



University of British Columbia
CPSC 314 Computer Graphics
Jan-Apr 2010

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Transformations IV

Week 3, Wed Jan 20

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010>

Assignments

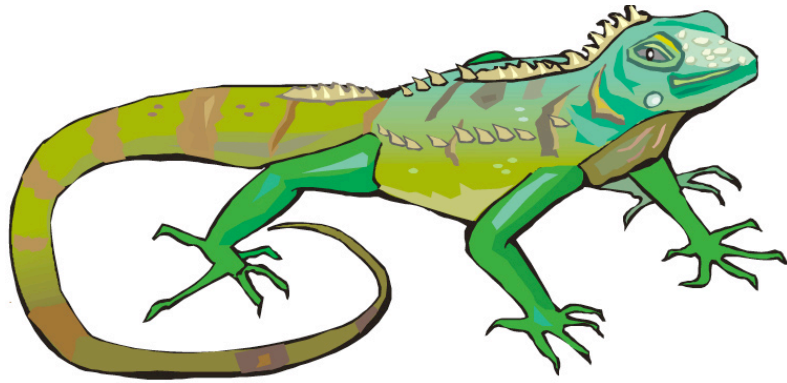
Correction: Assignments

- project 1
 - out today, due 5pm sharp Fri Jan 29
 - projects will go out before we've covered all the material
 - so you can think about it before diving in
 - template code gives you program shell and build tools
 - now out: separate packages for Linux, Mac, Windows
 - see <http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010/#assign>
 - p1_template_linux.tar.gz
 - p1_template_mac.tar.gz
 - p1_template_win.zip
- written homework 1
 - out today, due 5pm sharp **Fri Jan 29**
 - theoretical side of material

Demo

- animal out of boxes and matrices

Real Iguanas



<http://funkman.org/animal/reptile/iguana1.jpg>

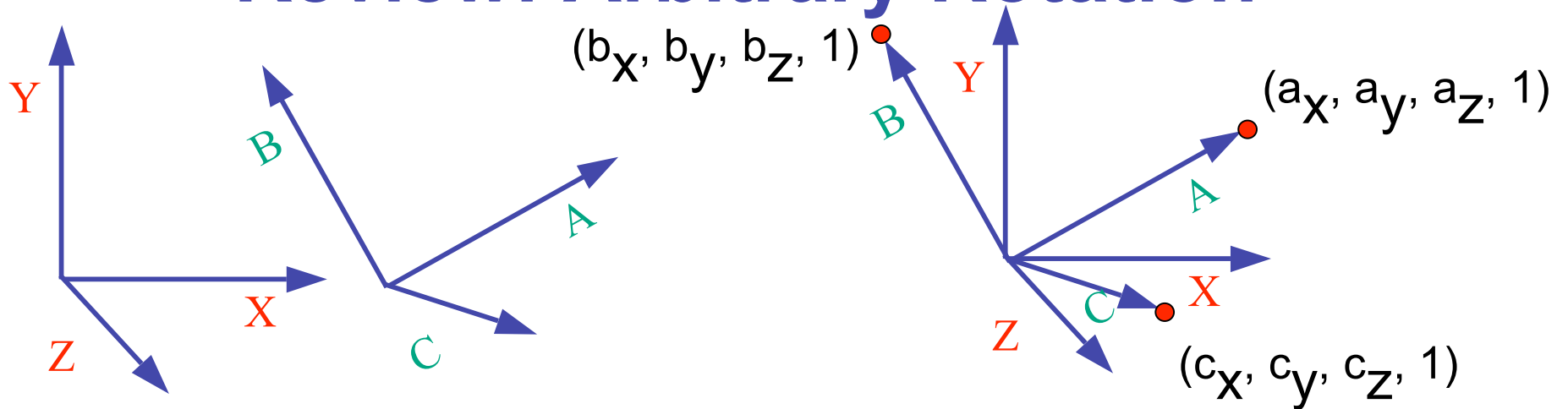


<http://www.mccullagh.org/db9/d30-3/iguana-closeup.jpg>



<http://www.naturephoto-cz.com/photos/sevcik/green-iguana--iguana-iguana-1.jpg>

Review: Arbitrary Rotation

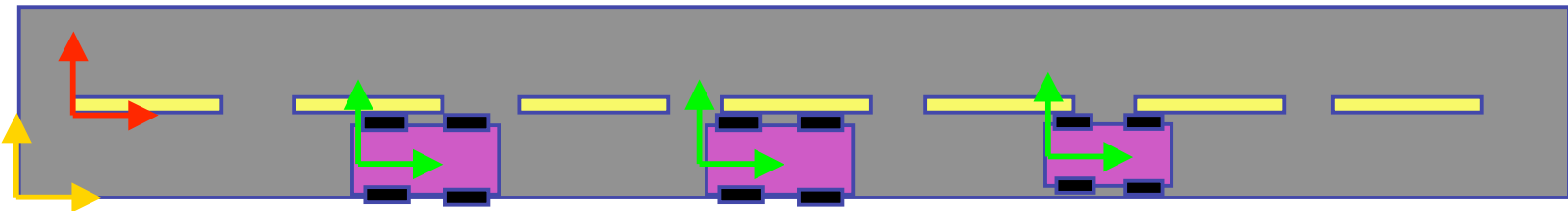


- arbitrary rotation: change of basis
 - given two **orthonormal** coordinate systems XYZ and ABC
 - A 's location in the XYZ coordinate system is $(a_x, a_y, a_z, 1), \dots$
- transformation from one to the other is matrix R whose **columns** are A, B, C :

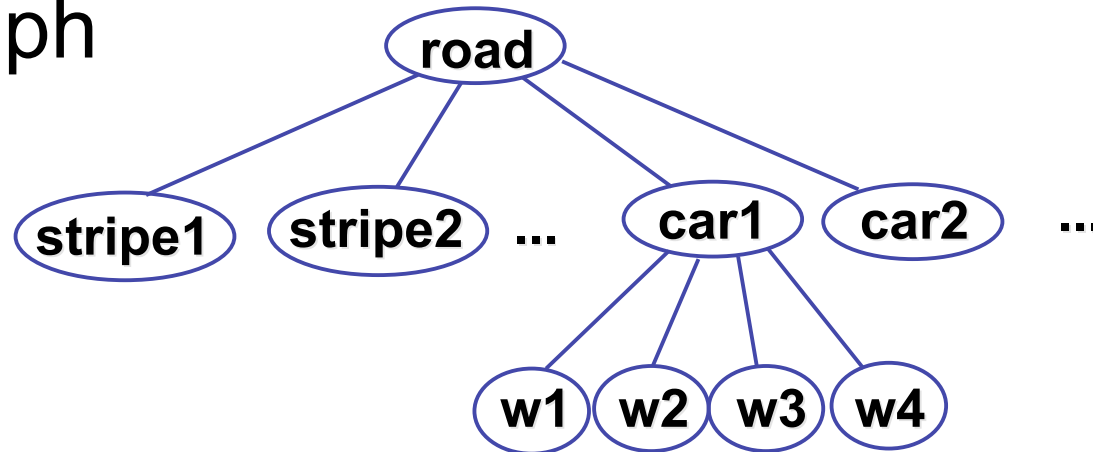
$$R(X) = \begin{bmatrix} a_x & b_x & c_x & 0 \\ a_y & b_y & c_y & 0 \\ a_z & b_z & c_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} = (a_x, a_y, a_z, 1) = A$$

Review: Transformation Hierarchies

- scene may have a hierarchy of coordinate systems
 - stores matrix at each level with incremental transform from parent's coordinate system

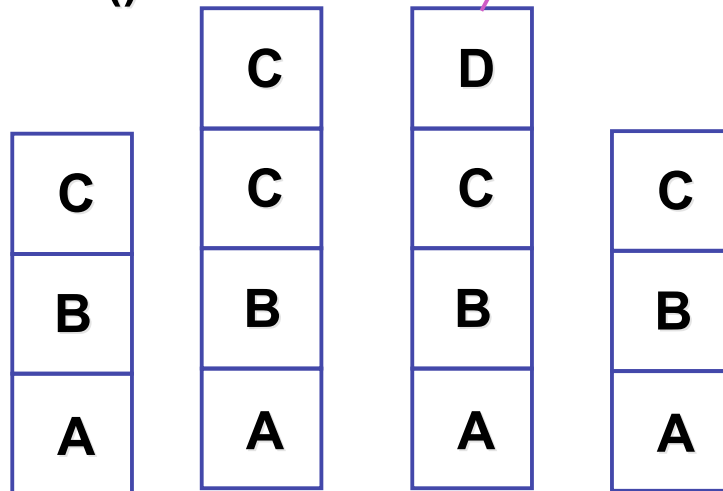


- scene graph



Review: Matrix Stacks

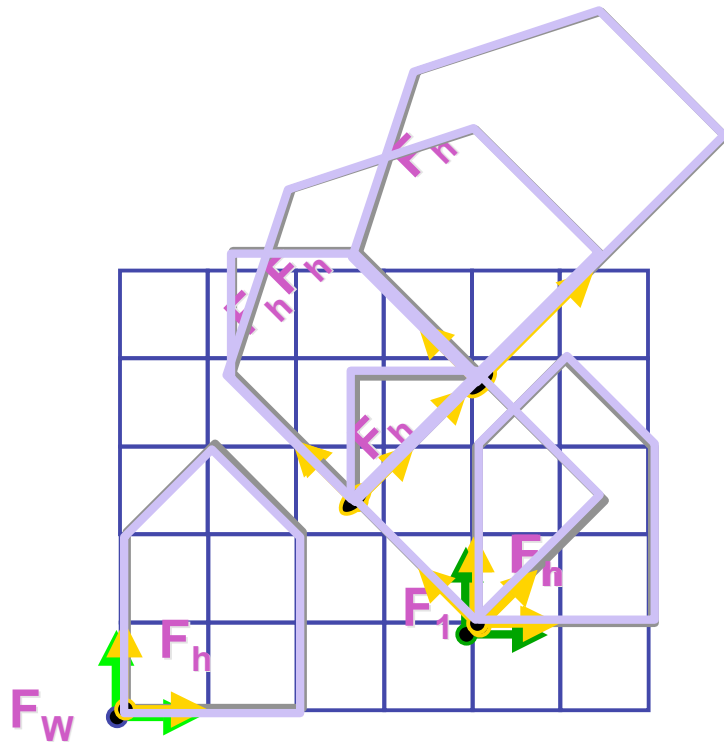
**glPushMatrix()
glPopMatrix()**



D = C scale(2,2,2) trans(1,0,0)

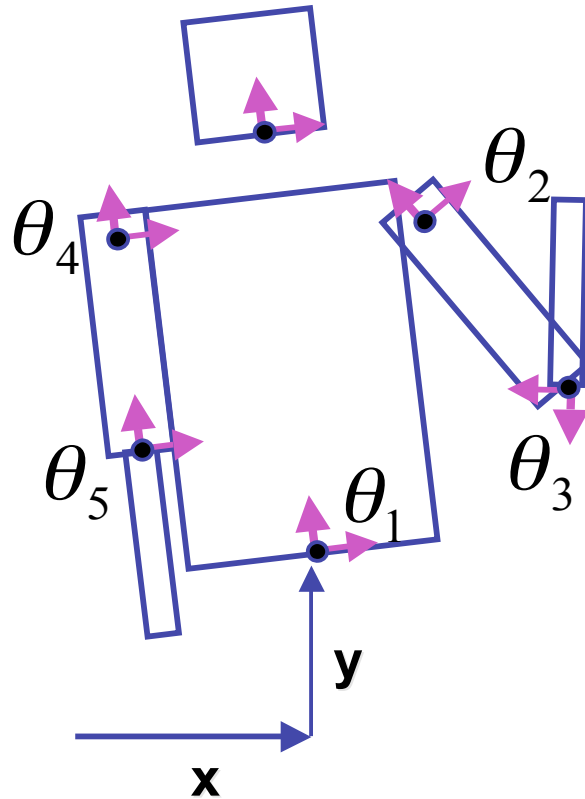
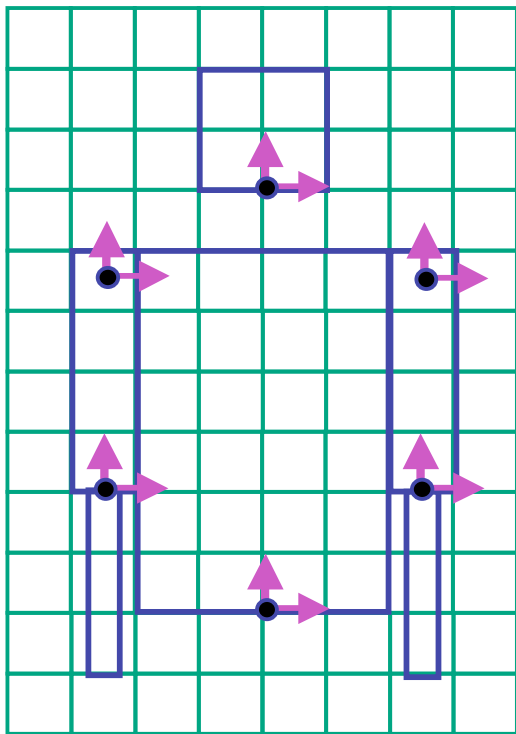
**DrawSquare()
glPushMatrix()
glScale3f(2,2,2)
glTranslate3f(1,0,0)
DrawSquare()
glPopMatrix()**

Transformation Hierarchy Example 3



```
glLoadIdentity();  
glTranslatef(4,1,0);  
glPushMatrix();  
glRotatef(45,0,0,1);  
glTranslatef(0,2,0);  
glScalef(2,1,1);  
glTranslate(1,0,0);  
glPopMatrix();
```

Transformation Hierarchy Example 4



```
glTranslate3f(x,y,0);  
glRotatef( $\theta_1$ ,0,0,1);  
DrawBody();  
glPushMatrix();  
    glTranslate3f(0,7,0);  
    DrawHead();  
glPopMatrix();  
glPushMatrix();  
    glTranslate(2.5,5.5,0);  
    glRotatef( $\theta_2$ ,0,0,1);  
    DrawUArm();  
    glTranslate(0,-3.5,0);  
    glRotatef( $\theta_3$ ,0,0,1);  
    DrawLArm();  
glPopMatrix();  
... (draw other arm)
```

Hierarchical Modelling

- advantages
 - define object once, instantiate multiple copies
 - transformation parameters often good control knobs
 - maintain structural constraints if well-designed
- limitations
 - expressivity: not always the best controls
 - can't do closed kinematic chains
 - keep hand on hip
 - can't do other constraints
 - collision detection
 - self-intersection
 - walk through walls

Display Lists

Display Lists

- precompile/cache block of OpenGL code for reuse
 - usually more efficient than **immediate mode**
 - exact optimizations depend on driver
 - good for multiple instances of same object
 - but cannot change contents, not parametrizable
 - good for static objects redrawn often
 - display lists persist across multiple frames
 - interactive graphics: objects redrawn every frame from new viewpoint from moving camera
 - can be nested hierarchically
- snowman example
 - <http://www.lighthouse3d.com/opengl/displaylists>

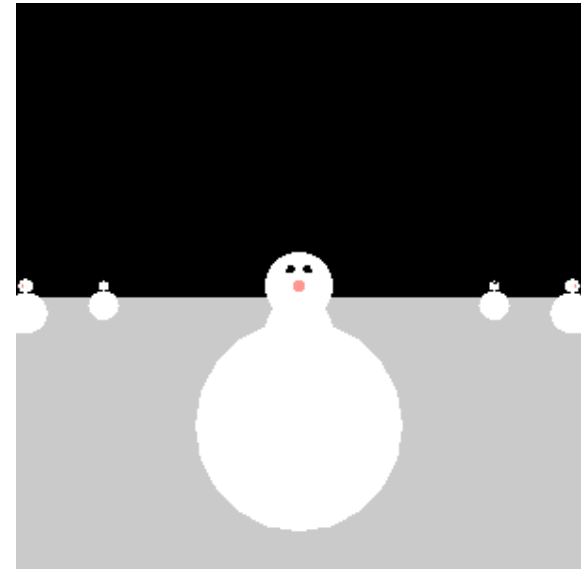
One Snowman



```
void drawSnowMan() {  
  
glColor3f(1.0f, 1.0f, 1.0f);  
  
// Draw Body  
glTranslatef(0.0f, 0.75f, 0.0f);  
glutSolidSphere(0.75f, 20, 20);  
  
// Draw Head  
glTranslatef(0.0f, 1.0f, 0.0f);  
glutSolidSphere(0.25f, 20, 20);  
  
// Draw Eyes  
glPushMatrix();  
glColor3f(0.0f, 0.0f, 0.0f);  
glTranslatef(0.05f, 0.10f, 0.18f);  
glutSolidSphere(0.05f, 10, 10);  
glTranslatef(-0.1f, 0.0f, 0.0f);  
glutSolidSphere(0.05f, 10, 10);  
glPopMatrix();  
  
// Draw Nose  
glColor3f(1.0f, 0.5f, 0.5f);  
glRotatef(0.0f, 1.0f, 0.0f, 0.0f);  
glutSolidCone(0.08f, 0.5f, 10, 2);  
}
```

Instantiate Many Snowmen

```
// Draw 36 Snowmen  
for(int i = -3; i < 3; i++)  
    for(int j=-3; j < 3; j++) {  
        glPushMatrix();  
        glTranslatef(i*10.0, 0, j * 10.0);  
        // Call the function to draw a snowman  
        drawSnowMan();  
        glPopMatrix();  
    }
```



36K polygons, 55 FPS

Making Display Lists

```
GLuint createDL() {  
    GLuint snowManDL;  
    // Create the id for the list  
    snowManDL = glGenLists(1);  
    glNewList(snowManDL, GL_COMPILE);  
    drawSnowMan();  
    glEndList();  
    return(snowManDL); }
```

```
snowmanDL = createDL();  
for(int i = -3; i < 3; i++)  
    for(int j=-3; j < 3; j++) {  
        glPushMatrix();  
        glTranslatef(i*10.0, 0, j * 10.0);  
        glCallList(Dlid);  
        glPopMatrix(); }
```

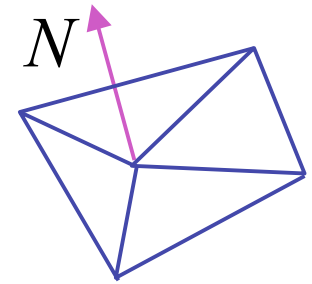
36K polygons, 153 FPS 16

Transforming Normals

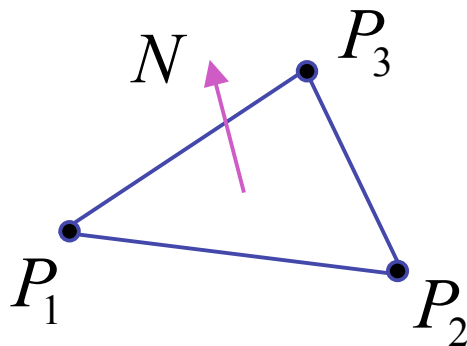
Transforming Geometric Objects

- lines, polygons made up of vertices
 - transform the vertices
 - interpolate between
- does this work for everything? no!
 - normals are trickier

Computing Normals



- normal
 - direction specifying orientation of polygon
 - $w=0$ means direction with homogeneous coords
 - vs. $w=1$ for points/vectors of object vertices
 - used for lighting
 - must be normalized to unit length
 - can compute if not supplied with object



$$N = (P_2 - P_1) \times (P_3 - P_1)$$

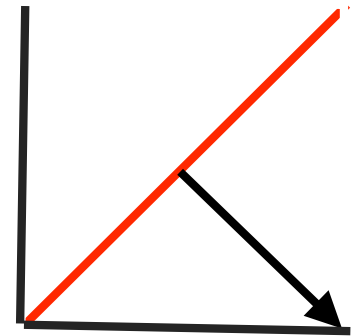
Transforming Normals

$$\begin{bmatrix} x' \\ y' \\ z' \\ 0 \end{bmatrix} = \begin{bmatrix} m_{11} & m_{12} & m_{13} & T_x \\ m_{21} & m_{22} & m_{23} & T_y \\ m_{31} & m_{32} & m_{33} & T_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 0 \end{bmatrix}$$

- so if points transformed by matrix **M**, can we just transform normal vector by **M** too?
 - translations OK: $w=0$ means unaffected
 - rotations OK
 - uniform scaling OK
- these all maintain direction

Transforming Normals

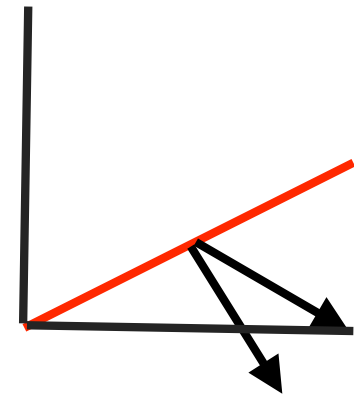
- nonuniform scaling does not work
- $x-y=0$ plane
 - line $x=y$
 - normal: $[1,-1,0]$
 - direction of line $x=-y$
 - (ignore normalization for now)



Transforming Normals

- apply nonuniform scale: stretch along x by 2
 - new plane $x = 2y$
- transformed normal: $[2, -1, 0]$

$$\begin{bmatrix} 2 \\ -1 \\ 0 \\ 0 \end{bmatrix} = \begin{bmatrix} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -1 \\ 0 \\ 0 \end{bmatrix}$$



- normal is direction of line $x = -2y$ or $x+2y=0$
- not perpendicular to plane!
- should be direction of $2x = -y$

Planes and Normals

- plane is all points perpendicular to normal
 - $N \bullet P = 0$ (with dot product)
 - $N^T \bullet P = 0$ (matrix multiply requires transpose)

$$N = \begin{bmatrix} a \\ b \\ c \\ d \end{bmatrix}, P = \begin{bmatrix} x \\ y \\ z \\ w \end{bmatrix}$$

- explicit form: plane = $ax + by + cz + d$

Finding Correct Normal Transform

- transform a plane

$$\begin{matrix} P \\ N \end{matrix} \longrightarrow \begin{matrix} P' = MP \\ N' = QN \end{matrix}$$

given M,
what should Q be?

$$N'^T P' = 0$$

stay perpendicular

$$(QN)^T (MP) = 0$$

substitute from above

$$N^T \underbrace{Q^T M}_{MP} P = 0$$

$$(AB)^T = B^T A^T$$

$$Q^T M = I$$

$$N^T P = 0 \text{ if } Q^T M = I$$

$$\mathbf{Q} = \left(\mathbf{M}^{-1}\right)^T$$

thus the normal to any surface can be transformed by the inverse transpose of the modelling transformation