

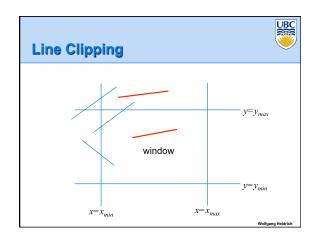
Line Clipping

Line segment:

• (p1,p2)

Trivial cases:

- \circ OC(p1)== 0 && OC(p2)==0
- Both points inside window, thus line segment completely visible (trivial accept)
- (OC(p1) & OC(p2))!= 0 (i.e. bitwise "and"!)
 - There is (at least) one boundary for which both points are outside (same flag set in both outcodes)
 - Thus line segment completely outside window (trivial



Line Clipping



α-Clipping

- · Handling of all the non-trivial cases
- Improvement of earlier algorithms (Cohen/Sutherland, Cyrus/Beck, Liang/Barsky)
- Define <u>window-edge-coordinates</u> of a point $\mathbf{p} = (x,y)^T$
 - $WEC_L(\mathbf{p}) = x x_{min}$
- $WEC_R(\mathbf{p}) = x_{max} x$
- $WEC_B(\mathbf{p}) = y y_{min}$

Negative if outside!

 $WEC_T(\mathbf{p}) = y_{max} - y$

Line Clipping



α-Clipping

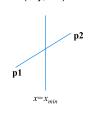
- Line segment defined as: p1+ α (p2-p1)
- Intersection point with one of the borders (say, left):

$$x_{1} + \alpha(x_{2} - x_{1}) = x_{min} \Leftrightarrow$$

$$\alpha = \frac{x_{min} - x_{1}}{x_{2} - x_{1}}$$

$$= \frac{x_{min} - x_{1}}{(x_{2} - x_{min}) - (x_{1} - x_{min})}$$

$$= \frac{\text{WEC}_{L}(x_{1})}{\text{WEC}_{L}(x_{1}) - \text{WEC}_{L}(x_{2})}$$



Line Clipping



α-Clipping: algorithm

alphaClip(p1, p2, window) {

Determine window-edge-coordinates of p1, p2

Determine outcodes OC(p1), OC(p2)

Handle trivial accept and reject

 $\alpha 1 = 0$; // line parameter for first point

 $\alpha 2=1$; // line parameter for second point

Line Clipping

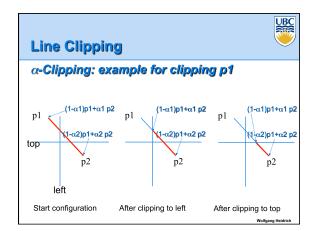


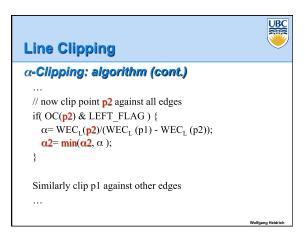
 α -Clipping: algorithm (cont.)

// now clip point p1 against all edges

if(OC(p1) & LEFT_FLAG) { α = WEC_L(p1)/(WEC_L(p1) - WEC_L(p2)); $\alpha 1 = \max(\alpha 1, \alpha);$

Similarly clip p1 against other edges





```
Line Clipping

\alpha-Clipping: algorithm (cont.)

...

// wrap-up

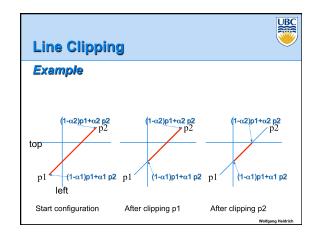
if(\alpha1 > \alpha2 )

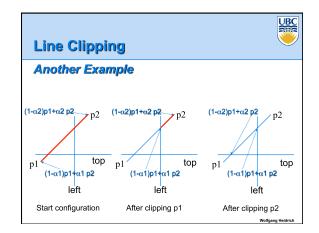
no output;

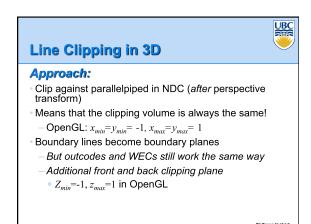
else

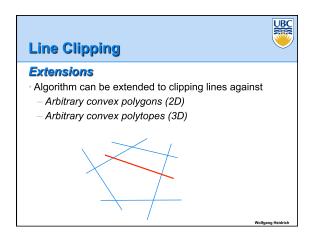
output line from p1+\alpha1(p2-p1) to p1+\alpha2(p2-p1)

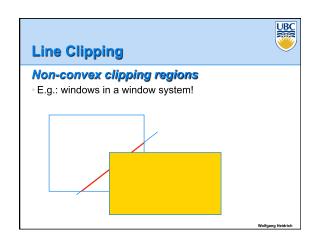
} // end of algorithm
```

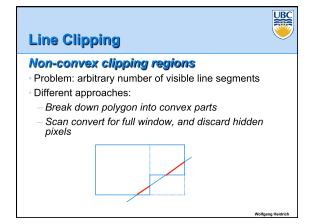


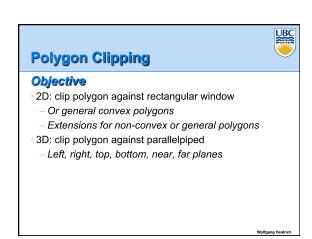


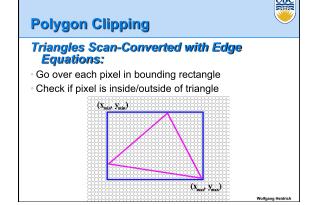


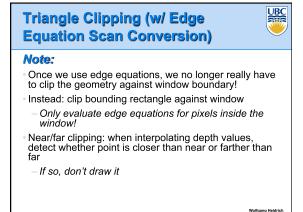


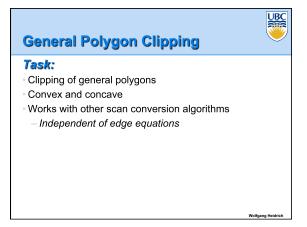


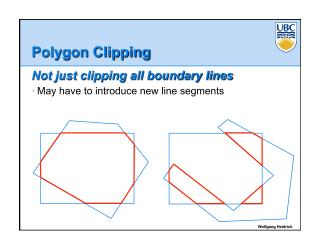


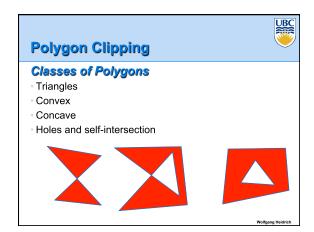


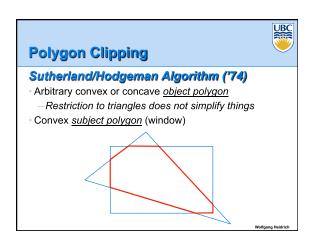


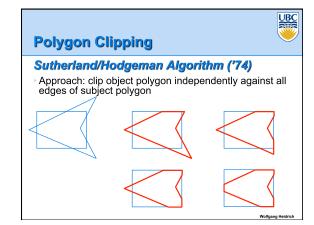


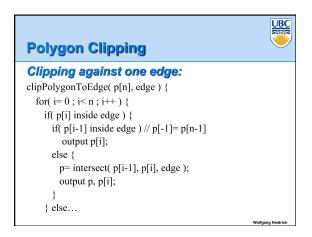


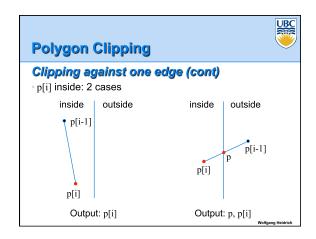


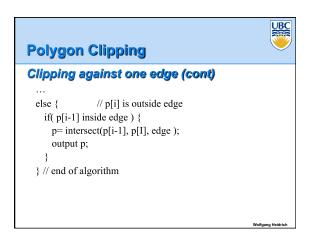


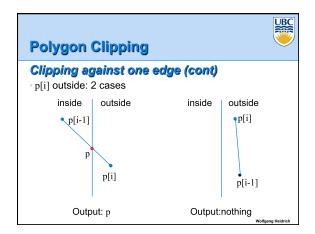


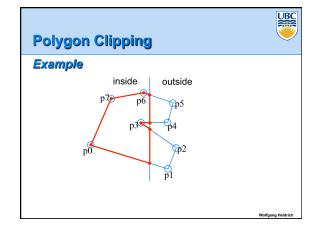




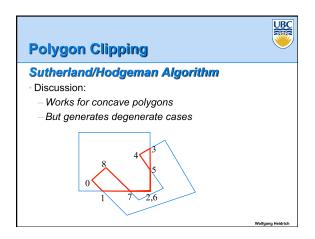








Polygon Clipping Sutherland/Hodgeman Algorithm Inside/outside tests: outcodes Intersection of line segment with edge: window-edge coordinates Similar to Cohen/Sutherland algorithm for line clipping



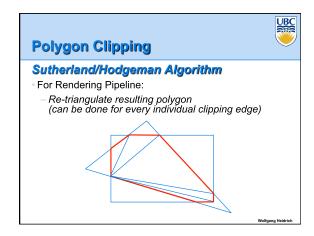
Polygon Clipping



Sutherland/Hodgeman Algorithm

- Discussion:
 - Clipping against individual edges independent
 - Great for hardware (pipelining)
 - All vertices required in memory at the same time
 - Not so good, but unavoidable
 - Another reason for using triangles only in hardware rendering

Volfgang Heidrich



Polygon Clipping



Other Polygon Clipping Algorithms

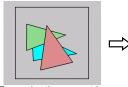
- · Weiler/Aetherton '77:
- Arbitrary concave polygons with holes both as subject and as object polygon
- Vatti '92:
 - Self intersection allowed as well
- · ... many more
 - Improved handling of degenerate cases
- But not often used in practice due to high complexity

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Occlusion



For most interesting scenes, some polygons overlap





 To render the correct image, we need to determine which polygons occlude which

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Painter's Algorithm



 Simple: render the polygons from back to front, "painting over" previous polygons







Draw cyan, then green, then red

will this work in the general case?

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Painter's Algorithm: Problems



- Intersecting polygons present a problem
- Even non-intersecting polygons can form a cycle with no valid visibility order:



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Hidden Surface Removal



Object Space Methods:

- Work in 3D before scan conversion
- E.g. Painter's algorithm
- Usually independent of resolution
 - Important to maintain independence of output device (screen/printer etc.)

Image Space Methods:

- Work on per-pixel/per fragment basis after scan conversion
- · Z-Buffer/Depth Buffer
- · Much faster, but resolution dependent

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The Z-Buffer Algorithm What happens if multiple primitives occupy the same pixel on the screen? Which is allowed to paint the pixel?

The Z-Buffer Algorithm



Idea: retain depth after projection transform

- · Each vertex maintains z coordinate
- Relative to eye point
- Can do this with canonical viewing volumes

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The Z-Buffer Algorithm



Augment color framebuffer with Z-buffer

- Also called depth buffer
- Stores z value at each pixel
- $\, \bullet \,$ At frame beginning, initialize all pixel depths to $\infty \,$
- When scan converting: interpolate depth (z) across polygon
- Check z-buffer before storing pixel color in framebuffer and storing depth in z-buffer
- don't write pixel if its z value is more distant than the z value already stored there

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Z-Buffer



Store (r,g,b,z) for each pixel

typically 8+8+8+24 bits, can be more
for all i,j {
 Depth[i,j] = MAX_DEPTH
 Image[i,j] = BACKGROUND_COLOUR
}
for all polygons P {
 for all pixels in P {
 if (Z_pixel < Depth[i,j]) {
 Image[i,j] = C_pixel
 Depth[i,j] = Z_pixel
 }
}</pre>

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Interpolating Z

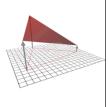


Edge walking

Just interpolate Z along edges and across spans

Barycentric coordinates

- Interpolate z like other parameters
- E.g. color



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The Z-Buffer Algorithm (mid-70's)

History:

- Object space algorithms were proposed when memory was expensive
- First 512x512 framebuffer was >\$50,000!

Radical new approach at the time

- The big idea:
- Resolve visibility independently at each pixel

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Depth Test Precision



- Reminder: projective transformation maps eyespace z to generic z-range (NDC)
- Simple example:

Thus:

$$T\begin{pmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & a & b \\ 0 & 0 & -1 & 0 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

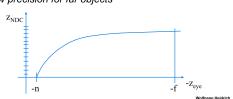
 $z_{NDC} = \frac{a z_{eye} + b}{z_{eye}} = a + \frac{b}{z_{eye}}$

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Depth Test Precision



- Therefore, depth-buffer essentially stores 1/z, rather than z!
- Issue with integer depth buffers
- High precision for near objects
- Low precision for far objects



Depth Test Precision



- Low precision can lead to depth fighting for far objects
 - Two different depths in eye space get mapped to same depth in framebuffer
 - Which object "wins" depends on drawing order and scan-conversion
- Gets worse for larger ratios f:n
 - Rule of thumb: $f:n \le 1000$ for 24 bit depth buffer
- With 16 bits cannot discern millimeter differences in objects at 1 km distance

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Z-Buffer Algorithm Questions



- · How much memory does the Z-buffer use?
- Does the image rendered depend on the drawing order?
- Does the time to render the image depend on the drawing order?
- How does Z-buffer load scale with visible polygons? with framebuffer resolution?

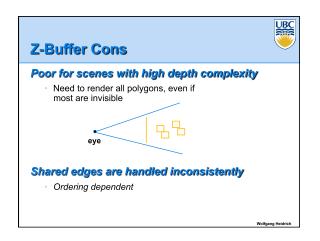
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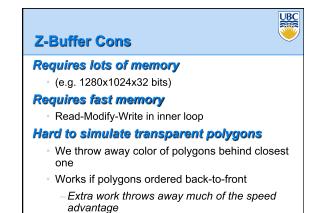
Z-Buffer Pros



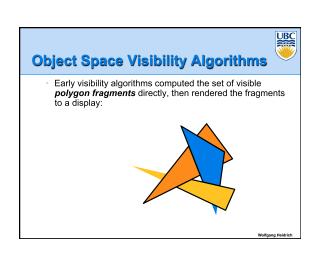
- Simple!!!
- Easy to implement in hardware
 - Hardware support in all graphics cards today
- · Polygons can be processed in arbitrary order
- Easily handles polygon interpenetration

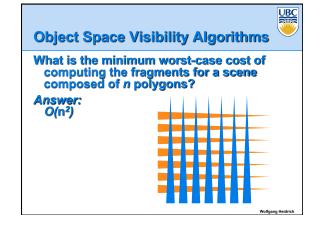
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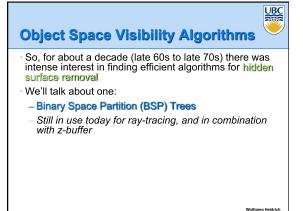




Object Space Algorithms Determine visibility on object or polygon level Using camera coordinates Resolution independent Explicitly compute visible portions of polygons Early in pipeline After clipping Requires depth-sorting Painter's algorithm BSP trees





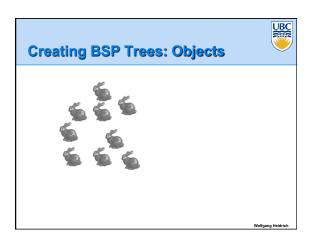


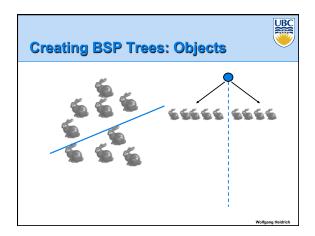
Binary Space Partition Trees (1979)

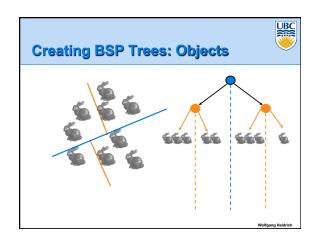
BSP Tree: partition space with binary tree of planes

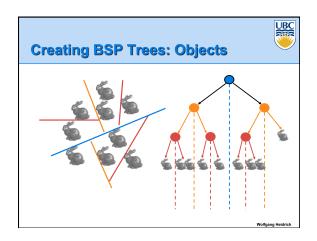
- Idea: divide space recursively into half-spaces by choosing splitting planes that separate objects in scene
- Preprocessing: create binary tree of planes
- Runtime: correctly traversing this tree enumerates objects from back to front

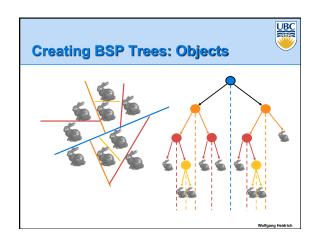
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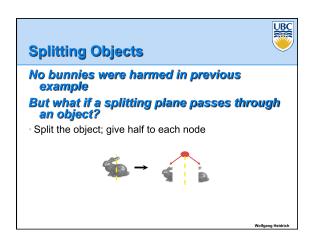








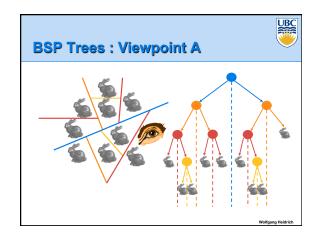


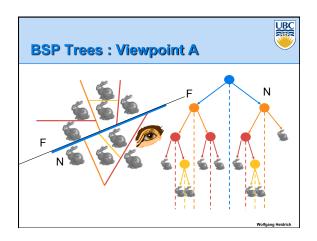


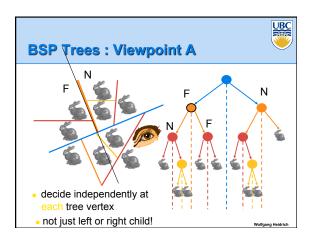


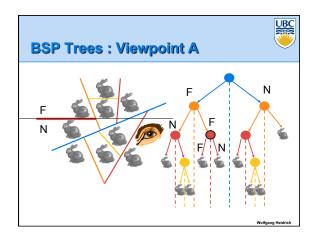
Traversing BSP Trees

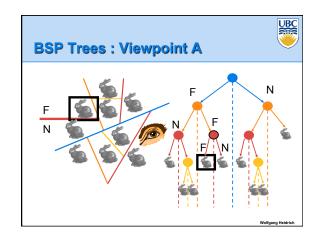
renderBSP(BSPtree *T)
BSPtree *near, *far;
if (eye on left side of T->plane)
 near = T->left; far = T->right;
else
 near = T->right; far = T->left;
renderBSP(far);
if (T is a leaf node)
 renderObject(T)
renderBSP(near);

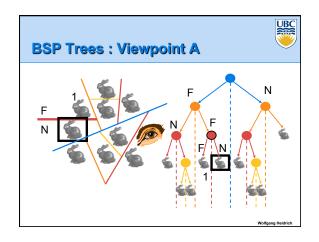


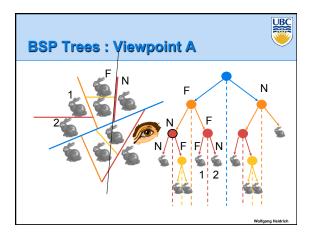


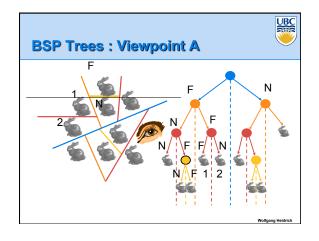


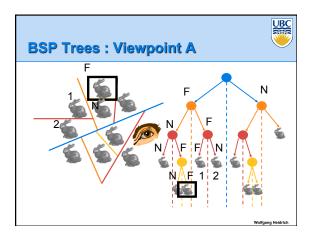


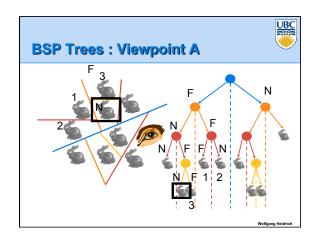


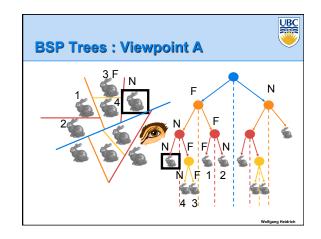


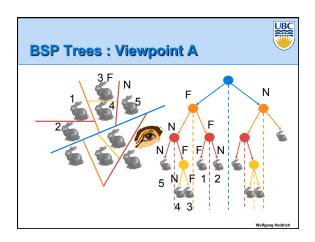


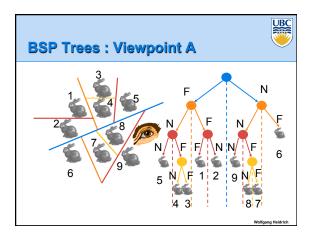


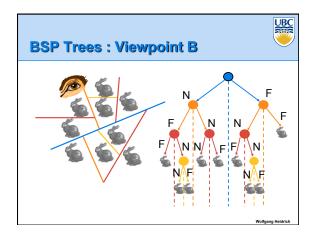


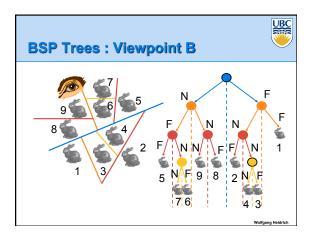






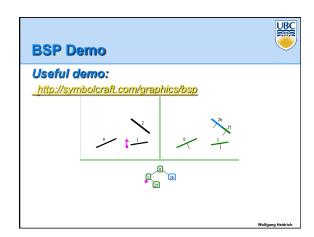








- Classify all polygons into positive or negative half-space of the plane
 - If a polygon intersects plane, split polygon into two and classify them both
- Recurse down the negative half-space
- Recurse down the positive half-space



Summary: BSP Trees



- Simple, elegant scheme
- Correct version of painter's algorithm back-to-front rendering approach
- Still very popular for video games (but getting less so)

- Slow(ish) to construct tree: O(n log n) to split, sort
- Splitting increases polygon count: O(n2) worst-
- Computationally intense preprocessing stage restricts algorithm to static scenes

Coming Up:



After Reading Week

- More hidden surface removal
- Blending
- Texture mapping