



Texture Mapping

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Course News

Assignment 3

- Project
- Handout will be up on Wednesday

Homework 5

- Out later today (this time for real)
- Remember that these are good practice for the exams!

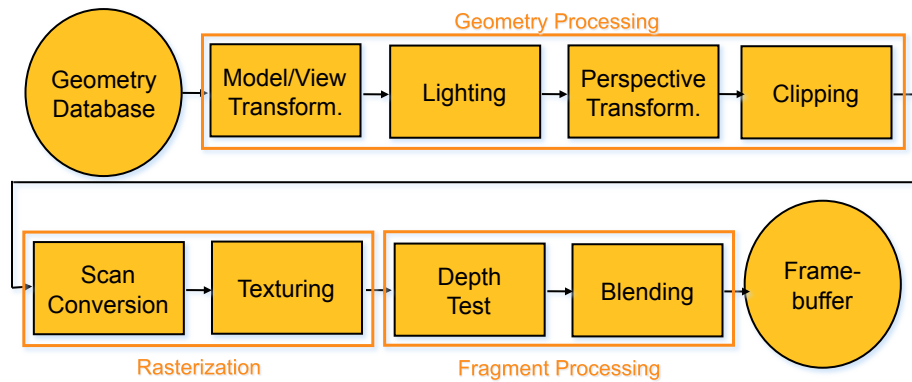
Reading

- Chapter 11 (Texture Mapping)

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The Rendering Pipeline

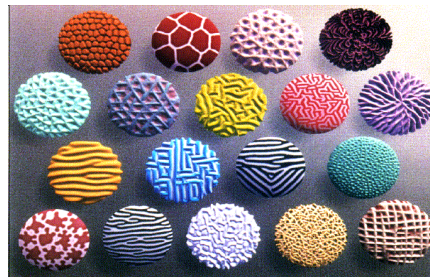


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Texture Mapping

- Real life objects have nonuniform colors, normals
- To generate realistic objects, reproduce coloring & normal variations = **texture**
- Can often replace complex geometric details



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Texture Mapping

Introduced to increase realism

- Lighting/shading models not enough

Hide geometric simplicity

- Images convey illusion of geometry
- Map a brick wall texture on a flat polygon
- Create bumpy effect on surface

Associate 2D information with 3D surface

- Point on surface corresponds to a point in texture
- “Paint” image onto polygon

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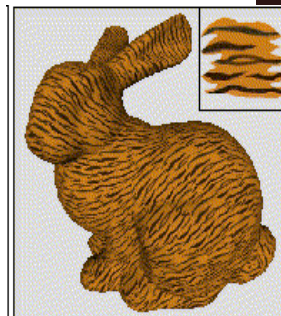
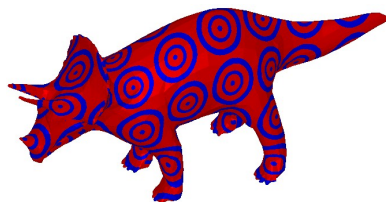


Color Texture Mapping

Define color (RGB) for each point on object surface

Two approaches

- Surface texture map (2D)
- Volumetric texture (3D)



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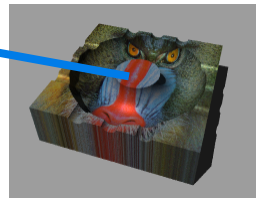
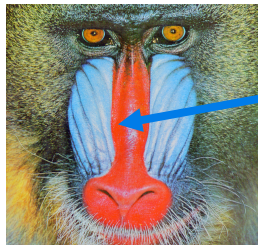
Surface (2D) Textures: Texture Coordinates



Texture map: 2D array of color (texels)
**Assigning texture coordinates (s,t) at vertex
with object coordinates (x,y,z,w)**

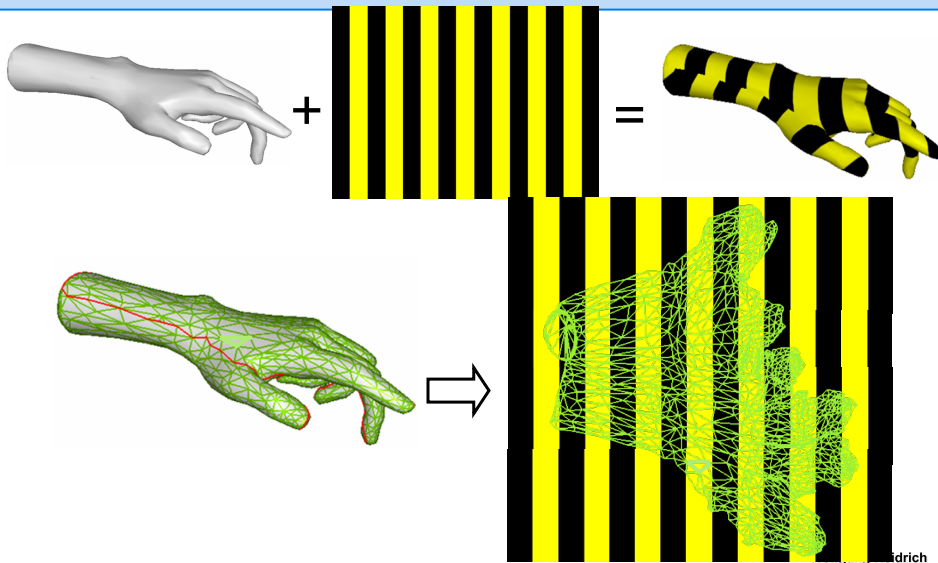
- Use interpolated (s,t) for texel lookup at each pixel
- Use value to modify a polygon's color
- Specified by programmer or artist

```
glTexCoord2f(s, t)  
glVertexf(x, y, z, w)
```



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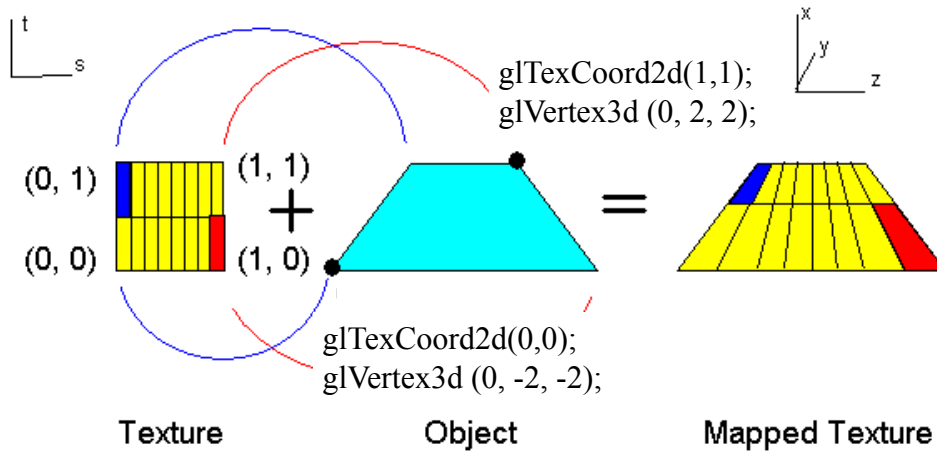
Texture Mapping Example



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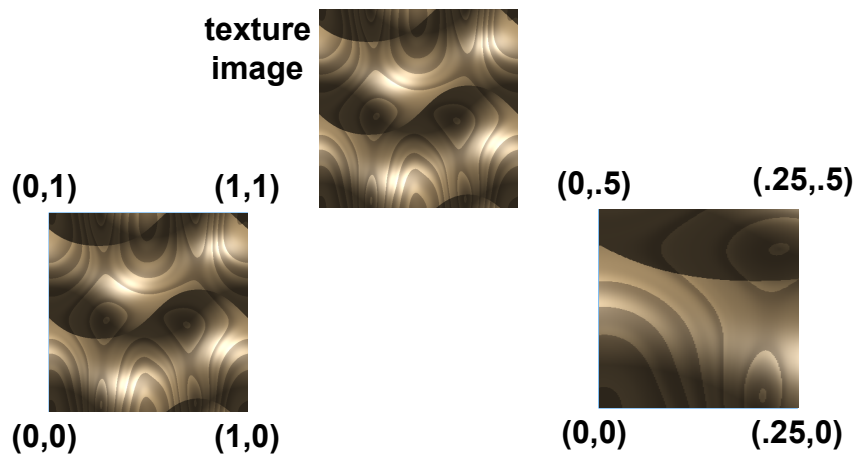
Example Texture Map



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Fractional Texture Coordinates



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Texture Lookup: Tiling and Clamping



What if s or t is outside the interval $[0...1]$? Multiple choices

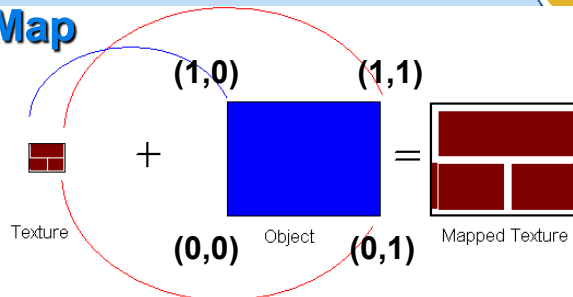
- Use fractional part of texture coordinates
 - Cyclic repetition of texture to tile whole surface
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_REPEAT, GL_TEXTURE_WRAP_T, GL_REPEAT, ...)`
- Clamp every component to range $[0...1]$
 - Re-use color values from texture image border
`glTexParameteri(..., GL_TEXTURE_WRAP_S, GL_CLAMP, GL_TEXTURE_WRAP_T, GL_CLAMP, ...)`

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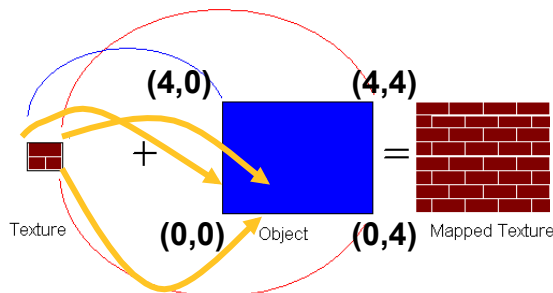
Tiled Texture Map



```
glTexCoord2d(1, 1);  
glVertex3d(x, y, z);
```



```
glTexCoord2d(4, 4);  
glVertex3d(x, y, z);
```



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Texture Coordinate Transformation

Motivation

- Change scale, orientation of texture on an object

Approach

- Texture matrix stack
- Transforms specified (or generated) tex coords

```
glMatrixMode( GL_TEXTURE );
```

```
glLoadIdentity();
```

```
glRotate();
```

...

- More flexible than changing (s,t) coordinates

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Texture Functions

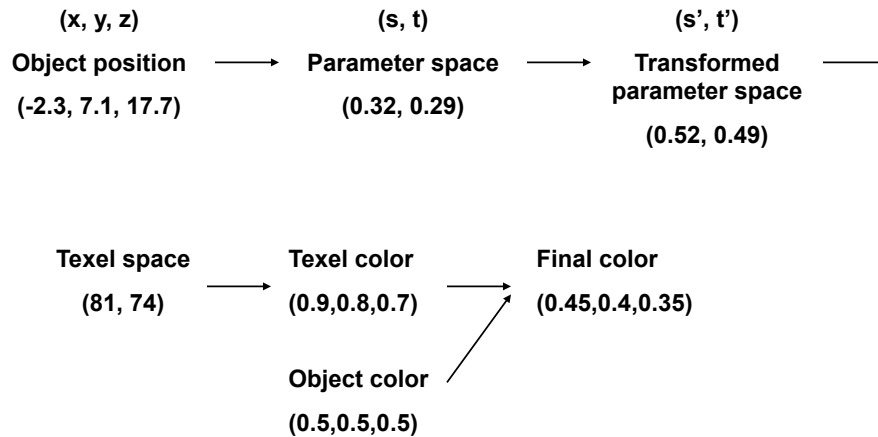
Given value from the texture map, we can:

- Directly use as surface color: GL_REPLACE
 - *Throw away old color, lose lighting effects*
- Modulate surface color: GL_MODULATE
 - *Multiply old color by new value, keep lighting info*
 - *Texturing happens after lighting, not relit*
- Use as surface color, modulate alpha: GL_DECAL
 - *Like replace, but supports texture transparency*
- Blend surface color with another: GL_BLEND
 - *New value controls which of 2 colors to use*

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Texture Pipeline



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Texture Objects and Binding

Texture object

- An OpenGL data type that keeps textures resident in memory and provides identifiers to easily access them
- Provides efficiency gains over having to repeatedly load and reload a texture
- You can prioritize textures to keep in memory
- OpenGL uses least recently used (LRU) if no priority is assigned

Texture binding

- Which texture to use right now
- Switch between preloaded textures

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Basic OpenGL Texturing

Create a texture object and fill w/ data:

- `glGenTextures(num, &indices)` to get identifiers for the objects
- `glBindTexture(GL_TEXTURE_2D, identifier)` to bind
 - *Following texture commands refer to the bound texture*
- `glTexParameterf(GL_TEXTURE_2D, ..., ...)` to specify parameters for use when applying the texture
- `glTexImage2D(GL_TEXTURE_2D,)` to specify the texture data (the image itself)

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Basic OpenGL Texturing (cont.)

Enable texturing:

- `glEnable(GL_TEXTURE_2D)`

State how the texture will be used:

- `glTexEnvf(...)`

Specify texture coordinates for the polygon:

- Use `glTexCoord2f(s,t)` before each vertex:
 - `glTexCoord2f(0,0); glVertex3f(x,y,z);`

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Low-Level Details

Large range of functions for controlling layout of texture data

- State how the data in your image is arranged
- e.g.: `glPixelStorei(GL_UNPACK_ALIGNMENT, 1)` tells OpenGL not to skip bytes at the end of a row
- You must state how you want the texture to be put in memory: how many bits per “pixel”, which channels,...

Textures must have a size of power of 2

- Common sizes are 32x32, 64x64, 256x256
- But don't need to be square, i.e. 32x64 is fine
- Smaller uses less memory, and there is a finite amount of texture memory on graphics cards

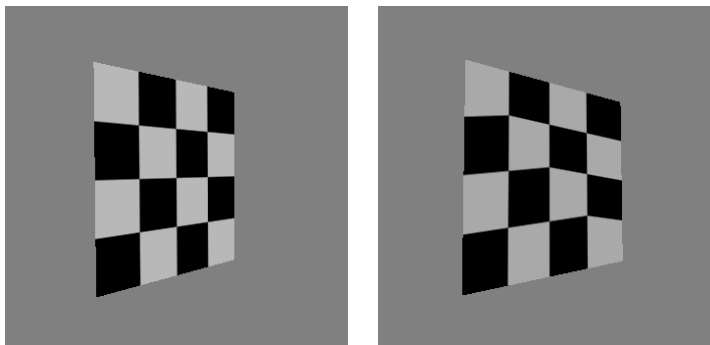
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Texture Mapping

Texture coordinate interpolation

- Perspective foreshortening problem



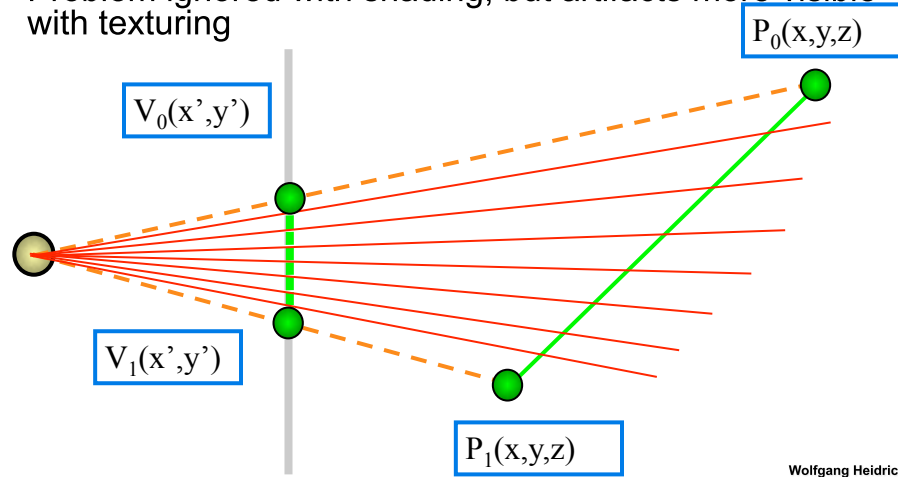
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Interpolation: Screen vs. World Space



Screen space interpolation incorrect

- Problem ignored with shading, but artifacts more visible with texturing



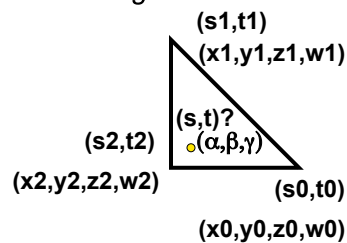
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Texture Coordinate Interpolation



Perspective correct interpolation

- α, β, γ :
 - Barycentric coordinates of a point P in a triangle
- s_0, s_1, s_2 :
 - Texture coordinates of vertices
- w_0, w_1, w_2 :
 - Homogeneous coordinates of vertices



$$s = \frac{\alpha \cdot s_0 / w_0 + \beta \cdot s_1 / w_1 + \gamma \cdot s_2 / w_2}{\alpha / w_0 + \beta / w_1 + \gamma / w_2}$$

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Texture Parameters

In addition to color can control other material/object properties

- Surface normal (bump mapping)
- Reflected color (environment mapping)



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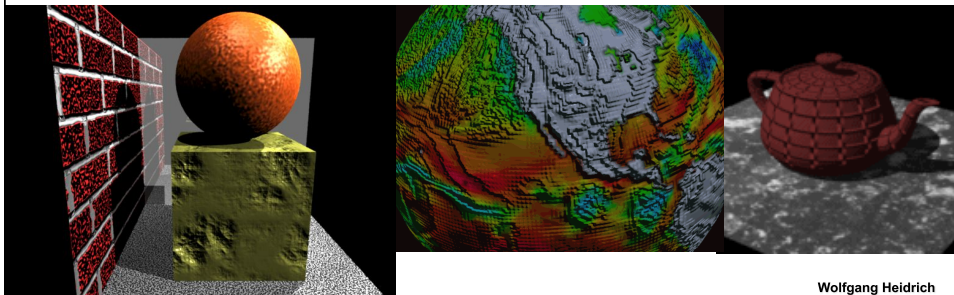


Bump Mapping: Normals As Texture

Object surface often not smooth – to recreate correctly need complex geometry model

Can control shape “effect” by locally perturbing surface normal

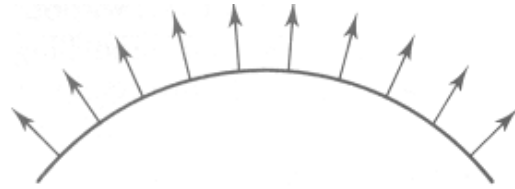
- Random perturbation
- Directional change over region



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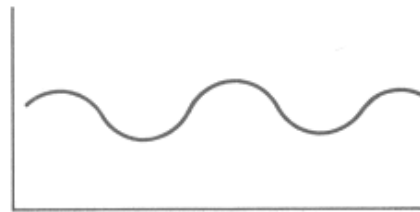


Bump Mapping



$O(u)$

Original surface



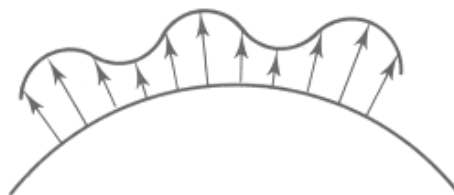
$B(u)$

A bump map

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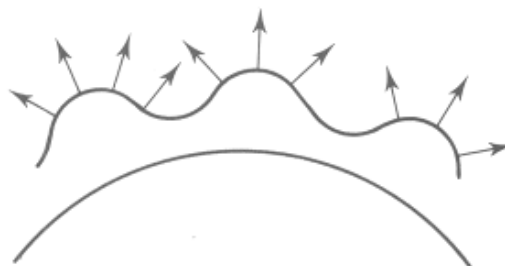


Bump Mapping



$O'(u)$

Lengthening or shortening
 $O(u)$ using $B(u)$



$N'(u)$

The vectors to the
'new' surface

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Displacement Mapping

Bump mapping gets silhouettes wrong

- Shadows wrong too

Change surface geometry instead

- Need to subdivide surface

GPU support

- Bump and displacement mapping not directly supported: require per-pixel lighting
- However: modern GPUs allow for programming both yourself



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Environment Mapping

Cheap way to achieve reflective effect

- Generate image of surrounding
- Map to object as texture

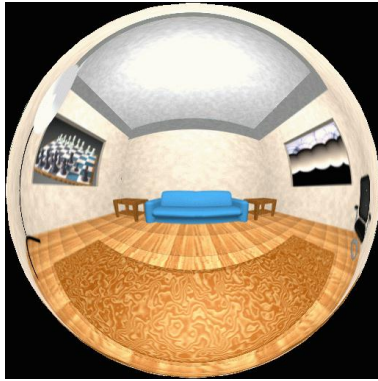


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Sphere Mapping

Texture is distorted fish-eye view

- Point camera at mirrored sphere
- Spherical texture mapping creates texture coordinates that correctly index into this texture map

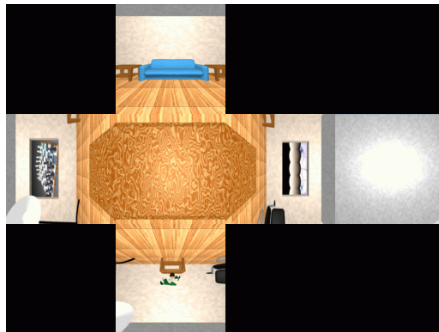


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Cube Mapping

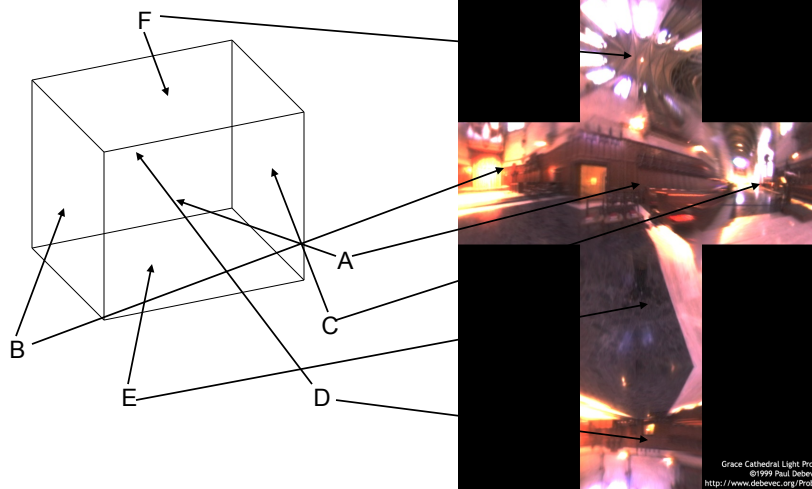
6 planar textures, sides of cube

- Point camera in 6 different directions, facing out from origin



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Cube Mapping



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Cube Mapping

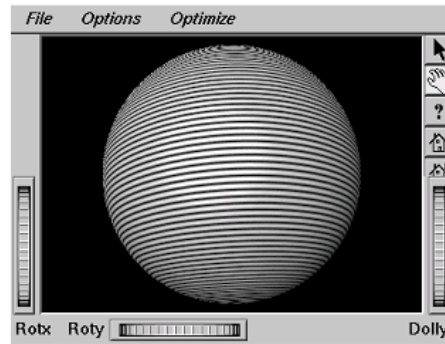
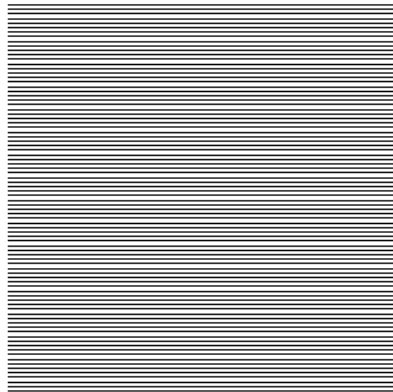
Direction of reflection vector r selects the face of the cube to be indexed

- Co-ordinate with largest magnitude
 - e.g., the vector $(-0.2, 0.5, -0.84)$ selects the $-Z$ face
- Remaining two coordinates (normalized by the 3rd coordinate) selects the pixel from the face.
 - E.g., $(-0.2, 0.5)$ gets mapped to $(0.38, 0.80)$
 - Why?

Difficulty in interpolating across faces

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Texture Lookup – Sampling & Reconstruction

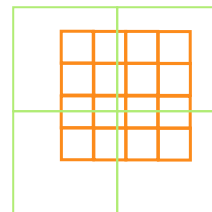
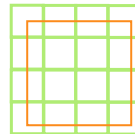


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Texture Lookup – Sampling & Reconstruction



- How to deal with:
 - **Pixels** that are much larger than **texels**?
 - Apply filtering, “averaging”
 - “Minification”
 - **Pixels** that are much smaller than **texels**?
 - Interpolate
 - “Magnification”



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Magnification: Interpolating Textures



- Nearest neighbor
- Bilinear
- Hermite (cubic)

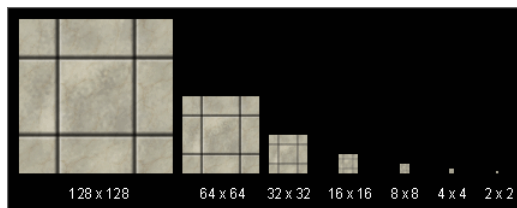


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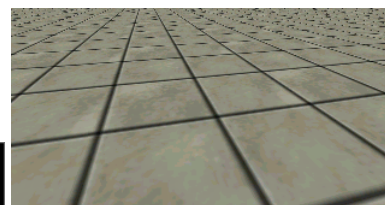
Minification: MIPmapping



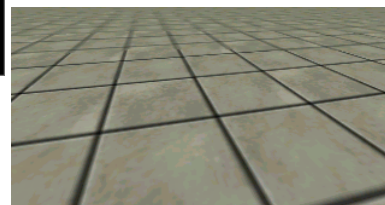
use “image pyramid” to precompute averaged versions of the texture



store whole pyramid in
single block of memory



Without MIP-mapping



With MIPmapping



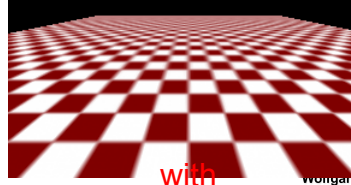
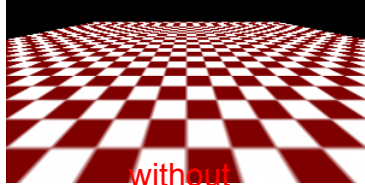
MIPmaps

Multum in parvo

- “many things in a small place”
- Series of prefiltered texture maps of decreasing resolutions
- Avoid shimmering and flashing as objects move

gluBuild2DMipmaps

- Automatically constructs a family of textures from original texture size down to 1x1



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MIPmap storage

Only 1/3 more space required



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Sampling & Reconstruction

CPSC 314

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Samples

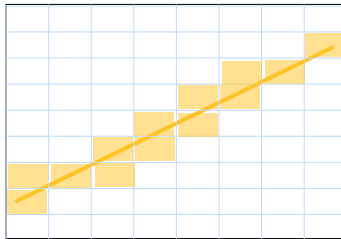
- Most things in the real world are **continuous**
- Everything in a computer is **discrete**
- The process of mapping a continuous function to a discrete one is called **sampling**
- The process of mapping a discrete function to a continuous one is called **reconstruction**
- The process of mapping a continuous variable to a discrete one is called **quantization**
- Rendering an image requires both **sampling** and **quantization**
- Displaying an image involves **reconstruction**

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Line Segments

- We tried to sample a line segment so it would map to a 2D raster display
- We quantized the pixel values to 0 or 1
- We saw stair steps, or jaggies

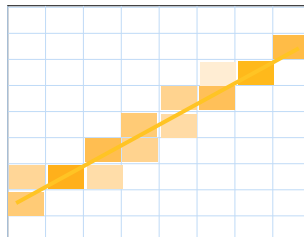


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Line Segments

- Instead, quantize to many shades
- But what sampling algorithm is used?



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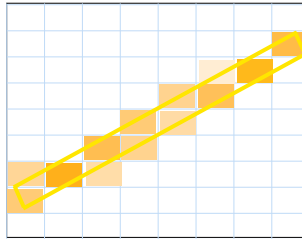


Unweighted Area Sampling

Shade pixels wrt area covered by thickened line
Equal areas cause equal intensity, regardless of distance from pixel center to area

- Rough approximation formulated by dividing each pixel into a finer grid of pixels

Primitive cannot affect intensity of pixel if it does not intersect the pixel



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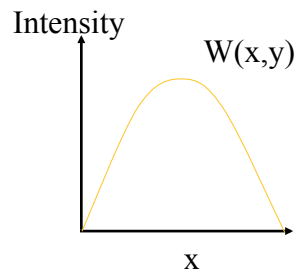
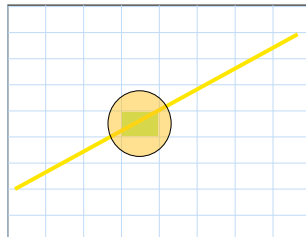


Weighted Area Sampling

Intuitively, pixel cut through the center should be more heavily weighted than one cut along corner

Weighting function, $W(x,y)$

- Specifies the contribution of primitive passing through the point (x, y) from pixel center



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Images

An image is a 2D function $I(x, y)$

- Specifies intensity for each point (x, y)
- (we consider each color channel independently)



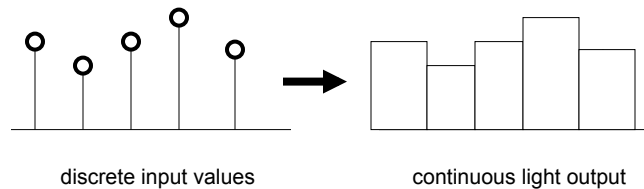
An image seen as a continuous 2D function

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Image Sampling and Reconstruction

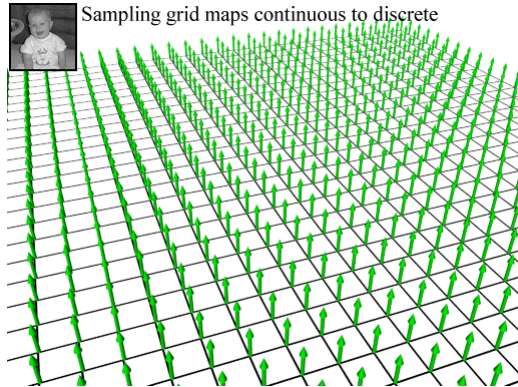
- Convert **continuous** image to **discrete** set of samples
- Display hardware **reconstructs** samples into continuous image
 - *Finite sized source of light for each pixel*



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Point Sampling an Image

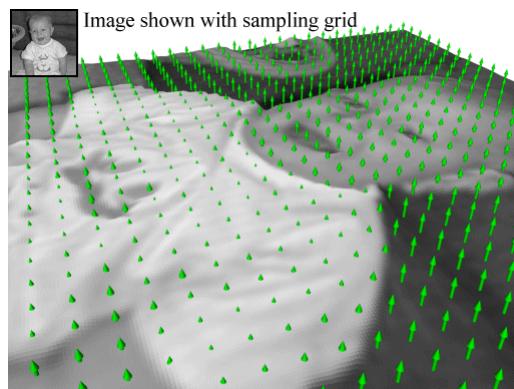
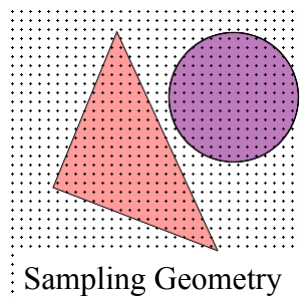
- Simplest sampling is on a grid
- Sample depends solely on value at grid points



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Point Sampling

Multiply sample grid by image intensity to obtain a discrete set of points, or samples.



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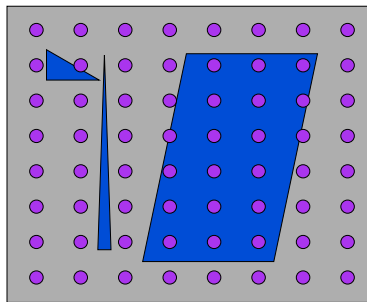


Sampling Errors

Some objects missed entirely, others poorly sampled

- Could try unweighted or weighted area sampling
- But how can we be sure we show everything?

Need to think about entire class of solutions!



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Image As Signal

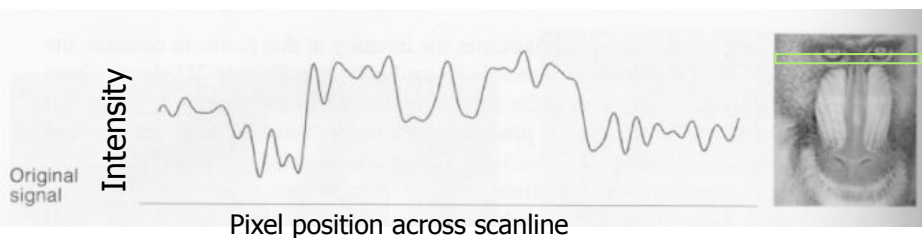
Image as spatial signal

2D raster image

- Discrete sampling of 2D spatial signal

1D slice of raster image

- Discrete sampling of 1D spatial signal



Examples from Foley, van Dam, Feiner, and Hughes

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Sampling Theory

How would we generate a signal like this out of simple building blocks?

Theorem

- Any signal can be represented as an (infinite) sum of sine waves at different frequencies

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Coming Up:

Friday

- Sampling & reconstruction

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