

## Shadow Volumes

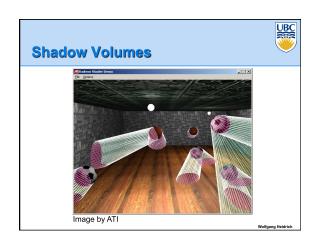
#### Use new buffer: stencil buffer

- Just another channel of the framebuffer
- · Can count how often a pixel is drawn

#### Algorithm (1):

- Generate silhouette polygons for all objects
  - Polygons starting at silhouette edges of object
  - Extending away from light source towards infinity
  - These can be computed in vertex programs

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#### **Shadow Volumes**

#### ..........

- Algorithm (2):
- Render all original geometry into the depth buffer
- I.e. do not draw any colors (or only draw ambient illumination term)
- Render front-facing silhouette polygons while incrementing the stencil buffer for every rendered fragment
- Render back-facing silhouette polygons while decrementing the stencil buffer for every rendered fragment
- Draw illuminated geometry where the stencil buffer is 0, shadow elsewhere

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# Shadow Volumes | Image by ATI

#### **Shadow Volumes**

#### **Discussion:**

- Object space method therefore no precision issues
- Lots of large polygons: can be slow
- High geometry count
- Large number of pixels rendered

UBC

#### **Ray Tracing**

**Wolfgang Heidrich** 

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### Course Topics for the Rest of the Term



#### Ray-tracing & Global Illumination

Today, next week

Parametric Curves/Surfaces

Overview of current research

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#### **Overview**



#### So far

- · Real-time/HW rendering w/ Rendering Pipeline
- · Rendering algorithms using the Rendering Pipeline

#### Now

- Ray-Tracing
  - Simple algorithm for software rendering
  - Usually offline (e.g. movies etc.)
  - But: research on making this method real-time
  - Extremely flexible (new effects can easily be incorporated)

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#### **Ray-Tracing**



#### Basic Algorithm (Whithead):

for every pixel  $\boldsymbol{p}_i$  {

Generate ray r from camera position through pixel p<sub>i</sub>

p<sub>i</sub>= background color

for every object o in scene {

if( r intersects o && intersection is closer than previously found intersections )

Compute lighting at intersection point, using local normal and material properties; store result in p<sub>i</sub>

}

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#### **Ray-Tracing**



#### Issues:

- Generation of rays
- Intersection of rays with geometric primitives
- Geometric transformations
- · Lighting and shading
- Efficient data structures so we don't have to test intersection with every object

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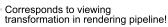
#### Ray-Tracing – Generation of Rays



#### Camera Coordinate System

- · Origin: C (camera position)
- · Viewing direction: v
- Up vector: u
- x direction: x= v×u

#### Note:



See gluLookAt…



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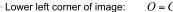
#### Ray-Tracing – Generation of Rays



#### Other parameters:

- Distance of Camera from image plane: d
- Image resolution (in pixels): w, h
- Left, right, top, bottom boundaries in image plane: l, r, t, b

#### Then:



- $O = C + d \cdot \mathbf{v} + l \cdot \mathbf{x} + b \cdot \mathbf{u}$
- Pixel at position i, j (i=0..w-1, j=0..h-1):

$$\begin{split} P_{i,j} &= O + i \cdot \frac{r - l}{w - 1} \cdot \mathbf{x} - j \cdot \frac{t - b}{h - 1} \cdot \mathbf{u} \\ &= O + i \cdot \Delta x \cdot \mathbf{x} - j \cdot \Delta y \cdot \mathbf{y} \end{split}$$

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#### Ray-Tracing – Generation of Rays



#### Ray in 3D Space:

$$\mathbf{R}_{i,j}(t) = C + t \cdot (P_{i,j} - C) = C + t \cdot \mathbf{v}_{i,j}$$

where  $t = \theta ... \infty$ 

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#### Ray Intersections



#### Task:

- Given an object o, find ray parameter t, such that  $\mathbf{R}_{i,j}(t)$  is a point on the object
- Such a value for t may not exist
- · Intersection test depends on geometric primitive

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#### **Ray Intersections**



#### Spheres at origin:

Implicit function:

$$S(x, y, z): x^2 + y^2 + z^2 = r^2$$

Ray equation:

$$\mathbf{R}_{i,j}(t) = C + t \cdot \mathbf{v}_{i,j} = \begin{pmatrix} c_x \\ c_y \\ c_z \end{pmatrix} + t \cdot \begin{pmatrix} v_x \\ v_y \\ v_z \end{pmatrix} = \begin{pmatrix} c_x + t \cdot v_x \\ c_y + t \cdot v_y \\ c_z + t \cdot v_z \end{pmatrix}$$

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#### **Ray Intersections**



#### To determine intersection:

• Insert ray  $\mathbf{R}_{i,i}(t)$  into S(x,y,z):

$$(c_x + t \cdot v_x)^2 + (c_v + t \cdot v_v)^2 + (c_z + t \cdot v_z)^2 = r^2$$

- Solve for t (find roots)
  - Simple quadratic equation

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#### **Ray Intersections**



#### Other Primitives:

- Implicit functions:
  - Spheres at arbitrary positions
  - Same thing
  - Conic sections (hyperboloids, ellipsoids, paraboloids, cones, cylinders)
    - Same thing (all are quadratic functions!)
  - Higher order functions (e.g. tori and other quartic functions)
  - In principle the same
  - But root-finding difficult
  - Net to resolve to numerical methods

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#### **Ray Intersections**



#### Other Primitives (cont)

- Polygons:
  - First intersect ray with plane
    - linear implicit function
- Then test whether point is inside or outside of polygon (2D test)
- For convex polygons
- Suffices to test whether point in on the right side of every boundary edge
- Similar to computation of outcodes in line clipping

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#### **Ray-Tracing**



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### Ray-Tracing – Geometric Transformations



#### **Geometric Transformations:**

- · Similar goal as in rendering pipeline:
- Modeling scenes convenient using different coordinate systems for individual objects
- · Problem:
  - Not all object representations are easy to transform
  - This problem is fixed in rendering pipeline by restriction to polygons (affine invariance!)

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## Ray-Tracing – Geometric Transformations



#### Geometric Transformations:

- Similar goal as in rendering pipeline:
  - Modeling scenes convenient using different coordinate systems for individual objects
- Problem:
- Not all object representations are easy to transform
- This problem is fixed in rendering pipeline by restriction to polygons (affine invariance!)
- -Ray-Tracing has different solution:
- The ray itself is always affine invariant!
- Thus: transform ray into object coordinates!

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#### Ray-Tracing – Geometric Transformations



#### Ray Transformation:

- For intersection test, it is only important that ray is in same coordinate system as object representation
- Transform all rays into object coordinates
  - Transform camera point and ray direction by <u>inverse</u> of model/view matrix
- Shading has to be done in world coordinates (where light sources are given)
- Transform object space intersection point to world coordinates
- Thus have to keep both world and object-space ray

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#### **Ray-Tracing**



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#### Ray-Tracing Lighting and Shading



#### Local Effects:

- Local Lighting
- Any reflection model possible
- Have to talk about light sources, normals...
- Texture mapping
  - Color textures
  - Bump maps
- Environment maps
- Shadow maps

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## Ray-Tracing Local Lighting



#### Light sources:

- For the moment: point and directional lights
- · Later: are light sources
- More complex lights are possible
  - Area lights
  - Global illumination
  - Other objects in the scene reflect light
  - Everything is a light source!
  - Talk about this on Monday

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## Ray-Tracing Local Lighting



#### Local surface information (normal...)

• For implicit surfaces F(x,y,z)=0: normal  $\mathbf{n}(x,y,z)$  can be easily computed at every intersection point using the gradient

$$\mathbf{n}(x, y, z) = \begin{pmatrix} \partial F(x, y, z) / \partial x \\ \partial F(x, y, z) / \partial y \\ \partial F(x, y, z) / \partial z \end{pmatrix}$$

• Example:

$$F(x, y, z) = x^2 + y^2 + z^2 - r^2$$

$$\mathbf{n}(x, y, z) = \begin{pmatrix} 2x \\ 2y \\ 2z \end{pmatrix}$$

Needs to be normalized!

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## Ray-Tracing Local Lighting



#### Local surface information

- Alternatively: can interpolate per-vertex information for triangles/meshes as in rendering pipeline
  - Phong shading!
  - Same as discussed for rendering pipeline
- Difference to rendering pipeline:
  - Interpolation cannot be done incrementally
  - Have to compute Barycentric coordinates for every intersection point (e.g plane equation for triangles)

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## Ray-Tracing Texture Mapping



#### Approach:

- · Works in principle like in rendering pipeline
- Given s, t parameter values, perform texture lookup
- Magnification, minification just as discussed
- Problem: how to get s, t
- Implicit surfaces often don't have parameterization
- For special cases (spheres, other conic sections), can use parametric representation
- Triangles/meshes: use interpolation from vertices

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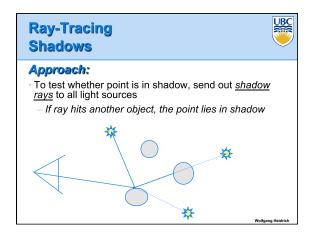
## Ray-Tracing Lighting and Shading

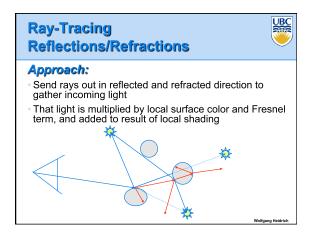


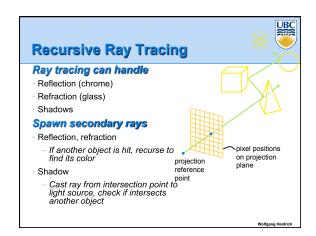
#### Global Effects

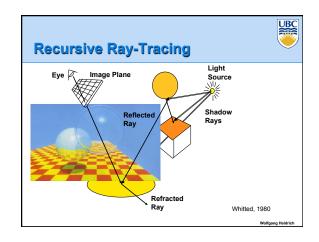
- Shadows
- Reflections/refractions

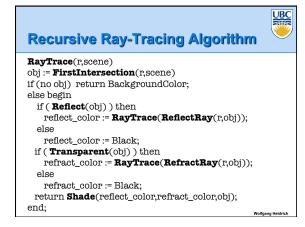
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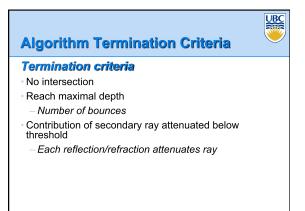


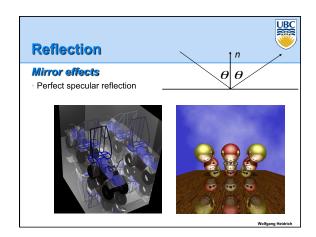


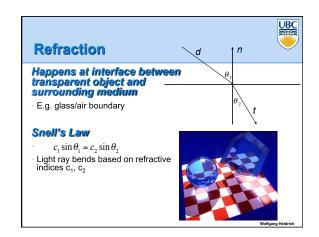


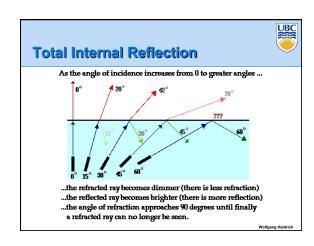


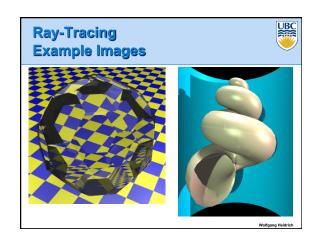












#### **Ray-Tracing Terminology**

#### **Terminology:**

- · Primary ray: ray starting at camera
- Shadow ray
- Reflected/refracted ray
- Ray tree: all rays directly or indirectly spawned off by a single primary ray

#### Note:

 Need to limit maximum depth of ray tree to ensure termination of ray-tracing process!

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#### **Ray-Tracing**

#### Issues:

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- Efficient data structures so we don't have to test intersection with every object

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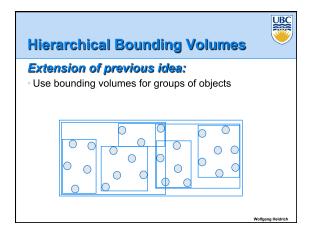
## Ray Tracing Data Structures Goal: reduce number of intersection tests per ray Lots of different approaches: (Hierarchical) bounding volumes Hierarchical space subdivision Oct-tree, k-D tree, BSP tree

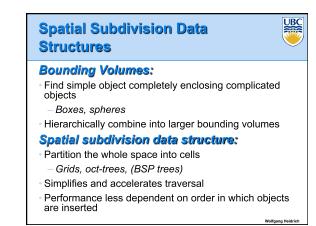
Rather than testing every ray against a potentially very complex object (e.g. triangle mesh), do a quick conservative test first which eliminates most rays

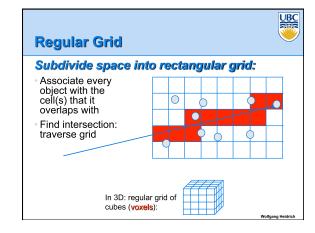
Surround complex object by simple, easy to test geometry (typically sphere or axis-aligned box)

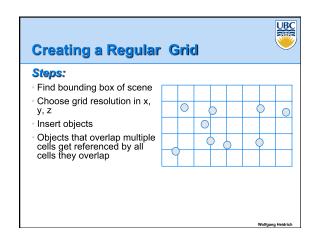
Want to make bounding volume as tight as possible!

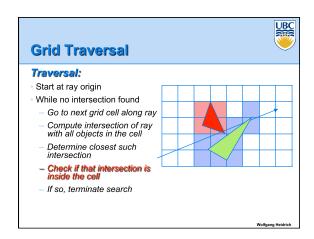
**Bounding Volumes** 

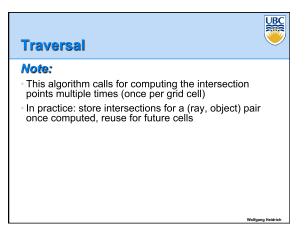












## Regular Grid Discussion Advantages? Easy to construct Easy to traverse Disadvantages? May be only sparsely filled Geometry may still be clumped

