

Perspective Projection

Wolfgang Heidrich

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Course News

Assignment 1

Due January 31

Homework 2

- Exercise problems for perspective
- Discussed in labs next week

Quiz 1

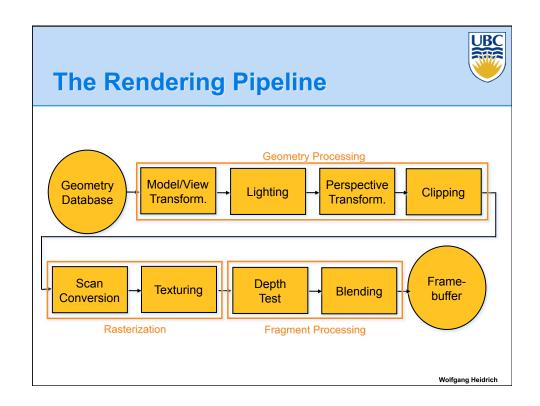
One week from today (Wed, Jan 26)



Course News (cont.)

Reading for Quiz (new book version):

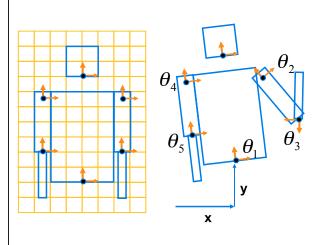
- Math prereq: Chapter 2.1-2.4, 4
- Intro: Chapter 1
- Affine transformations: Ch. 6 (Ch. 5, old book)
- Perspective: Ch 7 (Ch. 6, old book)
 - Also reading for this week...



Recap:

Transformation Hierarchies





```
glTranslate3f(x,y,0);
glRotatef(\theta_1,0,0,1);
DrawBody();
glPushMatrix();
 glTranslate3f(0,7,0);
 DrawHead();
glPopMatrix();
glPushMatrix();
 glTranslate(2.5,5.5,0);
 glRotatef(\theta_2,0,0,1);
 DrawUArm();
 glTranslate(0,-3.5,0);
 glRotatef(\theta_3,0,0,1);
 DrawLArm();
glPopMatrix();
... (draw other arm)
```

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Hierarchical Modeling



Advantages

- Define object once, instantiate multiple copies
- Transformation parameters often good control knobs
- Maintain structural constraints if well-designed

Limitations

- Expressivity: not always the best controls
- Can't do closed kinematic chains
 - Keep hand on hip



Display Lists

Concept:

 If multiple copies of an object are required, it can be compiled into a display list:

```
glNewList( listId, GL_COMPILE );
glBegin( ...);
... // geometry goes here
glEndList();
// render two copies of geometry offset by 1 in z-direction:
glCallList( listId );
glTranslatef( 0.0, 0.0, 1.0 );
glCallList( listId) ;
```

UBC

Display Lists

Advantages:

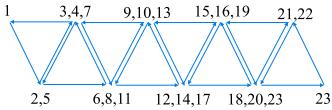
- More efficient than individual function calls for every vertex/attribute
- Can be cached on the graphics board (bandwidth!)
- Display lists exist across multiple frames
 - Represent static objects in an interactive application



Shared Vertices

Triangle Meshes

- Multiple triangles share vertices
- If individual triangles are sent to graphics board, every vertex is sent and transformed multiple times!
 - Computational expense
 - Bandwidth



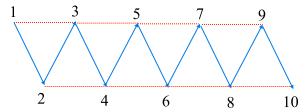
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Triangle Strips



Idea:

- Encode neighboring triangles that share vertices
- Use an encoding that requires only a constant-sized part of the whole geometry to determine a single triangle
- N triangles need n+2 vertices

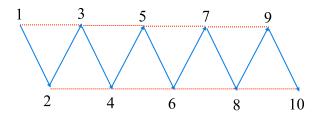


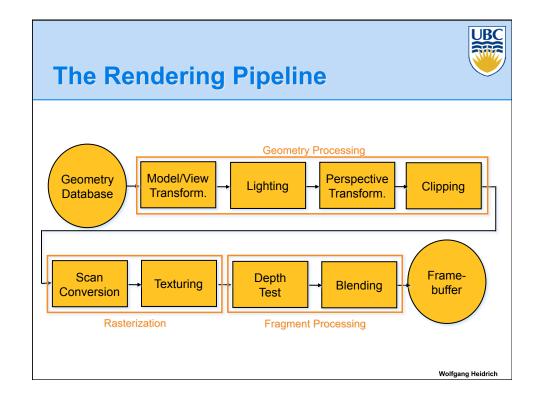


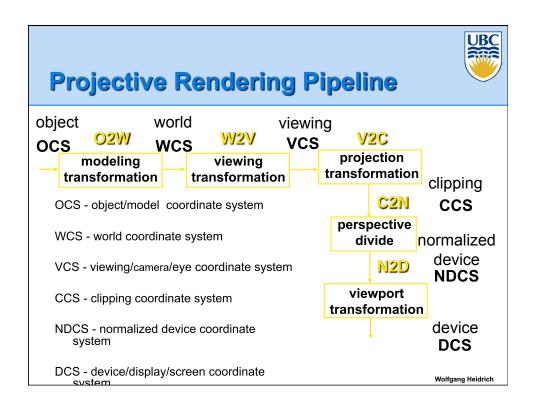
Triangle Strips

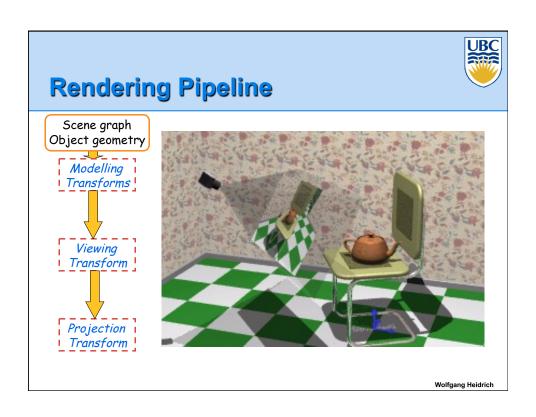
Orientation:

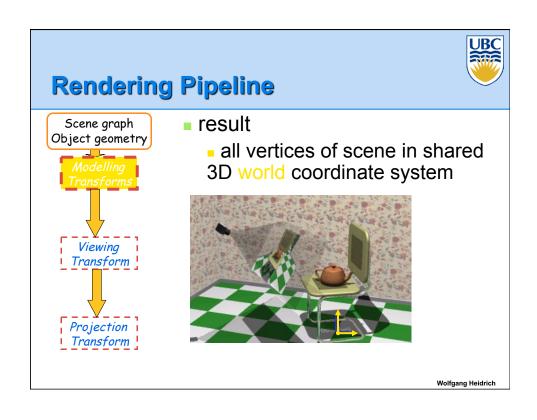
- Strip starts with a counter-clockwise triangle
- Then alternates between clockwise and counterclockwise

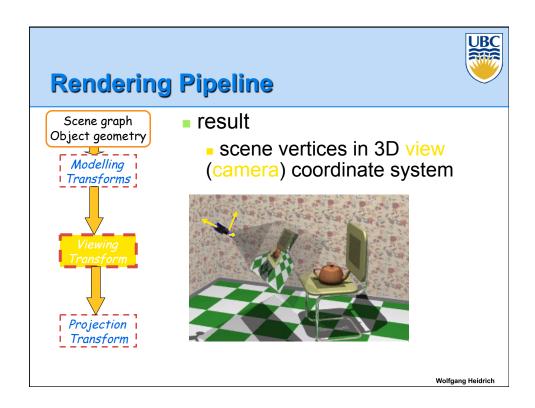






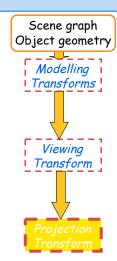








Rendering Pipeline



- result
 - 2D screen coordinates of clipped vertices



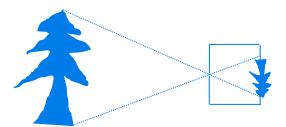
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Perspective Transformation



Pinhole Camera:

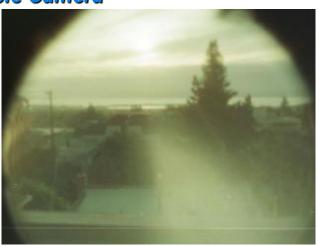
 Light shining through a tiny hole into a dark room yields upside-down image on wall





Perspective Transformation

Pinhole Camera



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Real Cameras



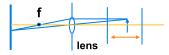
- pinhole camera has small aperture (lens opening)
 - hard to get enough light to expose the film

real pinhole camera



- lens permits larger apertures
- lens permits changing distance to film plane without actually moving the film plane

camera



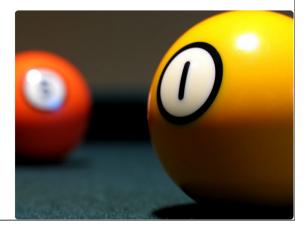
price to pay: limited depth of field

Real Cameras - Depth of Field



Limited depth of field

- Can be used to direct attention
- Artistic purposes



Perspective Transformation



In computer graphics:

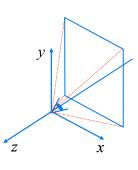
- Image plane is conceptually in front of the center of projection
- Perspective transformations belong to a class of operations that are called projective transformations
- Linear and affine transformations also belong to this class
- All projective transformations can be expressed as 4x4 matrix operations

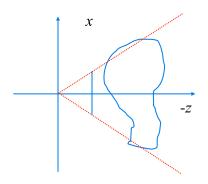


Perspective Projection

Synopsis:

 Project all geometry through a common center of projection (eye point) onto an image plane





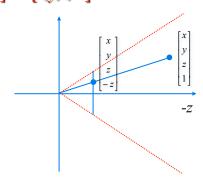
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Perspective Projection



Example:

- ullet Assume image plane at z=-1
- A point $[x,y,z,I]^T$ projects to $[-x/z,-y/z,-z/z,I]^T \equiv [x,y,z,-z]^T$





Perspective Projection

Analysis:

- This is a special case of a general family of transformations called <u>projective transformations</u>
- These can be expressed as 4x4 homogeneous matrices!
 - E.g. in the example:

$$T\begin{pmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{pmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix} \cdot \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \\ -z \end{bmatrix} \equiv \begin{bmatrix} -x/z \\ -y/z \\ -1 \\ 1 \end{bmatrix}$$

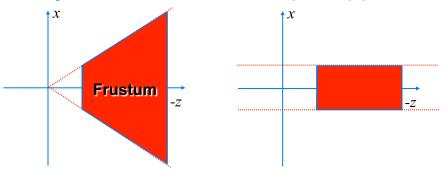
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Projective Transformations



Transformation of space:

- Center of projection moves to infinity
- Viewing frustum is transformed into a parallelpiped





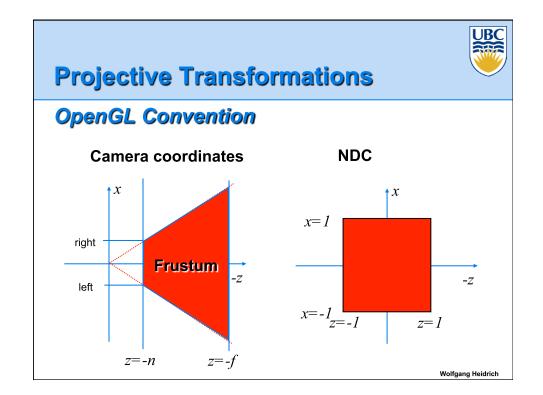
Projective Transformations

Convention:

- Viewing frustum is mapped to a specific parallelpiped
 - Normalized Device Coordinates (NDC)
- Only objects inside the parallelpiped get rendered
- Which parallelpied is used depends on the rendering system

OpenGL:

- Left and right image boundary are mapped to x=-1 and x=+1
- Top and bottom are mapped to y=-1 and y=+1
- Near and far plane are mapped to -1 and 1

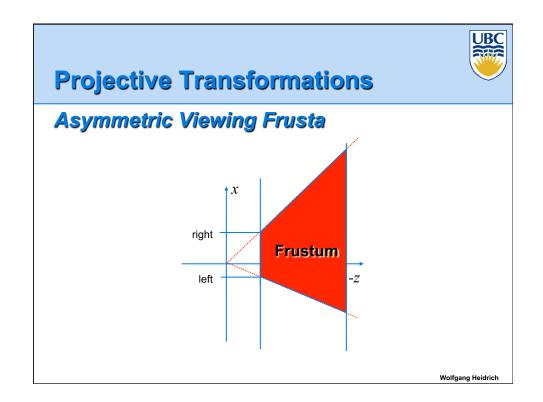




Projective Transformations

Why near and far plane?

- Near plane:
 - Avoid singularity (division by zero, or very small numbers)
- Far plane:
 - Store depth in fixed-point representation (integer), thus have to have fixed range of values (0...1)
 - Avoid/reduce numerical precision artifacts for distant objects

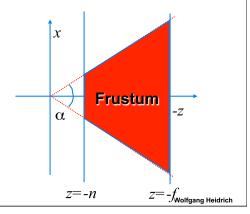




Projective Transformations

Alternative specification of symmetric frusta

- Field-of-view (fov) α
- Fov/2
- Field-of-view in y-direction (fovy) + aspect ratio



Demos



Tuebingen applets from Frank Hanisch

 http://www.gris.uni-tuebingen.de/edu/projects/grdev/doc/html/etc/ AppletIndex_en.html#Transform



Coming Up:

Wednesday:

More on perspective projection

Friday/Next Week

· Lighting/shading