

Scan Conversion

Wolfgang Heidrich

Wolfgang Heidricl

Course News

Assignment 2

Due Monday, Feb 28

Homework 3

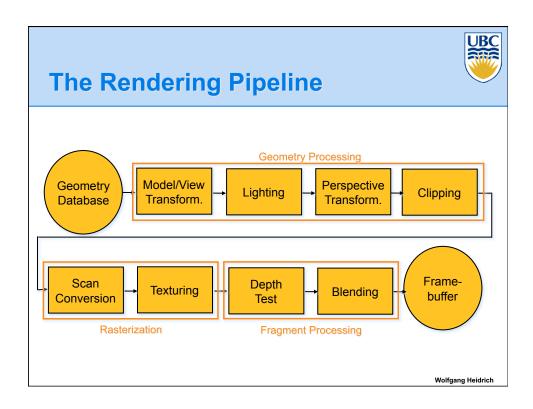
Discussed in labs this week

Homework 4

Hidden surface removal, out today

Reading

- · Chapters 8, 9
- Hidden surface removal, shading



Scan Conversion - Rasterization



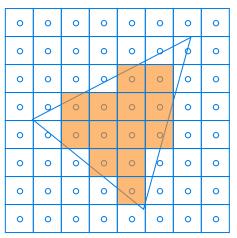
Convert continuous rendering primitives into discrete fragments/pixels

- Lines
 - Midpoint/Bresenham
- Triangles
 - Flood fill
 - Scanline
 - Implicit formulation
- Interpolation



Scan Conversion of Polygons

One possible scan conversion



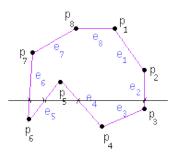
Wolfgang Heidrich



Scan Conversion of Polygons

A General Algorithm

- Intersect each scanline with all edges
- Sort intersections in x
- Calculate parity to determine in/out
- Fill the 'in' pixels





Edge Walking

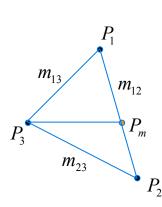
```
for (y=yB; y<=yT; y++) {
  for (x=xL; x<=xR; x++)
     setPixel(x,y);
  xL += DxL;
  xR += DxR;
}</pre>
```

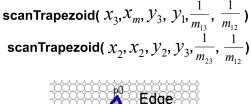
Wolfgang Heidrich

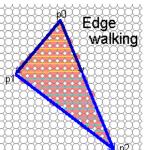
Edge Walking Triangles



 Split triangles into two regions with continuous left and right edges



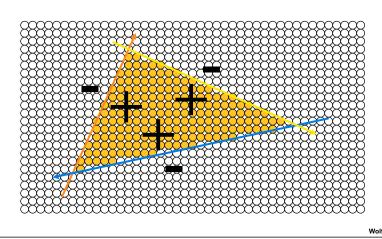




Modern Rasterization: Edge Equations



Define a triangle as follows:

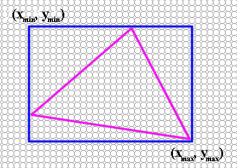


Using Edge Equations



Usage:

- Go over each pixel in bounding rectangle
- Check if pixel is inside/outside of triangle
 - Using sign of edge equations





Computing Edge Equations

Implicit equation of a triangle edge:

$$L(x, y) = \frac{(y_e - y_s)}{(x_e - x_s)}(x - x_s) - (y - y_s) = 0$$

(see Bresenham algorithm)

 L(x,y) positive on one side of edge, negative on the other

Question:

• What happens for vertical lines?

Wolfgang Heidrich



Edge Equations

Multiply with denominator

$$L(x,y) = (y_e - y_s)(x - x_s) - (y - y_s)(x_e - x_s) = 0$$

- Avoids singularity
- Works with vertical lines

What about the sign?

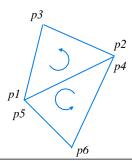
• Which side is in, which is out?



Edge Equations

Determining the sign

- Which side is "in" and which is "out" depends on order of start/end vertices...
- · Convention: specify vertices in counter-clockwise order



Wolfgang Heidrich



Edge Equations

Counter-Clockwise Triangles

- The equation L(x,y) as specified above is negative inside, positive outside
 - Flip sign:

$$L(x,y) = -(y_e - y_s)(x - x_s) + (y - y_s)(x_e - x_s) = 0$$

Clockwise triangles

Use original formula

$$L(x,y) = (y_a - y_s)(x - x_s) - (y - y_s)(x_a - x_s) = 0$$

Discussion of Polygon Scan Conversion Algorithms



On old hardware:

- Use first scan-conversion algorithm
 - Scan-convert edges, then fill in scanlines
 - Compute interpolated values by interpolating along edges, then scanlines
- Requires clipping of polygons against viewing volume
- Faster if you have a few, large polygons
- Possibly faster in software

Wolfgang Heidrich

Discussion of Polygon Scan Conversion Algorithms



Modern GPUs:

- Use edge equations
 - And plane equations for attribute interpolation
 - No clipping of primitives required
- Faster with many small triangles

Additional advantage:

- Can control the order in which pixels are processed
- Allows for more memory-coherent traversal orders
 - E.g. tiles or space-filling curve rather than scanlines

Triangle Rasterization Issues (Independent of Algorithm)



Exactly which pixels should be lit?

A: Those pixels inside the triangle edge (of course)

But what about pixels exactly on the edge?

- Draw them: order of triangles matters (it shouldn't)
- Don't draw them: gaps possible between triangles

We need a consistent (if arbitrary) rule

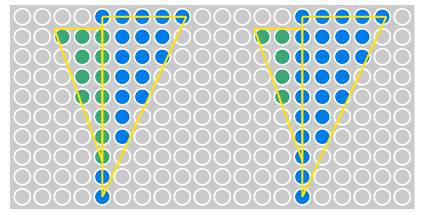
 Example: draw pixels on left or top edge, but not on right or bottom edge

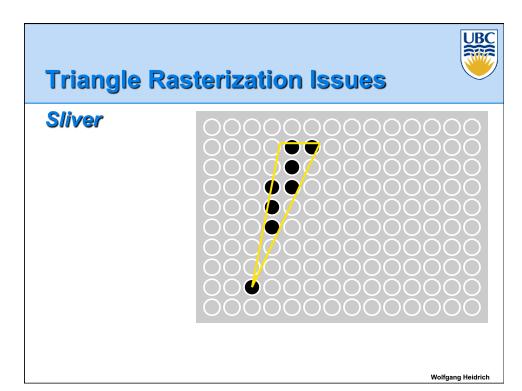
Wolfgang Heidrich

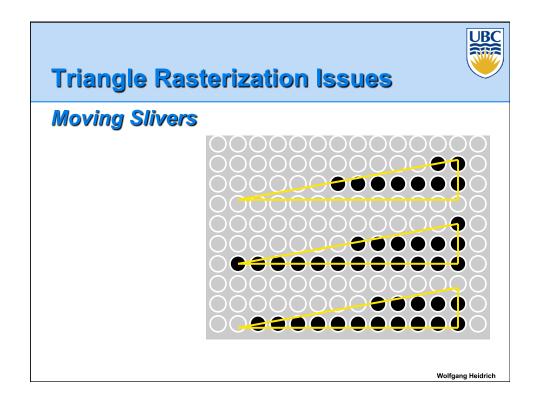
Triangle Rasterization Issues



Shared Edge Ordering









Triangle Rasterization Issues

These are ALIASING Problems

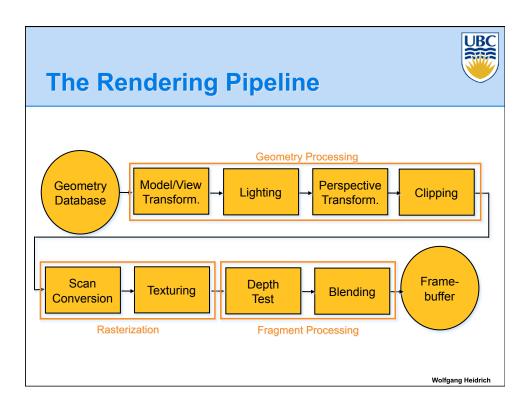
- Problems associated with representing continuous functions (triangles) with finite resolution (pixels)
- More on this problem when we talk about sampling...

Wolfgang Heidrich



Shading

Wolfgang Heidrich



Shading



Input to Scan Conversion:

- Vertices of triangles (lines, quadrilaterals...)
- Color (per vertex)
 - Specified with glColor
 - Or: computed with lighting
- World-space normal (per vertex)
 - Left over from lighting stage

Shading Task:

Determine color of every pixel in the triangle



Shading

How can we assign pixel colors using this information?

- Easiest: flat shading
 - Whole triangle gets one color (color of 1st vertex)
- Better: Gouraud shading
 - Linearly interpolate color across triangle
- Even better:
 - Linearly interpolate the normal vector
 - Compute lighting for every pixel
 - Note: not supported by rendering pipeline as discussed so far

Wolfgang Heidrich



Flat Shading

 Simplest approach calculates illumination at a single point for each polygon



Obviously inaccurate for smooth surfaces

Flat Shading Approximations

If an object really <u>is</u> faceted, is this accurate?



Wolfgang Heidrich

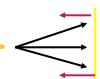
Flat Shading Approximations

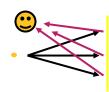
If an object really <u>is</u> faceted, is this accurate?

no!

- For point sources, the direction to light varies across the facet
- For specular reflectance, direction to eye varies across the facet









Improving Flat Shading

What if evaluate Phong lighting model at each pixel of the polygon?

Better, but result still clearly faceted

For smoother-looking surfaces we introduce vertex normals at each vertex

- Usually different from facet normal
- Used only for shading
- Think of as a better approximation of the real surface that the polygons approximate

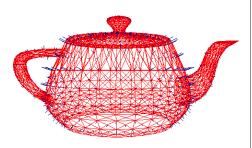
Wolfgang Heidrich



Vertex Normals

Vertex normals may be

- Provided with the model
- Computed from first principles
- Approximated by averaging the normals of the facets that share the vertex

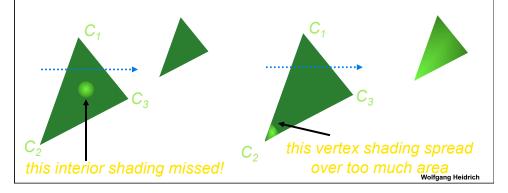




Gourand Shading Artifacts

often appears dull, chalky lacks accurate specular component

• if included, will be averaged over entire polygon

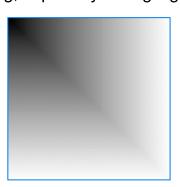


Gourand Shading Artifacts



Mach bands

- Eye enhances discontinuity in first derivative
- Very disturbing, especially for highlights





Phong Shading

linearly interpolating surface normal across the facet, applying Phong lighting model at every pixel

- Same input as Gouraud shading
- Pro: much smoother results
- Con: considerably more expensive



Not the same as Phong lighting

- Common confusion
- Phong lighting: empirical model to calculate illumination at a point on a surface



Wolfgang Heidrich

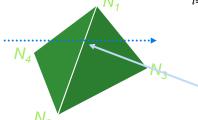
Phong Shading



Linearly interpolate the vertex normals

- Compute lighting equations at each pixel
- Can use specular component

$$I_{total} = k_a I_{ambient} + \sum_{i=1}^{\# lights} I_i \left(k_d \left(\mathbf{n} \cdot \mathbf{l_i} \right) + k_s \left(\mathbf{v} \cdot \mathbf{r_i} \right)^{n_{shiny}} \right)$$



remember: normals used in diffuse and specular terms

discontinuity in normal's rate of change harder to detect



Phong Shading Difficulties

Computationally expensive

- Per-pixel vector normalization and lighting computation!
- Floating point operations required

Lighting after perspective projection

- Messes up the angles between vectors
- · Have to keep eye-space vectors around

No direct support in standard rendering pipeline

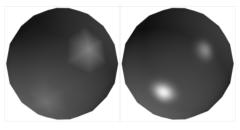
 But can be simulated with texture mapping, procedural shading hardware (see later)

Wolfgang Heidrich



Shading Artifacts: Silhouettes

Polygonal silhouettes remain



Gouraud Phong



How to Interpolate?

Need to propagate vertex attributes to pixels

- Interpolate between vertices:
 - z (depth)
 - r,g,b color components
 - $-N_x, N_y, N_z$ surface normals
 - u,v texture coordinates (talk about these later)
- Three equivalent ways of viewing this (for triangles)
 - 1. Linear interpolation
 - 2. Barycentric coordinates
 - 3. Plane Equation

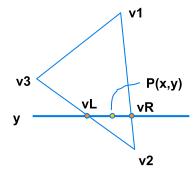
Wolfgang Heidrich



1. Linear Interpolation

Interpolate quantity along L and R edges

- (as a function of y)
- Then interpolate quantity as a function of x



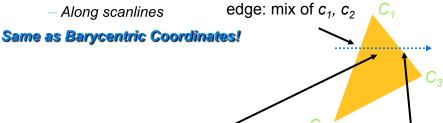


Linear Interpolation

Most common approach, and what OpenGL does

- Perform Phong lighting at the vertices
- Linearly interpolate the resulting colors over faces
 - Along edges

Along scanlines



interior: mix of c1, c2, c3

edge: mix of c1, c3

Wolfgang Heidrich



2. Barycentric Coordinates

Have seen this before

· Barycentric Coordinates: weighted combination of vertices, with weights summing to 1

$$P = \alpha \cdot P_1 + \beta \cdot P_2 + \gamma \cdot P_3$$

$$\alpha + \beta + \gamma = 1$$

$$0 \le \alpha, \beta, \gamma \le 1$$

$$P_1 \quad (1,0,0)$$

$$\beta = 0$$

$$\beta = 0.5$$



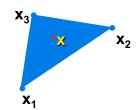
Barycentric Coordinates

Convex combination of 3 points

$$\mathbf{x} = \alpha \cdot \mathbf{x}_1 + \beta \cdot \mathbf{x}_2 + \gamma \cdot \mathbf{x}_3$$

with $\alpha + \beta + \gamma = 1, \ 0 \le \alpha, \beta, \gamma \le 1$

• α, β, and γ are called barycentric coordinates



Wolfgang Heidrich

Barycentric Coordinates



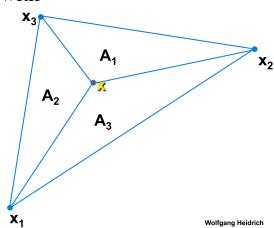
One way to compute them:

$$\mathbf{x} = \alpha \mathbf{x}_1 + \beta \mathbf{x}_2 + \gamma \mathbf{x}_3$$
 with

$$\alpha = A_1/A$$

$$\beta = A_2/A$$

$$\gamma = A_3/A$$





Barycentric Coordinates

How to compute areas?

Cross products!

• e.g:

e.g:
$$A_{1} = \frac{1}{2} \| (\mathbf{x}_{2} - \mathbf{x}_{1}) \times (\mathbf{x} - \mathbf{x}_{1}) \|$$

$$A_{2}$$

$$A_{3}$$



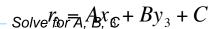
3. Plane Equation

Observation: Quantities vary linearly across image plane

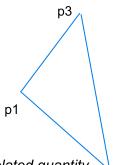
- E.g.: r = Ax + By + C
 - r= red channel of the color
 - Same for g, b, Nx, Ny, Nz, z...
- From info at vertices we know:

$$r_1 = Ax_1 + By_1 + C$$

$$r_2 = Ax_2 + By_2 + C$$



One-time set-up cost per triangle and interpolated quantity



Wolfgang Heidrich

p2



Coming Up:

Wednesday/Friday

Clipping, hidden surface removal