform operation
- transform geometry back to original coordinate system


## Rotation About an Arbitrary Axis

- axis defined by two points
- translate point to the origin
- rotate to align axis with z-axis (or $x$ or $y$ )
- perform rotation
- undo aligning rotations
- undo translation


## Arbitrary Rotation



- arbitrary rotation: change of basis
- given two orthonormal coordinate systems XYZ and $A B C$
- $A$ 's location in the XYZ coordinate system is ( $\mathrm{a}_{\mathrm{x}}, \mathrm{a}_{\mathrm{y}}, \mathrm{a}_{\mathrm{z}}, 1$ ), ...


## Arbitrary Rotation




- arbitrary rotation: change of basis
- given two orthonormal coordinate systems XYZ and $A B C$
- $A$ 's location in the $X Y Z$ coordinate system is $\left(a_{x}, a_{y}, a_{z}, 1\right), \ldots$


## Arbitrary Rotation



$$
\left(b_{x}, b_{y}, b_{z}, 1\right)
$$



- arbitrary rotation: change of basis
- given two orthonormal coordinate systems XYZ and $A B C$
- $A$ 's location in the XYZ coordinate system is $\left(\mathrm{a}_{\mathrm{x}}, \mathrm{a}_{\mathrm{y}}, \mathrm{a}_{\mathrm{z}}, 1\right), \ldots$
- transformation from one to the other is matrix R whose columns are $A, B, C$ :

$$
R(X)=\left[\begin{array}{llll}
a_{x} & b_{x} & c_{x} & 0 \\
a_{y} & b_{y} & c_{y} & 0 \\
a_{z} & b_{z} & c_{z} & 0 \\
0 & 0 & 0 & 1
\end{array}\right] \|\left[\begin{array}{l}
1 \\
0 \\
0 \\
1
\end{array}\right]=\left(a_{x}, a_{y}, a_{z}, 1\right)=A
$$

## Transformation Hierarchies

## Transformation Hierarchies

- scene may have a hierarchy of coordinate systems
- stores matrix at each level with incremental transform from parent's coordinate system

- scene graph



## Transformation Hierarchy Example 1



## Transformation Hierarchy Example 2

- draw same 3D data with different transformations: instancing



## Matrix Stacks

- challenge of avoiding unnecessary computation
- using inverse to return to origin
- computing incremental $T_{1}->T_{2}$


Object coordinates


