

Wolfgang Heidrich

Wolfgang Heidrich



Course News

Assignment 3 (project)

Due April 1

Reading

- · Chapter 10 (ray tracing), except 10.8-10.10
- Chapter 14 (global illumination)

Friday Lecture

- Out of town for program committee meeting
- Anika will continue discussion of ray-tracing



Overview

So far

- Real-time/HW rendering w/ Rendering Pipeline
- Rendering algorithms using the Rendering Pipeline

Now

- Ray-Tracing
 - Simple algorithm for software rendering
 - Usually offline (e.g. movies etc.)
 - But: research on making this method real-time
 - Extremely flexible (new effects can easily be incorporated)

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Ray-Tracing

Basic Algorithm (Whithead):

```
for every pixel p<sub>i</sub> {

Generate ray r from camera position through pixel p<sub>i</sub>

p<sub>i</sub>= background color

for every object o in scene {

if( r intersects o && intersection is closer than previously found intersections )

Compute lighting at intersection point, using local normal and material properties; store result in p<sub>i</sub>

}
```



Issues:

- Generation of rays
- Intersection of rays with geometric primitives
- Geometric transformations
- Lighting and shading
- Efficient data structures so we don't have to test intersection with every object

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Ray-Tracing – Generation of Rays

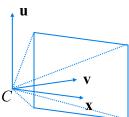


Camera Coordinate System

- Origin: C (camera position)
- Viewing direction: v
- Up vector: u
- x direction: x= v×u

Note:

- Corresponds to viewing transformation in rendering pipeline!
- · See gluLookAt...

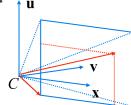


Ray-Tracing – Generation of Rays



Other parameters:

- Distance of Camera from image plane: d
- Image resolution (in pixels): w, h
- Left, right, top, bottom boundaries in image plane: l, r, t, b



Then:

- Lower left corner of image: $O = C + d \cdot \mathbf{v} + l \cdot \mathbf{x} + b \cdot \mathbf{u}$
- Pixel at position i, j (i=0..w-1, j=0..h-1):

$$\begin{split} P_{i,j} &= O + i \cdot \frac{r - l}{w - 1} \cdot \mathbf{x} - j \cdot \frac{t - b}{h - 1} \cdot \mathbf{u} \\ &= O + i \cdot \Delta x \cdot \mathbf{x} - j \cdot \Delta y \cdot \mathbf{y} \end{split}$$

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Ray-Tracing – Generation of Rays



Ray in 3D Space:

$$\mathbf{R}_{i,j}(t) = C + t \cdot (P_{i,j} - C) = C + t \cdot \mathbf{v}_{i,j}$$

where $t = 0... \infty$



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Ray Intersections

Task:

- Given an object o, find ray parameter t, such that $\mathbf{R}_{i,j}(t)$ is a point on the object
 - Such a value for t may not exist
- Intersection test depends on geometric primitive



Ray Intersections

Spheres at origin:

Implicit function:

$$S(x, y, z): x^2 + y^2 + z^2 = r^2$$

Ray equation:

$$\mathbf{R}_{i,j}(t) = C + t \cdot \mathbf{v}_{i,j} = \begin{pmatrix} c_x \\ c_y \\ c_z \end{pmatrix} + t \cdot \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} = \begin{pmatrix} c_x + t \cdot v_x \\ c_y + t \cdot v_y \\ c_z + t \cdot v_z \end{pmatrix}$$

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Ray Intersections

To determine intersection:

• Insert ray $\mathbf{R}_{i,j}(t)$ into S(x,y,z):

$$(c_x + t \cdot v_x)^2 + (c_v + t \cdot v_v)^2 + (c_z + t \cdot v_z)^2 = r^2$$

- Solve for t (find roots)
 - Simple quadratic equation



Ray Intersections

Other Primitives:

- Implicit functions:
 - Spheres at arbitrary positions
 - Same thing
 - Conic sections (hyperboloids, ellipsoids, paraboloids, cones, cylinders)
 - Same thing (all are quadratic functions!)
 - Higher order functions (e.g. tori and other quartic functions)
 - In principle the same
 - But root-finding difficult
 - Net to resolve to numerical methods

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Ray Intersections

Other Primitives (cont)

- Polygons:
 - First intersect ray with plane
 - linear implicit function
 - Then test whether point is inside or outside of polygon (2D test)
 - For convex polygons
 - Suffices to test whether point in on the right side of every boundary edge
 - Similar to computation of outcodes in line clipping



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Ray-Tracing – Geometric Transformations



Geometric Transformations:

- Similar goal as in rendering pipeline:
 - Modeling scenes convenient using different coordinate systems for individual objects
- Problem:
 - Not all object representations are easy to transform
 - This problem is fixed in rendering pipeline by restriction to polygons (affine invariance!)

Ray-Tracing – Geometric Transformations



Geometric Transformations:

- Similar goal as in rendering pipeline:
 - Modeling scenes convenient using different coordinate systems for individual objects
- Problem:
 - Not all object representations are easy to transform
 - This problem is fixed in rendering pipeline by restriction to polygons (affine invariance!)
 - Ray-Tracing has different solution:
 - The ray itself is always affine invariant!
 - Thus: transform ray into object coordinates!

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Ray-Tracing – Geometric Transformations



Ray Transformation:

- For intersection test, it is only important that ray is in same coordinate system as object representation
- Transform all rays into object coordinates
 - Transform camera point and ray direction by <u>inverse</u> of model/view matrix
- Shading has to be done in world coordinates (where light sources are given)
 - Transform object space intersection point to world coordinates
 - Thus have to keep both world and object-space ray



Issues:

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Ray-Tracing Lighting and Shading



Local Effects:

- Local Lighting
 - Any reflection model possible
 - Have to talk about light sources, normals...
- Texture mapping
 - Color textures
 - Bump maps
 - Environment maps
 - Shadow maps

Ray-Tracing Local Lighting



Light sources:

- For the moment: point and directional lights
- Later: are light sources
- More complex lights are possible
 - Area lights
 - Global illumination
 - Other objects in the scene reflect light
 - Everything is a light source!
 - Talk about this on Monday

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Ray-Tracing Local Lighting



Local surface information (normal...)

• For implicit surfaces F(x,y,z)=0: normal $\mathbf{n}(x,y,z)$ can be easily computed at every intersection point using the gradient

$$\mathbf{n}(x, y, z) = \begin{pmatrix} \partial F(x, y, z) / \partial x \\ \partial F(x, y, z) / \partial y \\ \partial F(x, y, z) / \partial z \end{pmatrix}$$

• Example: $F(x, y, z) = x^2 + y^2 + z^2 - r^2$

$$\mathbf{n}(x, y, z) = \begin{pmatrix} 2x \\ 2y \\ 2z \end{pmatrix}$$
 Needs to be normalized!

Ray-Tracing Local Lighting



Local surface information

- Alternatively: can interpolate per-vertex information for triangles/meshes as in rendering pipeline
 - Phong shading!
 - Same as discussed for rendering pipeline
- Difference to rendering pipeline:
 - Interpolation cannot be done incrementally
 - Have to compute Barycentric coordinates for every intersection point (e.g plane equation for triangles)

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Ray-Tracing Texture Mapping



Approach:

- Works in principle like in rendering pipeline
 - − Given s, t parameter values, perform texture lookup
 - Magnification, minification just as discussed
- Problem: how to get s, t
 - Implicit surfaces often don't have parameterization
 - For special cases (spheres, other conic sections), can use parametric representation
 - Triangles/meshes: use interpolation from vertices

Ray-Tracing Lighting and Shading



Global Effects

- Shadows
- Reflections/refractions

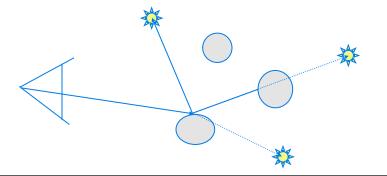
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Ray-Tracing Shadows



Approach:

- To test whether point is in shadow, send out <u>shadow</u> <u>rays</u> to all light sources
 - If ray hits another object, the point lies in shadow

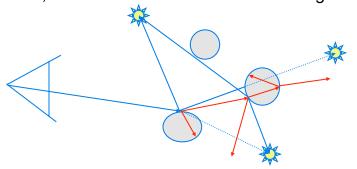


Ray-Tracing Reflections/Refractions



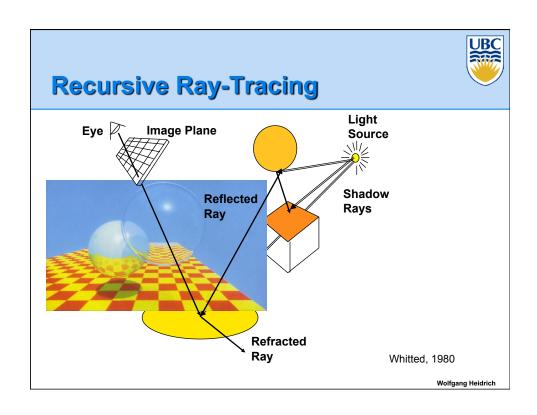
Approach:

- Send rays out in reflected and refracted direction to gather incoming light
- That light is multiplied by local surface color and Fresnel term, and added to result of local shading



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Recursive Ray Tracing Ray tracing can handle Reflection (chrome) Refraction (glass) **Shadows** Spawn secondary rays Reflection, refraction pixel positions If another object is hit, recurse to on projection find its color projection plane reference Shadow point Cast ray from intersection point to light source, check if intersects another object Wolfgang Heidrich



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Recursive Ray-Tracing Algorithm

```
RayTrace(r,scene)
obj := FirstIntersection(r,scene)
if (no obj) return BackgroundColor;
else begin
  if ( Reflect(obj) ) then
    reflect_color := RayTrace(ReflectRay(r,obj));
  else
    reflect_color := Black;
if ( Transparent(obj) ) then
    refract_color := RayTrace(RefractRay(r,obj));
  else
    refract_color := Black;
  return Shade(reflect_color,refract_color,obj);
end;
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```



Algorithm Termination Criteria

Termination criteria

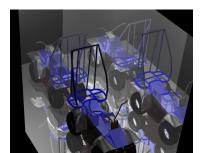
- No intersection
- Reach maximal depth
 - Number of bounces
- Contribution of secondary ray attenuated below threshold
 - Each reflection/refraction attenuates ray

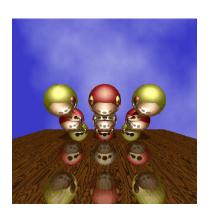
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Reflection

Mirror effects

Perfect specular reflection





 $\theta \mid \theta$

Refraction

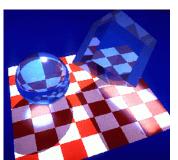


Happens at interface between transparent object and surrounding medium

E.g. glass/air boundary

Snell's Law

- $c_1 \sin \theta_1 = c_2 \sin \theta_2$
- Light ray bends based on refractive indices c₁, c₂



n

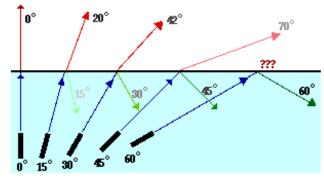
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Total Internal Reflection



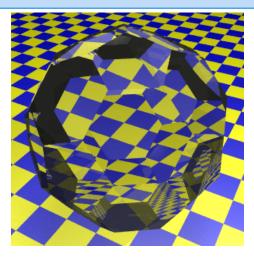
As the angle of incidence increases from 0 to greater angles ...

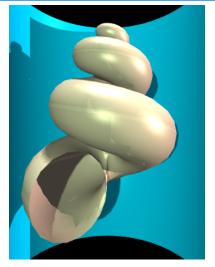


- ...the refracted ray becomes dimmer (there is less refraction)
- ...the reflected ray becomes brighter (there is more reflection)
- ...the angle of refraction approaches 90 degrees until finally a refracted ray can no longer be seen.

Ray-Tracing Example Images







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Ray-Tracing Terminology



Terminology:

- Primary ray: ray starting at camera
- Shadow ray
- Reflected/refracted ray
- Ray tree: all rays directly or indirectly spawned off by a single primary ray

Note:

 Need to limit maximum depth of ray tree to ensure termination of ray-tracing process!



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- Efficient data structures so we don't have to test intersection with every object

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Ray Tracing

Data Structures

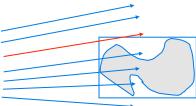
- Goal: reduce number of intersection tests per ray
- Lots of different approaches:
 - (Hierarchical) bounding volumes
 - Hierarchical space subdivision
 - Oct-tree, k-D tree, BSP tree



Bounding Volumes

Idea:

- Rather than testing every ray against a potentially very complex object (e.g. triangle mesh), do a quick <u>conservative</u> test first which eliminates most rays
 - Surround complex object by simple, easy to test geometry (typically sphere or axis-aligned box)
 - Want to make bounding volume as tight as possible!



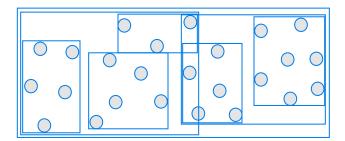
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Hierarchical Bounding Volumes



Extension of previous idea:

Use bounding volumes for groups of objects



Spatial Subdivision Data Structures



Bounding Volumes:

- Find simple object completely enclosing complicated objects
 - Boxes, spheres
- Hierarchically combine into larger bounding volumes

Spatial subdivision data structure:

- Partition the whole space into cells
 - Grids, oct-trees, (BSP trees)
- Simplifies and accelerates traversal
- Performance less dependent on order in which objects are inserted

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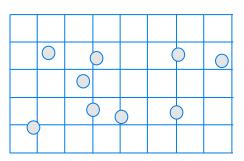
Regular Grid Subdivide space into rectangular grid: - Associate every object with the cell(s) that it overlaps with - Find intersection: traverse grid In 3D: regular grid of cubes (voxels): Wofgang Heidrich

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Creating a Regular Grid

Steps:

- · Find bounding box of scene
- Choose grid resolution in x, y, z
- Insert objects
- Objects that overlap multiple cells get referenced by all cells they overlap

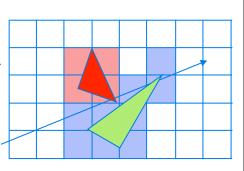


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Grid Traversal

Traversal:

- Start at ray origin
- · While no intersection found
 - Go to next grid cell along ray
 - Compute intersection of ray with all objects in the cell
 - Determine closest such intersection
 - Check if that intersection is inside the cell
 - If so, terminate search





Traversal

Note:

- This algorithm calls for computing the intersection points multiple times (once per grid cell)
- In practice: store intersections for a (ray, object) pair once computed, reuse for future cells

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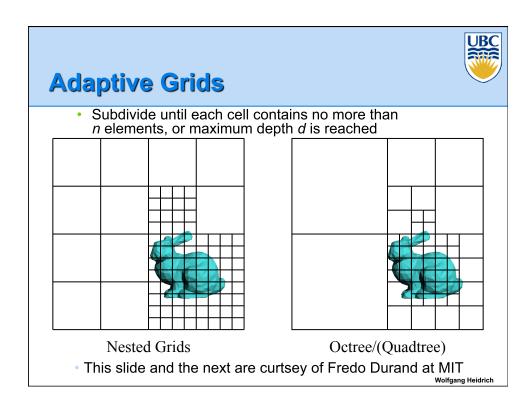
Regular Grid Discussion

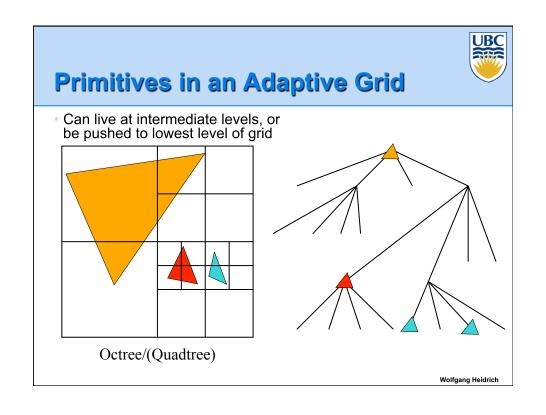
Advantages?

- Easy to construct
- Easy to traverse

Disadvantages?

- May be only sparsely filled
- · Geometry may still be clumped







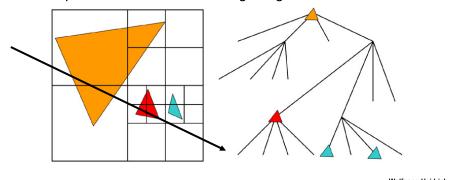
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Advantages

Grid complexity matches geometric density

Disadvantages

More expensive to traverse than regular grid



Coming Up...

Friday:

More ray-tracing (Anika)

Next Week:

Global illumination