



University of British Columbia
CPSC 314 Computer Graphics
Jan-Apr 2010

Tamara Munzner

Transformations III

Week 3, Mon Jan 18

<http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010>

News

- CS dept announcements
- Undergraduate Summer Research Award (USRA)
 - applications due Feb 26
 - see Guiliana for more details

Department of Computer Science
Undergraduate Events

Events this week

Drop-in Resume/Cover Letter Editing

Date: Tues., Jan 19
Time: 12:30 – 2 pm
Location: Rm 255, ICICS/CS Bldg.

Interview Skills Workshop

Date: Thurs., Jan 21
Time: 12:30 – 2 pm
Location: DMP 201
Registration: Email dianejoh@cs.ubc.ca

Project Management Workshop

Speaker: David Hunter (ex-VP, SAP)
Date: Thurs., Jan 21
Time: 5:30 – 7 pm
Location: DMP 110

CSSS Laser Tag

Date: Sun., Jan 24
Time: 7 – 9 pm
Location: Planet Laser
@ 100 Braid St., New
Westminster

Event next week

Public Speaking 11

Date: Mon., Jan 25
Time: 5 – 6 pm
Location: DMP 101

Assignments

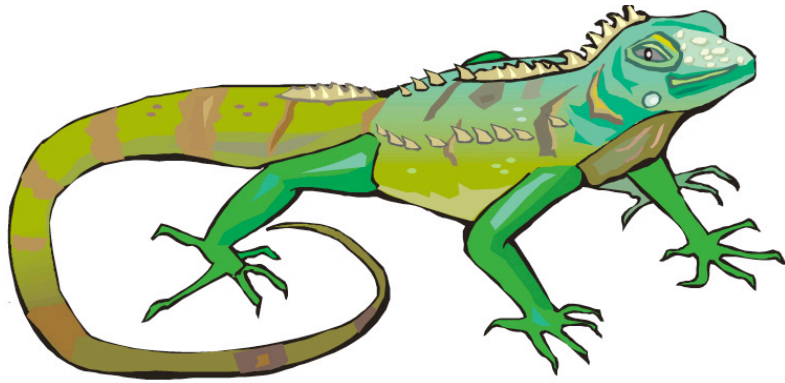
Assignments

- project 1
 - out today, due 5pm sharp Fri Jan 29
 - projects will go out before we've covered all the material
 - so you can think about it before diving in
 - build iguana out of cubes and 4x4 matrices
 - think cartoon, not beauty
 - template code gives you program shell, Makefile
 - <http://www.ugrad.cs.ubc.ca/~cs314/Vjan2010/p1.tar.gz>
- written homework 1
 - out today, due 5pm sharp Wed Feb 6
 - theoretical side of material

Demo

- animal out of boxes and matrices

Real Iguanas



<http://funkman.org/animal/reptile/iguana1.jpg>

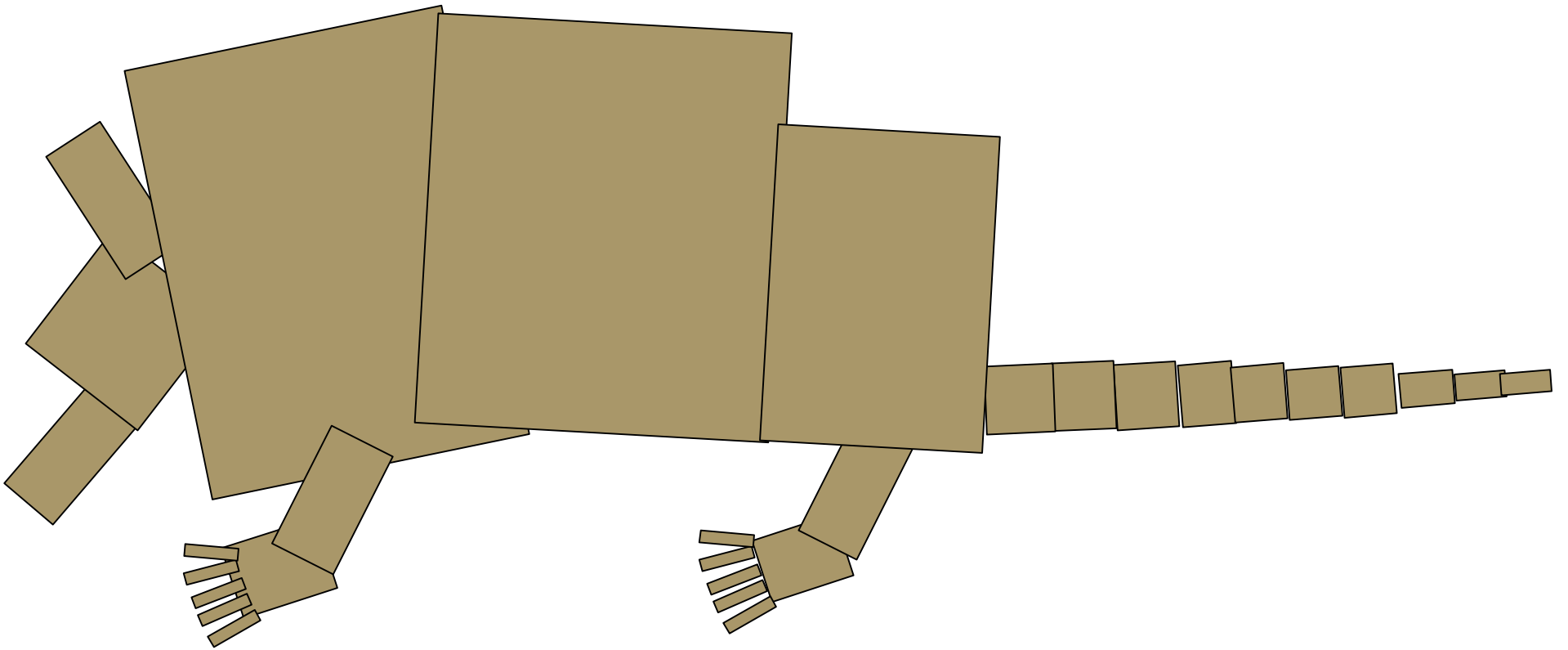


<http://www.mccullagh.org/db9/d30-3/iguana-closeup.jpg>

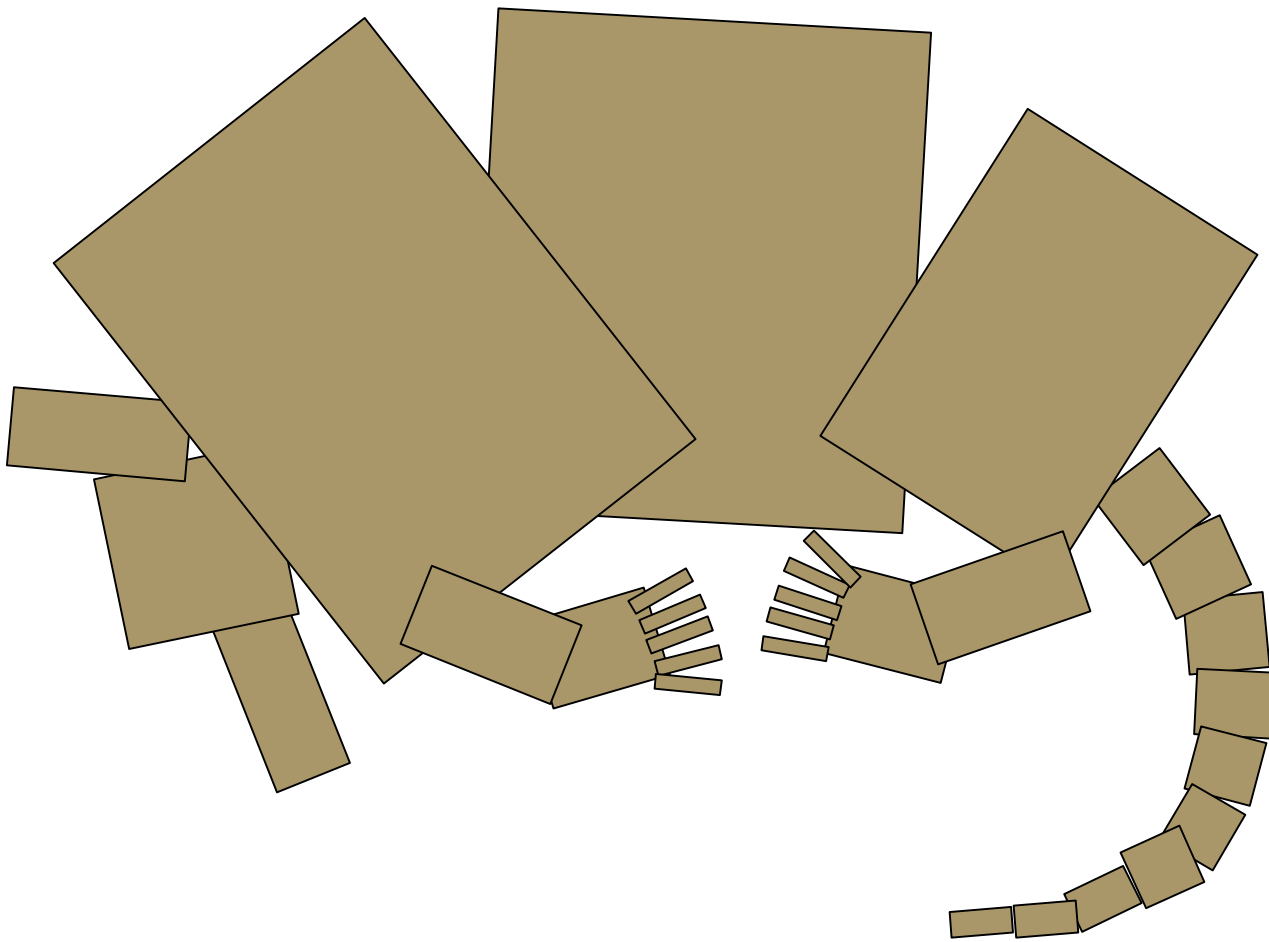


<http://www.naturephoto-cz.com/photos/sevcik/green-iguana--iguana-iguana-1.jpg>

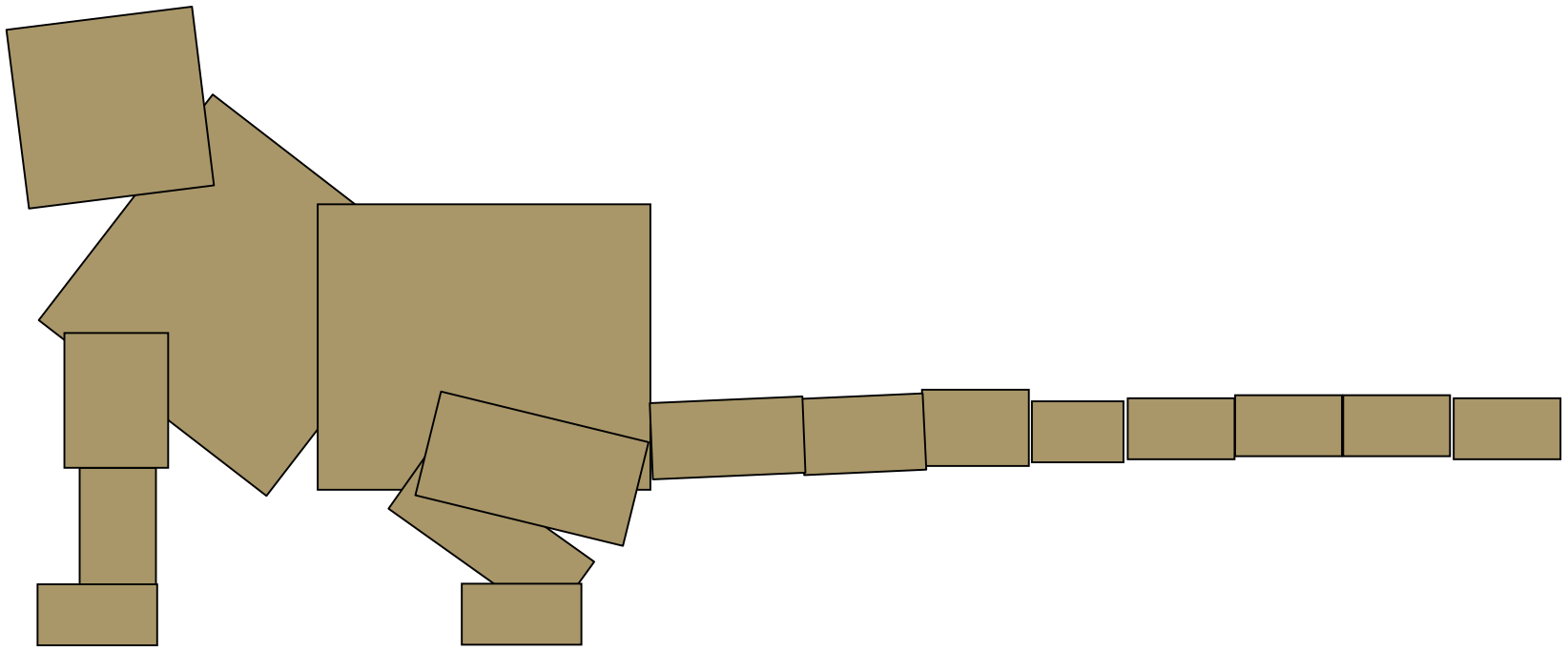
Armadillos!



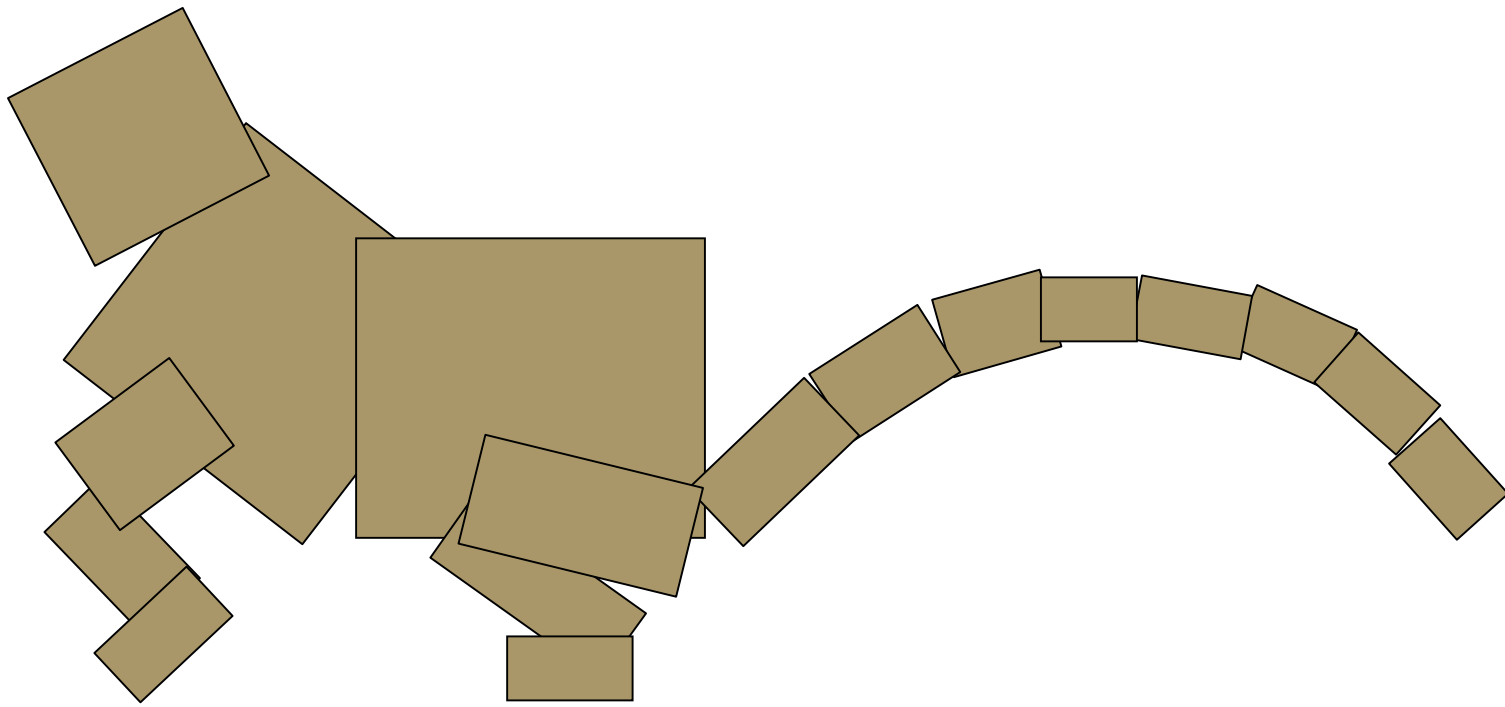
Armadillos!



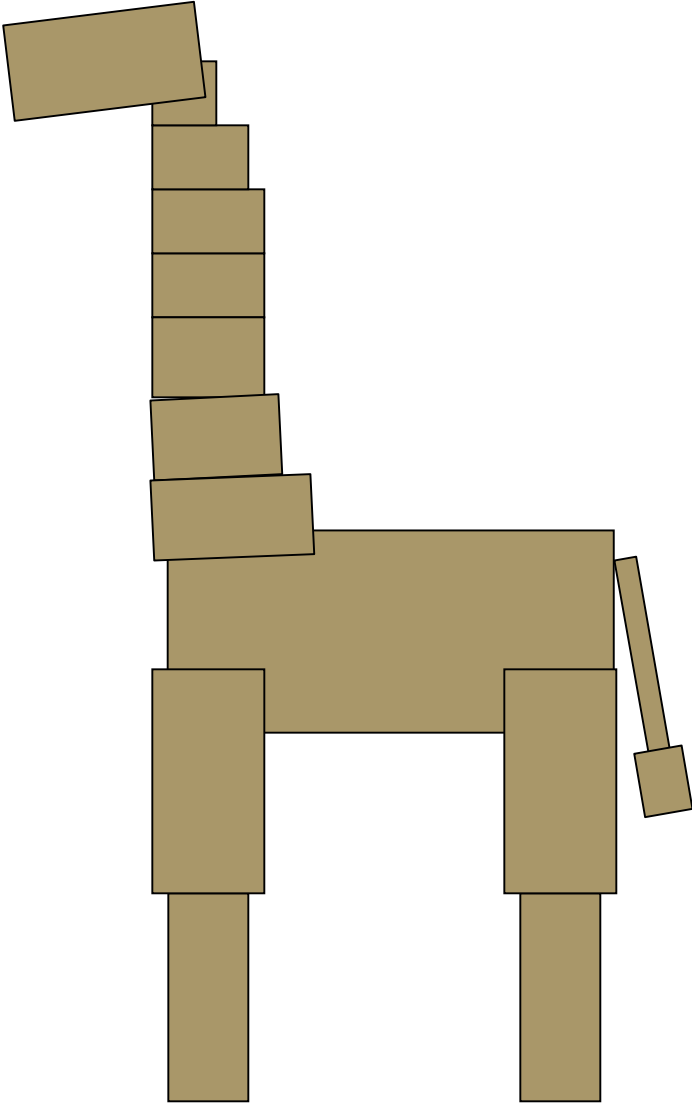
Monkeys!



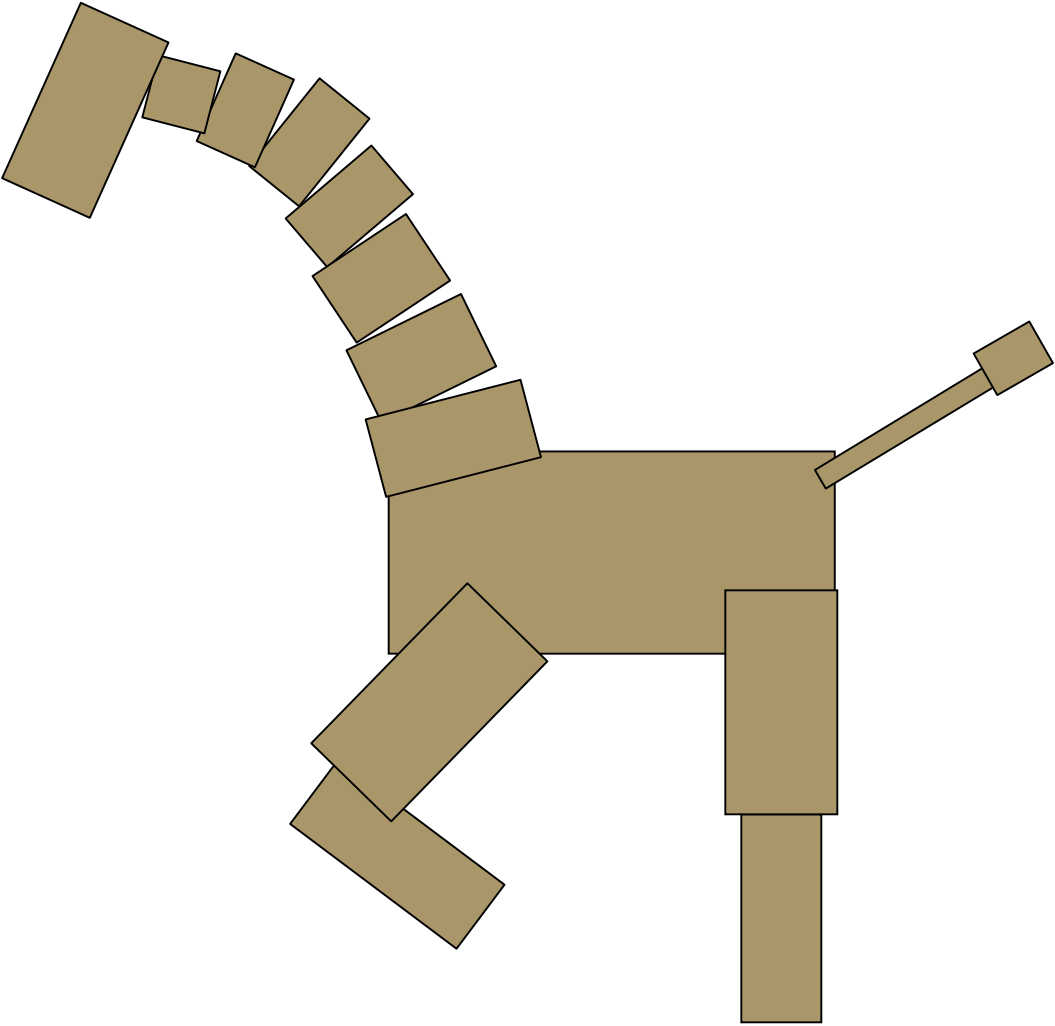
Monkeys!



Giraffes!



Giraffes!



Project 1 Advice

- do **not** model everything first and only then worry about animating
- interleave modelling, animation
 - for each body part: add it, then jumpcut animate, then smooth animate
 - discover if on wrong track sooner
 - dependencies: can't get anim credit if no model
 - use body as scene graph root
- check from all camera angles

Project 1 Advice

- finish all required parts before
 - going for extra credit
 - playing with lighting or viewing
- ok to use `glRotate`, `glTranslate`, `glScale`
- ok to use `glutSolidCube`, or build your own
 - where to put origin? your choice
 - center of object, range - .5 to +.5
 - corner of object, range 0 to 1

Project 1 Advice

- visual debugging
 - color cube faces differently
 - colored lines sticking out of glutSolidCube faces
 - make your cubes wireframe to see inside
- thinking about transformations
 - move physical objects around
 - play with demos
 - Brown scenegraph applets

Project 1 Advice

- smooth transition
 - change happens gradually over X frames
 - key click triggers animation
 - one way: redraw happens X times
 - linear interpolation:
each time, $\text{param} += (\text{new-old})/30$
 - or redraw happens over X seconds
 - even better, but not required

Project 1 Advice

- transitions
 - safe to linearly interpolate parameters for `glRotate/glTranslate/glScale`
 - do **not** interpolate individual elements of 4x4 matrix!

Style

- you can lose up to 15% for poor style
- most critical: reasonable structure
 - yes: parametrized functions
 - no: cut-and-paste with slight changes
- reasonable names (variables, functions)
- adequate commenting
 - rule of thumb: what if you had to fix a bug two years from now?
- global variables are indeed acceptable

Version Control

- bad idea: just keep changing same file
- save off versions often
 - after got one thing to work, before you try starting something else
 - just before you do something drastic
- how?
 - not good: commenting out big blocks of code
 - a little better: save off file under new name
 - p1.almostworks.cpp, p1.fixedbug.cpp
- much better: use version control software
 - strongly recommended

Version Control Software

- easy to browse previous work
- easy to revert if needed
- for maximum benefit, use meaningful comments to describe what you did
 - “started on tail”, “fixed head breakoff bug”, “leg code compiles but doesn’t run”
- useful when you’re working alone
- critical when you’re working together
- many choices: RCS, CVS, svn/subversion
 - all are installed on lab machines
 - svn tutorial is part of next week’s lab

Graphical File Comparison

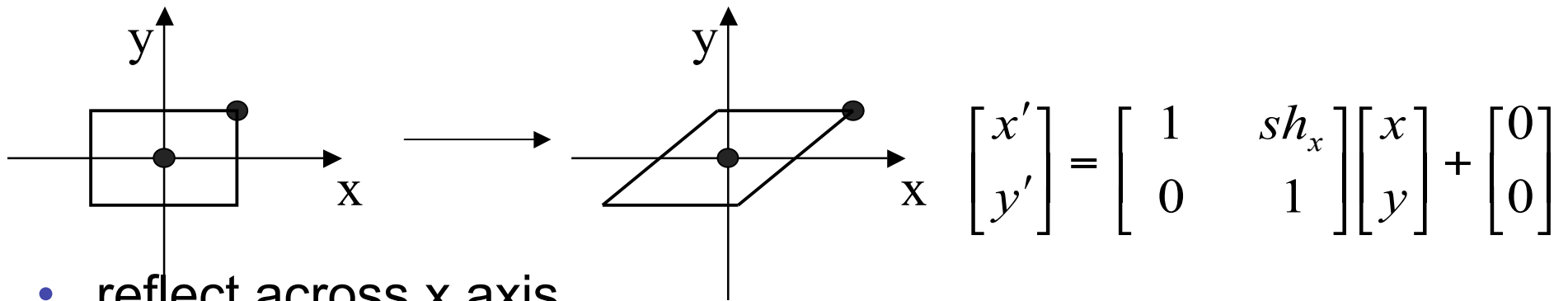
- installed on lab machines
 - xfdiff4 (side by side comparison)
 - xwdiff (in-place, with crossouts)
- Windows: windiff
 - <http://keithdevens.com/files/windiff>
- Macs: FileMerge
 - in /Developer/Applications/Utilities

Readings for Transformations I-IV

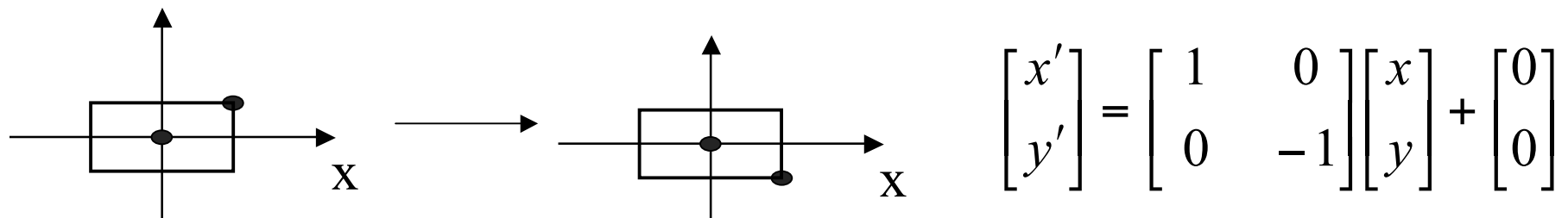
- FCG Chap 6 Transformation Matrices
 - *except* 6.1.6, 6.3.1
- FCG Sect 13.3 Scene Graphs
- RB Chap Viewing
 - Viewing and Modeling Transforms *until* Viewing Transformations
 - Examples of Composing Several Transformations *through* Building an Articulated Robot Arm
- RB Appendix Homogeneous Coordinates and Transformation Matrices
 - *until* Perspective Projection
- RB Chap Display Lists

Review: Shear, Reflection

- shear along x axis
 - push points to right in proportion to height



- reflect across x axis
 - mirror



Review: 2D Transformations

matrix multiplication

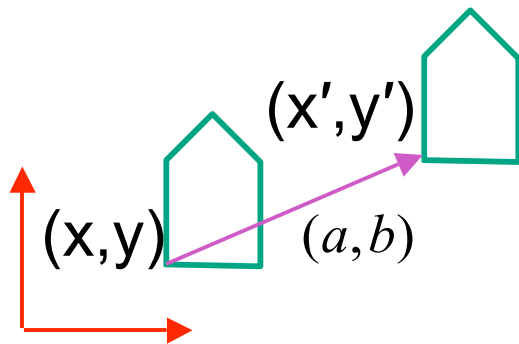
$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} a & 0 \\ 0 & b \end{bmatrix}} \begin{bmatrix} x \\ y \end{bmatrix}$$

scaling matrix

matrix multiplication

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \underbrace{\begin{bmatrix} \cos(\theta) & -\sin(\theta) \\ \sin(\theta) & \cos(\theta) \end{bmatrix}} \begin{bmatrix} x \\ y \end{bmatrix}$$

rotation matrix



vector addition

$$\begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} a \\ b \end{bmatrix} = \begin{bmatrix} x + a \\ y + b \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

$$\underbrace{\begin{bmatrix} a & b \\ c & d \end{bmatrix}} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x' \\ y' \end{bmatrix}$$

translation multiplication matrix??

Review: Linear Transformations

- linear transformations are combinations of

- shear

- scale

- rotate

- reflect

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$x' = ax + by$$

$$y' = cx + dy$$

- properties of linear transformations

- satisfies $T(s\mathbf{x} + t\mathbf{y}) = sT(\mathbf{x}) + tT(\mathbf{y})$

- origin maps to origin

- lines map to lines

- parallel lines remain parallel

- ratios are preserved

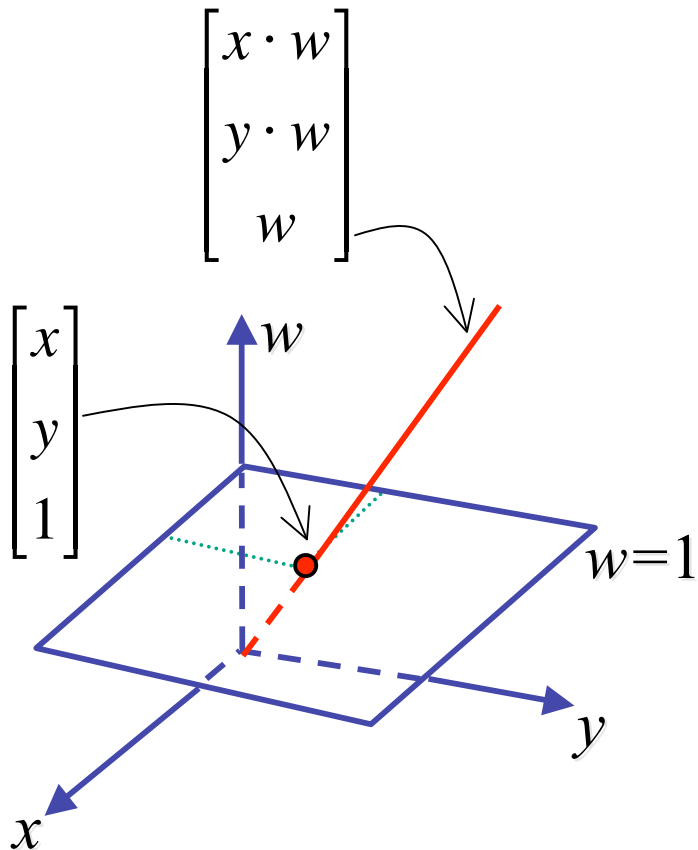
- closed under composition

Review: Homogeneous Coordinates

homogeneous

cartesian

$$(x, y, w) \xrightarrow{/w} \left(\frac{x}{w}, \frac{y}{w} \right)$$



- point in 2D cartesian + weight w = point P in 3D homog. coords
 - multiples of (x,y,w) form 3D line L
 - all homogeneous points on L represent same 2D cartesian point
- **homogenize** to convert homog. 3D point to cartesian 2D point:
 - divide by w to get $(x/w, y/w, 1)$
 - projects line to point onto $w=1$ plane
 - like normalizing, one dimension up²⁷

Review: Homogeneous Coordinates

- 2D transformation matrices are now 3x3:

$$\mathbf{Rotation} = \begin{bmatrix} \cos(\theta) & -\sin(\theta) & 0 \\ \sin(\theta) & \cos(\theta) & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \mathbf{Scale} = \begin{bmatrix} a & 0 & 0 \\ 0 & b & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{Translation} = \begin{bmatrix} 1 & 0 & T_x \\ 0 & 1 & T_y \\ 0 & 0 & 1 \end{bmatrix} \quad \text{use rightmost column!}$$

$$\begin{bmatrix} 1 & 0 & a \\ 0 & 1 & b \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} = \begin{bmatrix} x*1 + a*1 \\ y*1 + b*1 \\ 1 \end{bmatrix} = \begin{bmatrix} x + a \\ y + b \\ 1 \end{bmatrix}$$

Review: Affine Transformations

- affine transforms are combinations of

- linear transformations
- translations

$$\begin{bmatrix} x' \\ y' \\ w \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

- properties of affine transformations

- origin does not necessarily map to origin
- lines map to lines
- parallel lines remain parallel
- ratios are preserved
- closed under composition

Review: 3D Transformations

$$\text{shear}(hxy, hxz, hyx, hyz, hzx, hzy) \begin{bmatrix} 1 & hxy & hxz & 0 \\ hxy & 1 & hzy & 0 \\ hxz & hzy & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

translate(a,b,c)

scale(a,b,c)

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & & & a \\ & 1 & & b \\ & & 1 & c \\ & & & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} a & & & \\ & b & & \\ & & c & \\ & & & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Rotate(x, θ)

Rotate(y, θ)

Rotate(z, θ)

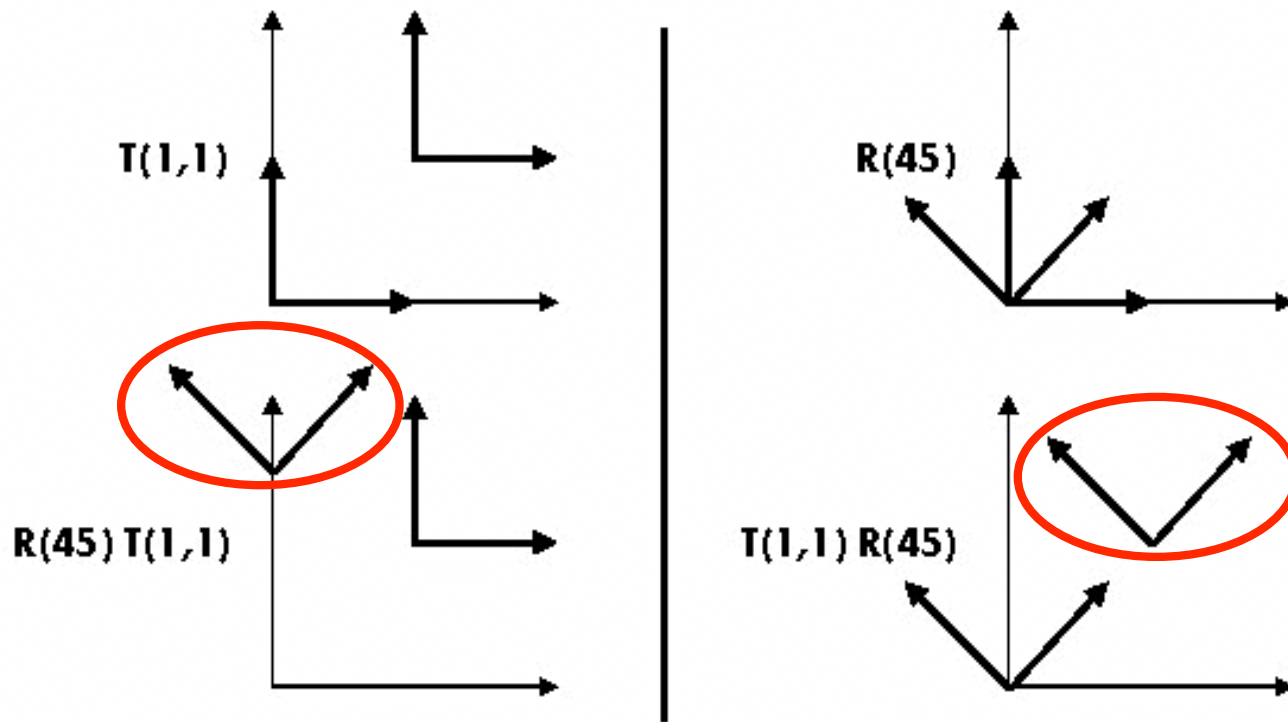
$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & & & \\ & \cos \theta & -\sin \theta & \\ & \sin \theta & \cos \theta & \\ & & & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos \theta & & & \\ & 1 & & \\ -\sin \theta & & \cos \theta & \\ & & & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} \cos \theta & -\sin \theta & & \\ \sin \theta & \cos \theta & & \\ & & 1 & \\ & & & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Review: Composing Transformations

ORDER MATTERS!



$T_a T_b = T_b T_a$, but $R_a R_b \neq R_b R_a$ and $T_a R_b \neq R_b T_a$

- translations commute
- rotations around same axis commute
- rotations around different axes do not commute
- rotations and translations do not commute


Review: Composing Transformations

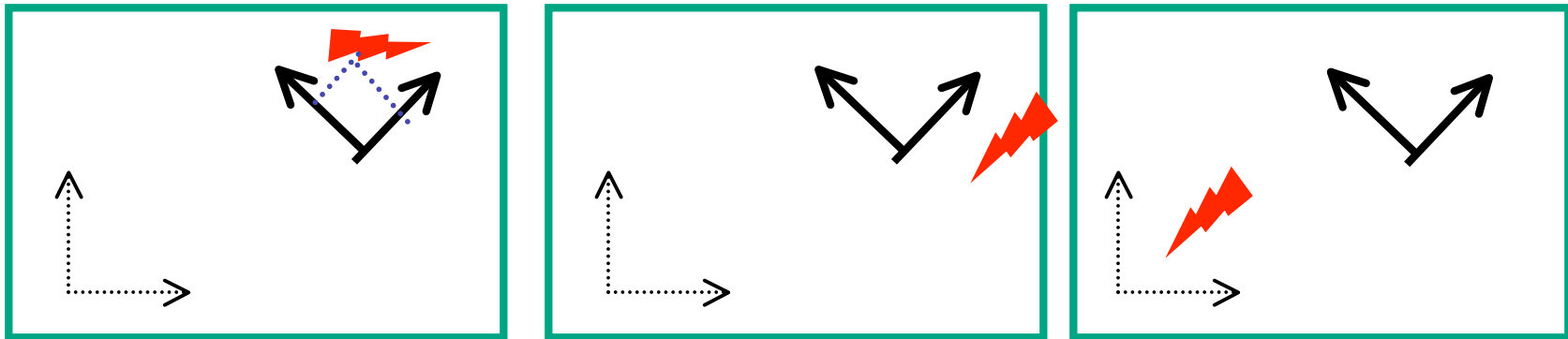
$$\mathbf{p}' = \mathbf{TRp}$$

- which direction to read?
 - right to left
 - interpret operations wrt fixed coordinates
 - **moving object**
 - left to right **OpenGL pipeline ordering!**
 - interpret operations wrt local coordinates
 - **changing coordinate system**
 - OpenGL updates current matrix with postmultiply
 - `glTranslatef(2,3,0);`
 - `glRotatef(-90,0,0,1);`
 - `glVertexf(1,1,1);`
 - specify vector last, in final coordinate system
 - first matrix to affect it is specified second-to-last

More: Composing Transformations


$$\mathbf{p}' = \mathbf{TRp}$$

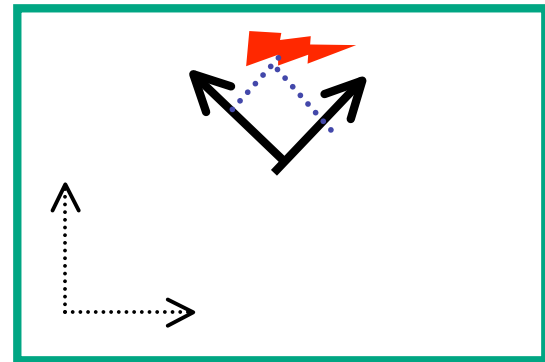
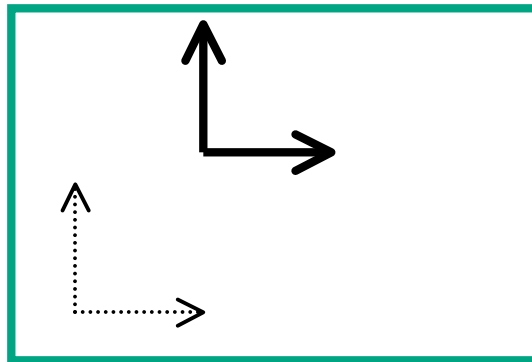
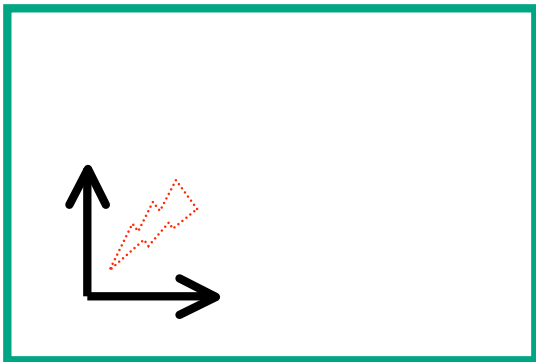
- which direction to read?
 - right to left 
 - interpret operations wrt fixed coordinates
 - **moving object**
 - draw thing
 - rotate thing by -90 degrees wrt origin
 - translate it (-2, -3) over



More: Composing Transformations

$$\mathbf{p}' = \mathbf{TRp}$$

- which direction to read?
 - left to right 
 - interpret operations wrt local coordinates
 - **changing coordinate system**
 - translate coordinate system (2, 3) over
 - rotate coordinate system 90 degrees wrt origin
 - draw object in current coordinate system
 - in OpenGL, cannot move object once it is drawn!!



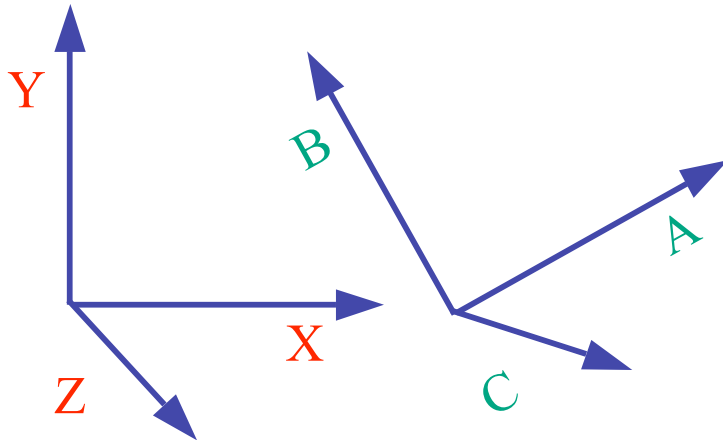
General Transform Composition

- transformation of geometry into coordinate system where operation becomes simpler
 - typically translate to origin
- perform operation
- transform geometry back to original coordinate system

Rotation About an Arbitrary Axis

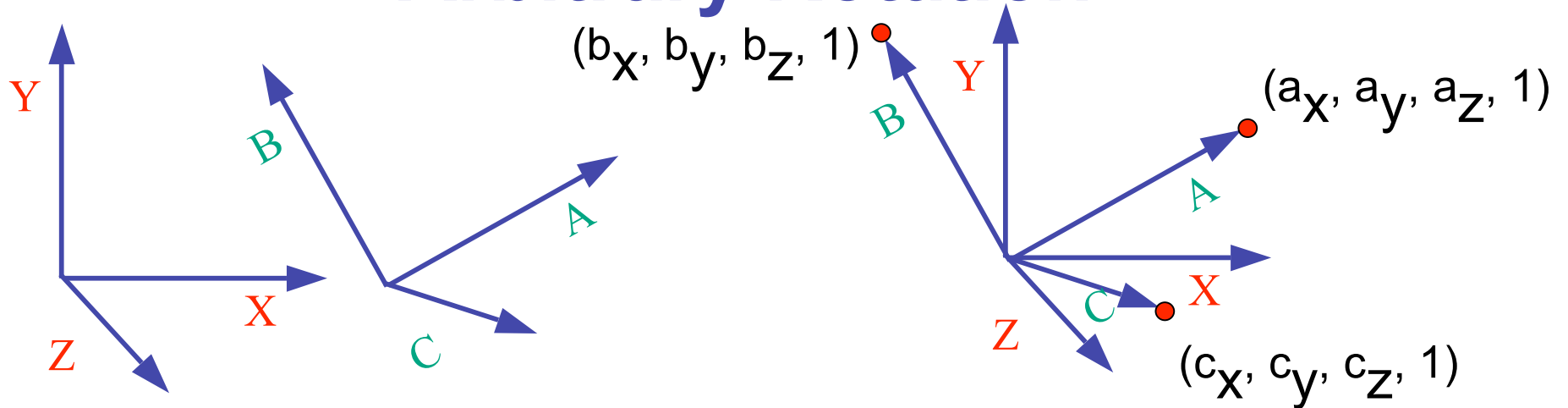
- axis defined by two points
- translate point to the origin
- rotate to align axis with z-axis (or x or y)
- perform rotation
- undo aligning rotations
- undo translation

Arbitrary Rotation



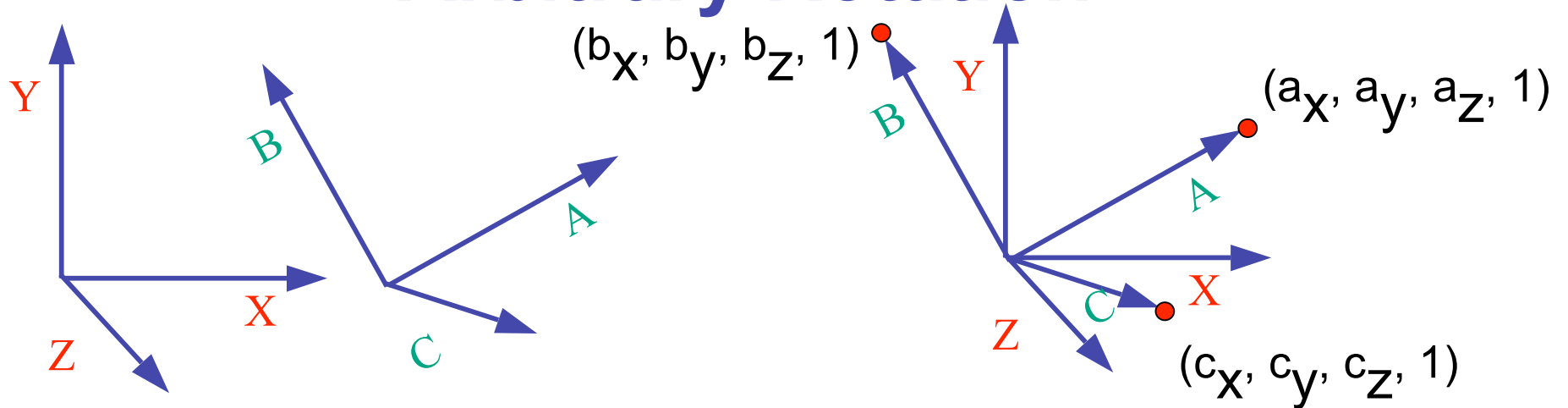
- arbitrary rotation: change of basis
 - given two **orthonormal** coordinate systems *XYZ* and *ABC*
 - *A*'s location in the XYZ coordinate system is $(a_x, a_y, a_z, 1), \dots$

Arbitrary Rotation



- arbitrary rotation: change of basis
 - given two **orthonormal** coordinate systems XYZ and ABC
 - A 's location in the XYZ coordinate system is $(a_x, a_y, a_z, 1)$, ...

Arbitrary Rotation



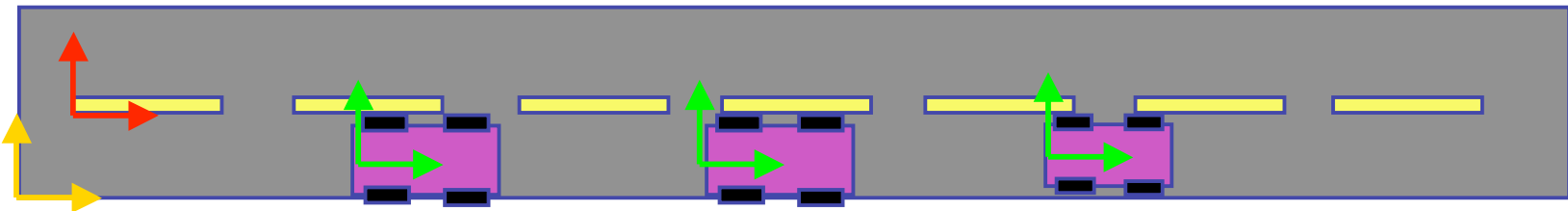
- arbitrary rotation: change of basis
 - given two **orthonormal** coordinate systems XYZ and ABC
 - A 's location in the XYZ coordinate system is $(a_x, a_y, a_z, 1), \dots$
- transformation from one to the other is matrix R whose **columns** are A, B, C :

$$R(X) = \begin{bmatrix} a_x & b_x & c_x & 0 \\ a_y & b_y & c_y & 0 \\ a_z & b_z & c_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 1 \end{bmatrix} = (a_x, a_y, a_z, 1) = A$$

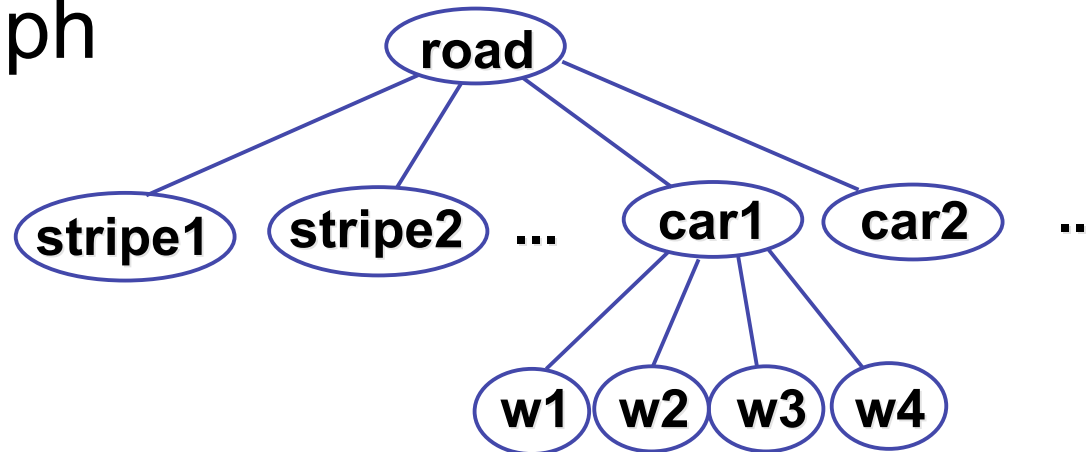
Transformation Hierarchies

Transformation Hierarchies

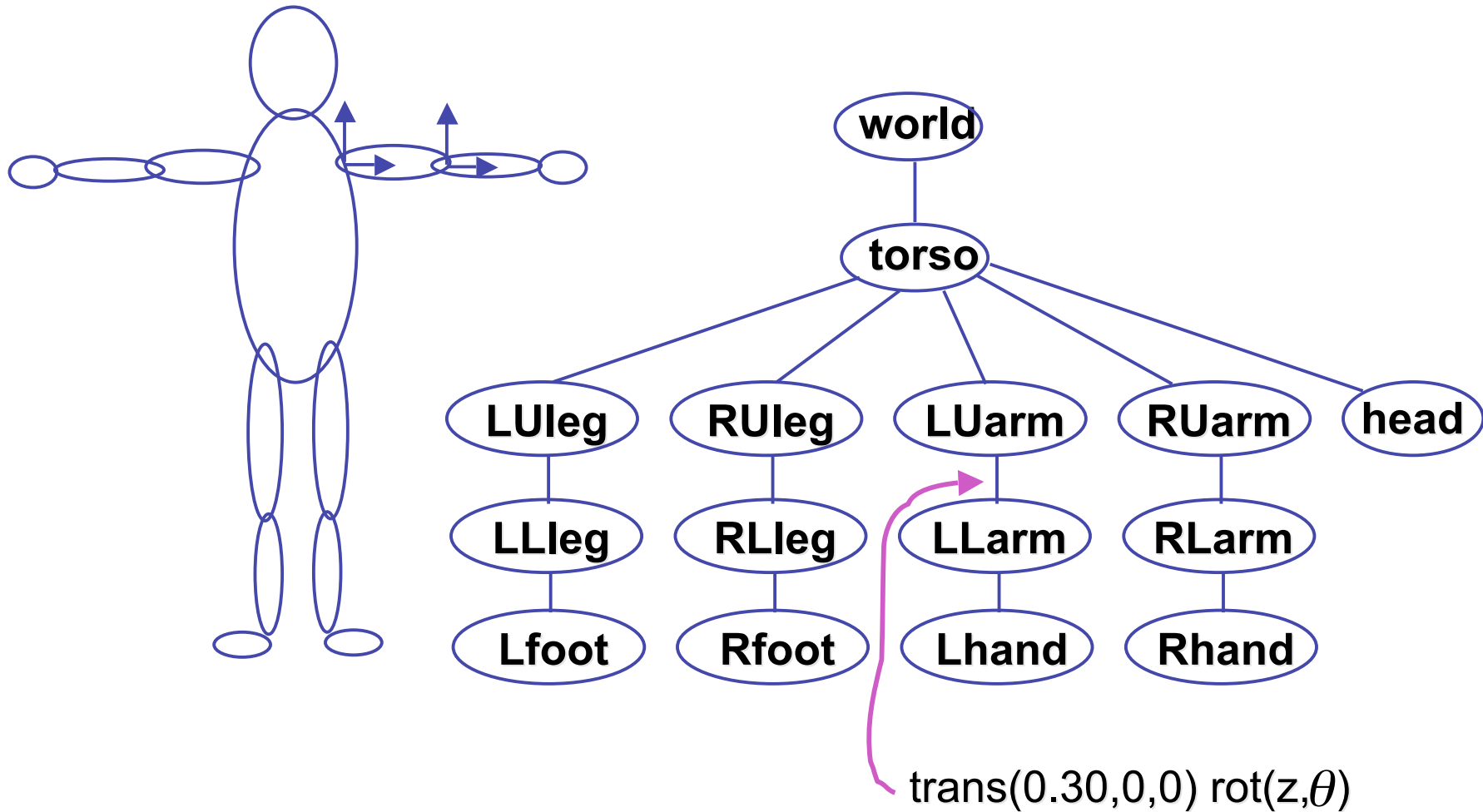
- scene may have a hierarchy of coordinate systems
 - stores matrix at each level with incremental transform from parent's coordinate system



- scene graph

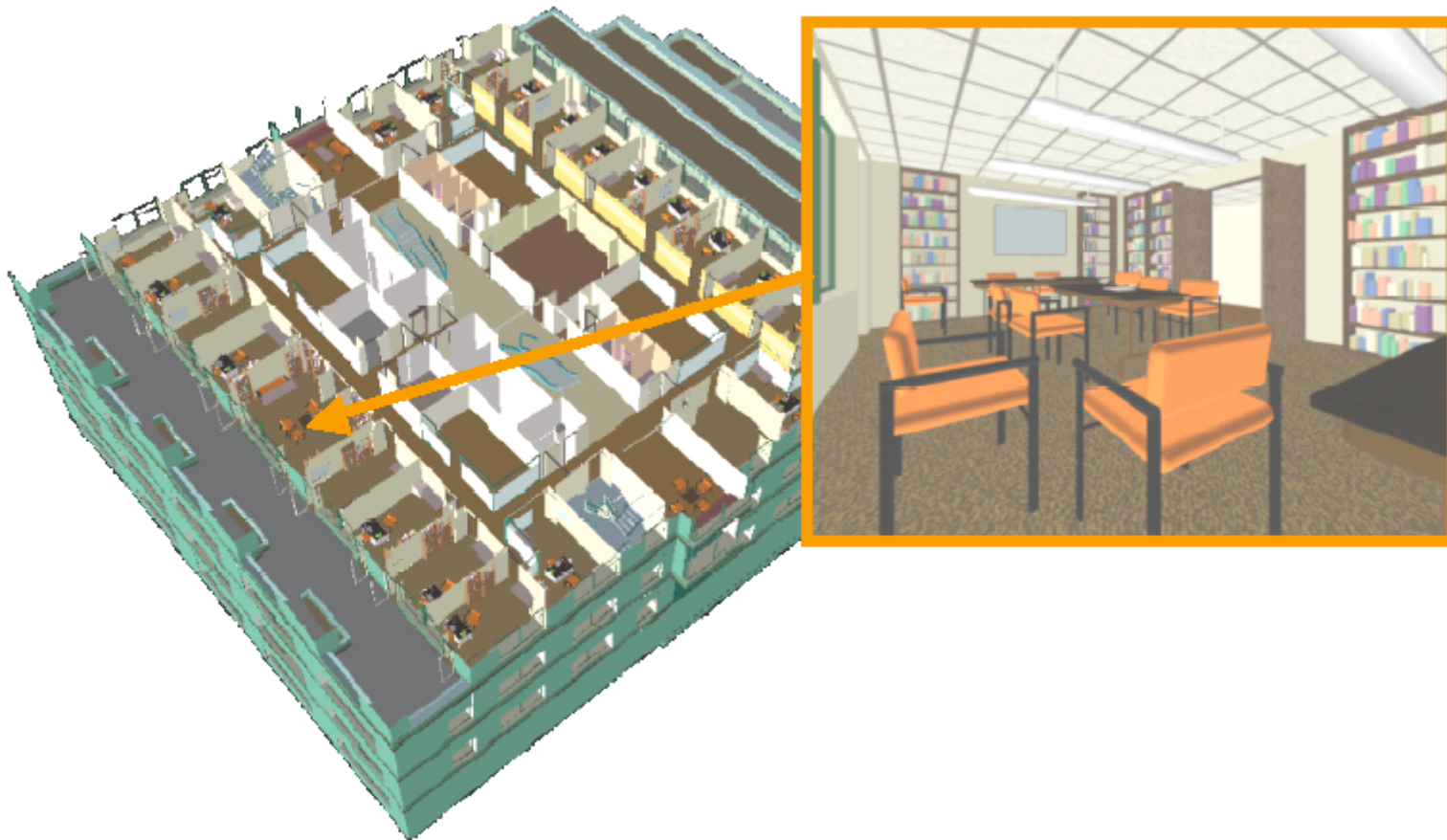


Transformation Hierarchy Example 1



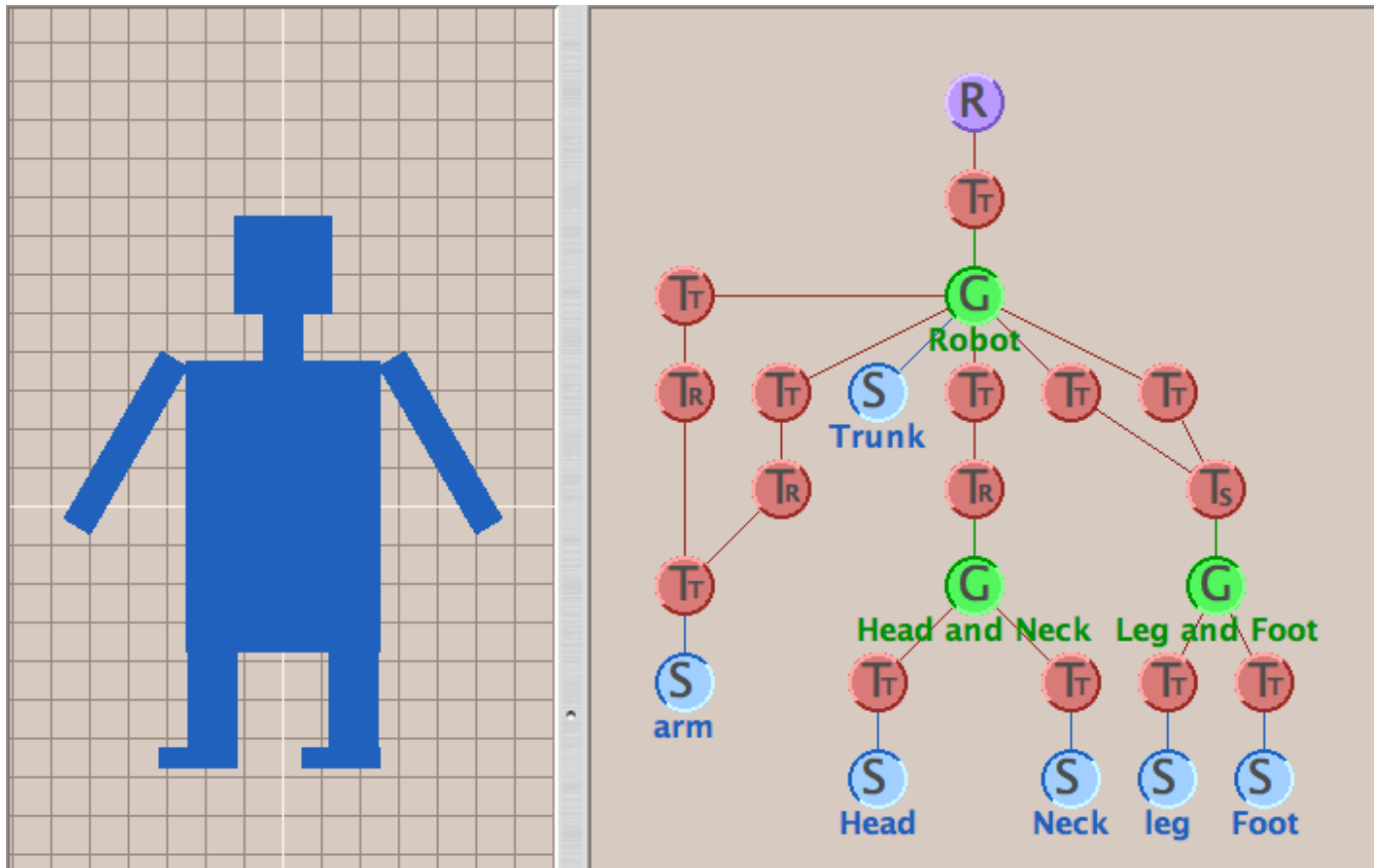
Transformation Hierarchy Example 2

- draw same 3D data with different transformations: instancing



Transformation Hierarchies Demo

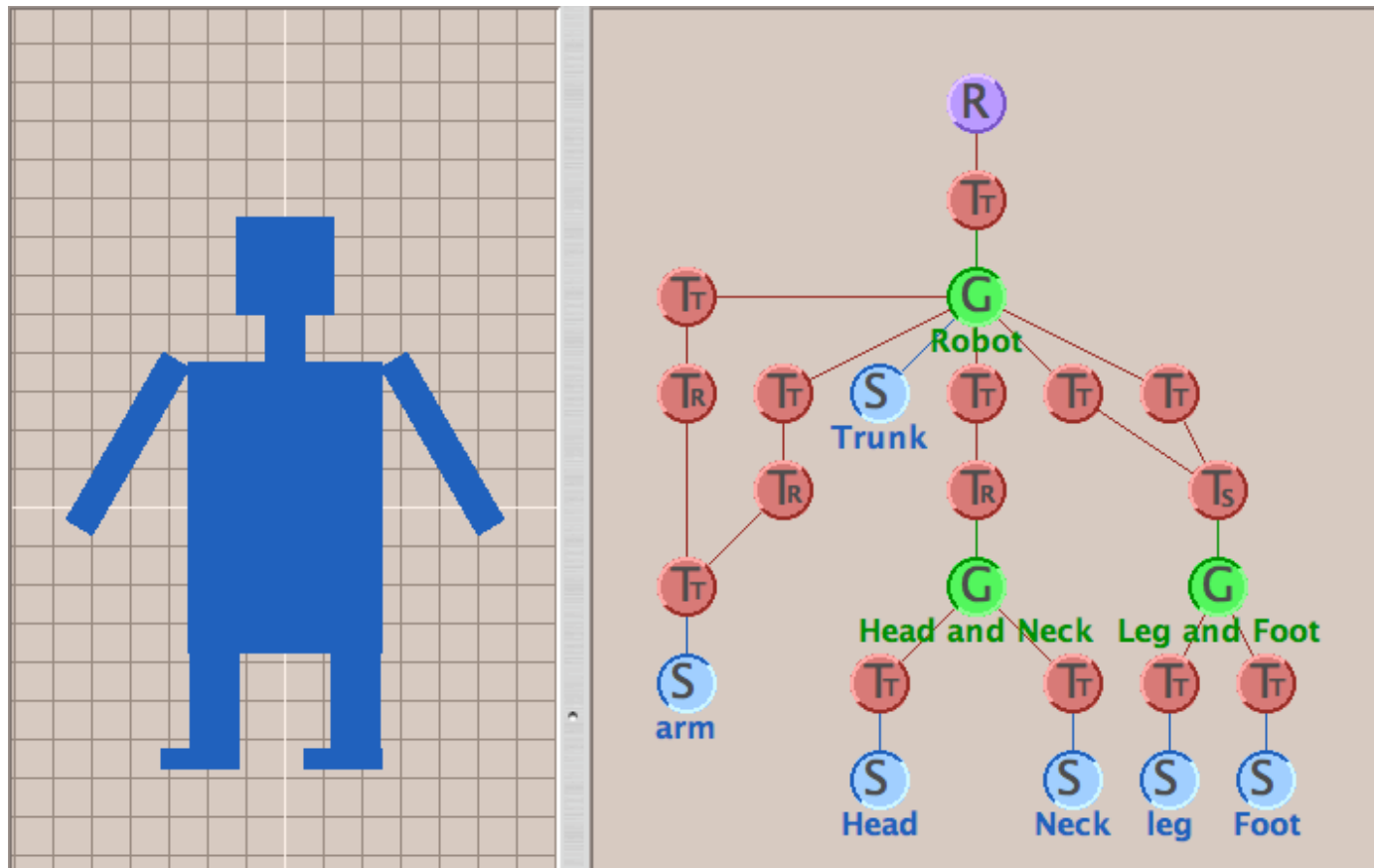
- transforms apply to graph nodes beneath



<http://www.cs.brown.edu/exploratories/freeSoftware/catalogs/scenegraphs.html>

Transformation Hierarchies Demo

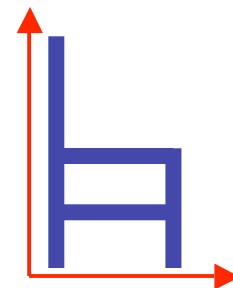
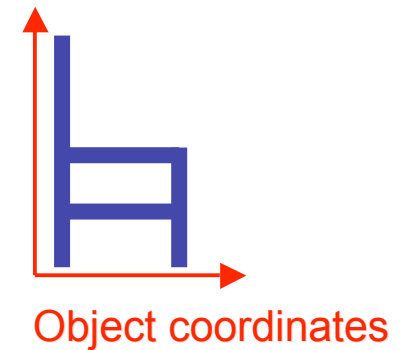
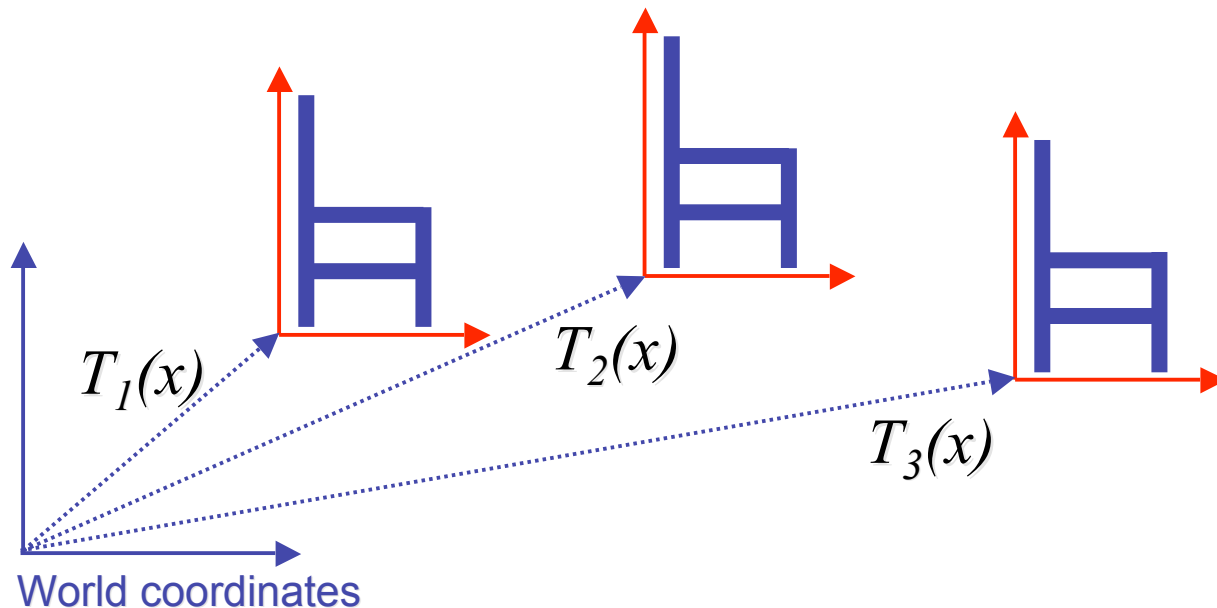
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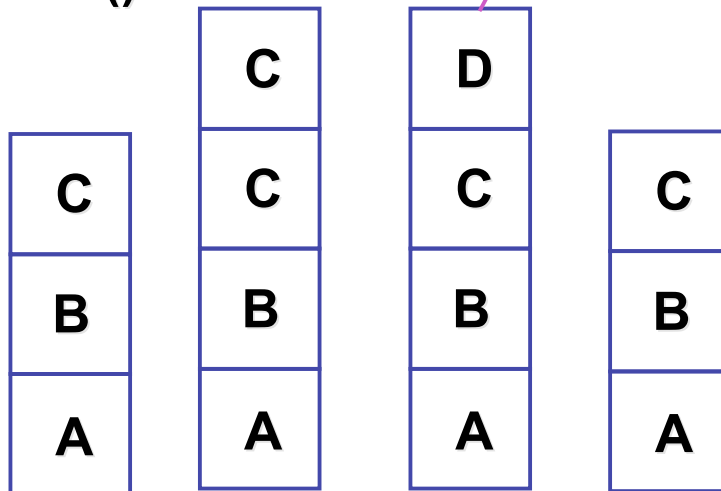
Matrix Stacks

- challenge of avoiding unnecessary computation
 - using inverse to return to origin
 - computing incremental $T_1 \rightarrow T_2$



Matrix Stacks

**glPushMatrix()
glPopMatrix()**



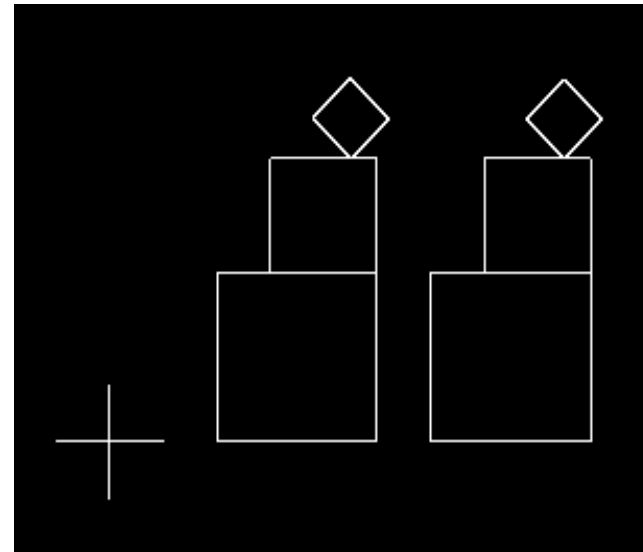
D = C scale(2,2,2) trans(1,0,0)

**DrawSquare()
glPushMatrix()
glScale3f(2,2,2)
glTranslate3f(1,0,0)
DrawSquare()
glPopMatrix()**

Modularization

- drawing a scaled square
 - push/pop ensures no coord system change

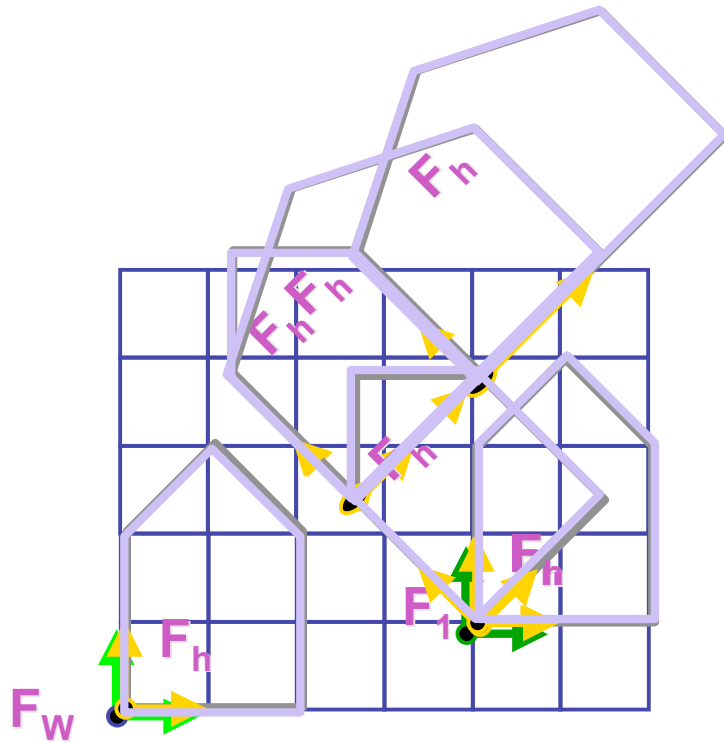
```
void drawBlock(float k) {  
    glPushMatrix();  
  
    glScalef(k,k,k);  
    glBegin(GL_LINE_LOOP);  
    glVertex3f(0,0,0);  
    glVertex3f(1,0,0);  
    glVertex3f(1,1,0);  
    glVertex3f(0,1,0);  
    glEnd();  
  
    glPopMatrix();  
}
```



Matrix Stacks

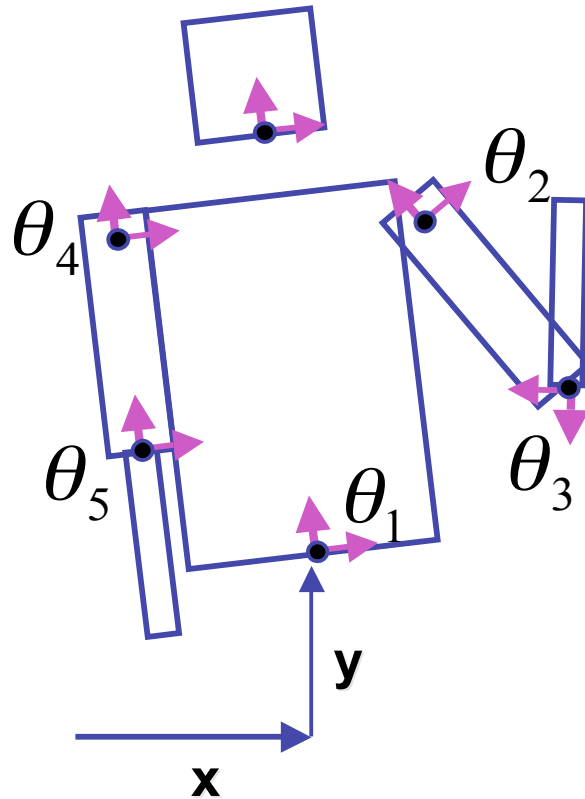
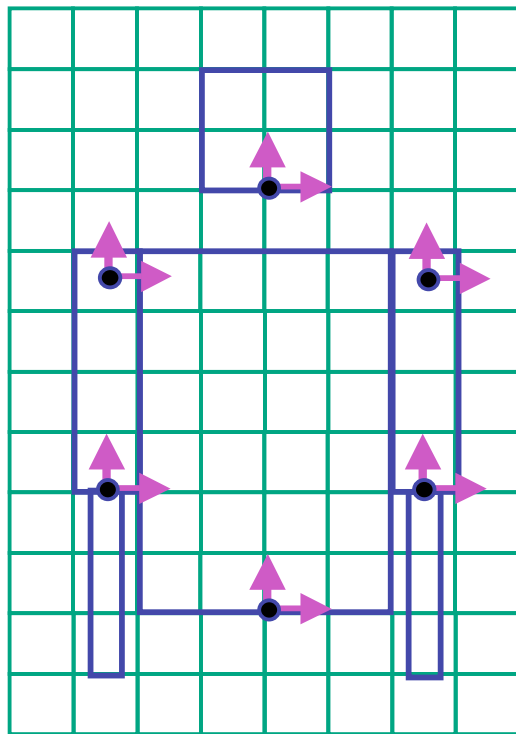
- advantages
 - no need to compute inverse matrices all the time
 - modularize changes to pipeline state
 - avoids incremental changes to coordinate systems
 - accumulation of numerical errors
- practical issues
 - in graphics hardware, depth of matrix stacks is limited
 - (typically 16 for model/view and about 4 for projective matrix)

Transformation Hierarchy Example 3



```
glLoadIdentity();  
glTranslatef(4,1,0);  
glPushMatrix();  
glRotatef(45,0,0,1);  
glTranslatef(0,2,0);  
glScalef(2,1,1);  
glTranslate(1,0,0);  
glPopMatrix();
```

Transformation Hierarchy Example 4



```

glTranslate3f(x,y,0);
glRotatef( $\theta_1$ ,0,0,1);
DrawBody();
glPushMatrix();
    glTranslate3f(0,7,0);
    DrawHead();
glPopMatrix();
glPushMatrix();
    glTranslate(2.5,5.5,0);
    glRotatef( $\theta_2$ ,0,0,1);
    DrawUArm();
    glTranslate(0,-3.5,0);
    glRotatef( $\theta_3$ ,0,0,1);
    DrawLArm();
glPopMatrix();
... (draw other arm)

```

Hierarchical Modelling

- advantages
 - define object once, instantiate multiple copies
 - transformation parameters often good control knobs
 - maintain structural constraints if well-designed
- limitations
 - expressivity: not always the best controls
 - can't do closed kinematic chains
 - keep hand on hip
 - can't do other constraints
 - collision detection
 - self-intersection
 - walk through walls