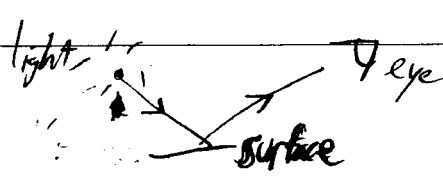


Phong Lighting Model



local illumination
(one³ bounce)

$$I = \underbrace{I_a k_a}_{\text{ambient}} + \sum_L \underbrace{I_L k_d (\vec{N} \cdot \vec{L})}_{\text{diffuse}} + \underbrace{I_L k_s (\vec{R} \cdot \vec{V})^n}_{\text{specular}}$$

lights: I_a, I_L
surface: k_a, k_d, k_s

Suppose we want: white light, shiny yellow material

geom: N, L, R, V

$$\begin{bmatrix} I_r \\ I_g \\ I_b \end{bmatrix} = \begin{bmatrix} 0.2 \\ 0.2 \\ 0.2 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} (\vec{N} \cdot \vec{L}) + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} (\vec{R} \cdot \vec{V})^{50}$$

ensure $\vec{N} \cdot \vec{L} \geq 0$, i.e., use $\max(0, \vec{N} \cdot \vec{L})$
ensure $\vec{R} \cdot \vec{V} \geq 0$, i.e., use $\max(0, \vec{R} \cdot \vec{V})$

+ basic demos of Phong illumination on a teapot.
WebGL

Q: What is the colour of the darkest pixel on a rendered sphere?

occurs when $N \cdot L = 0$, only left with ambient light, $I = \begin{bmatrix} 0.12 \\ 0.12 \\ 0 \end{bmatrix}$
when $R \cdot V = 0$

Q: What is the colour of the brightest pixel on a rendered sphere?

occurs when $N \cdot L = 1$
when $R \cdot V = 1$

$$I = \begin{bmatrix} 0.12 \\ 0.12 \\ 0 \end{bmatrix} + \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} + \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} = \begin{bmatrix} 1.22 \\ 1.22 \\ 0 \end{bmatrix} \xrightarrow{\text{clamp to 1}} \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$$

Q: What would we see when the yellow surface is illuminated with a blue light?

black

$$I = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} 0.2 \\ 0.2 \\ 0 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} (N \cdot L) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} (R \cdot V)^{50} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

yellow surface absorbs blue light

Q: What would be seen with a red light?

$$\begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0.2 \\ 0.2 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} (N \cdot L) + \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} (R \cdot V)^{50} = \begin{bmatrix} 0 \dots 1 \\ 0 \\ 0 \end{bmatrix}$$

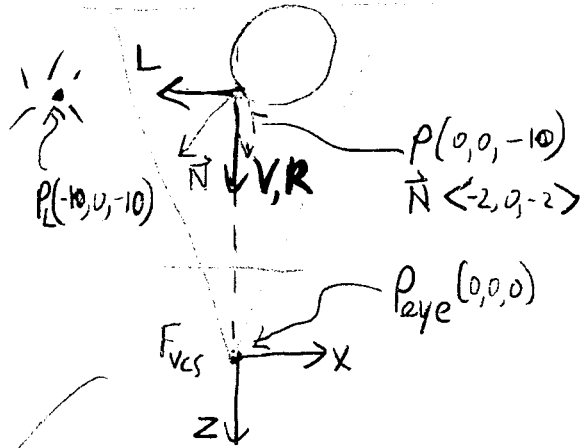
Q: Do specular highlights have the colour of the light or the surface?

⇒ Usually the colour of light

i.e., commonly use $k_s = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix}$

Need $\hat{N}, \hat{L}, \hat{R}, \hat{V}$

Q: What is the rendered colour for point P , as shown below? ⁵



$$\hat{N} = \frac{N}{\|N\|} = \frac{1}{\sqrt{8}} \langle -2, 0, -2 \rangle$$

$$\hat{L} = \frac{L}{\|L\|} = \frac{1}{10} \langle -10, 0, 0 \rangle$$

$$\hat{V} = \frac{V}{\|V\|} = \frac{1}{10} \langle -10, 0, 0 \rangle$$

$$\hat{V} = \frac{V}{\|V\|} = \frac{1}{10} \langle -10, 0, 0 \rangle$$

$$\hat{V} = \langle 0, 0, 1 \rangle$$

$$\hat{R} = 2\hat{N}(\hat{N} \cdot \hat{L}) - \hat{L} \quad (\text{see notes})$$

$$= \langle 0, 0, 1 \rangle$$

lighting computations done in VCS

$$I = f(\dots)$$

$$\hat{N} \cdot \hat{L} = \frac{1}{\sqrt{2}} \approx 0.7$$

$$\hat{R} \cdot \hat{V} = 1$$

$$I = \begin{bmatrix} 0.2 \\ 0.7 \\ 0.2 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0.6 \\ 0.6 \\ 0 \end{bmatrix} (0.7) + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} (1)$$

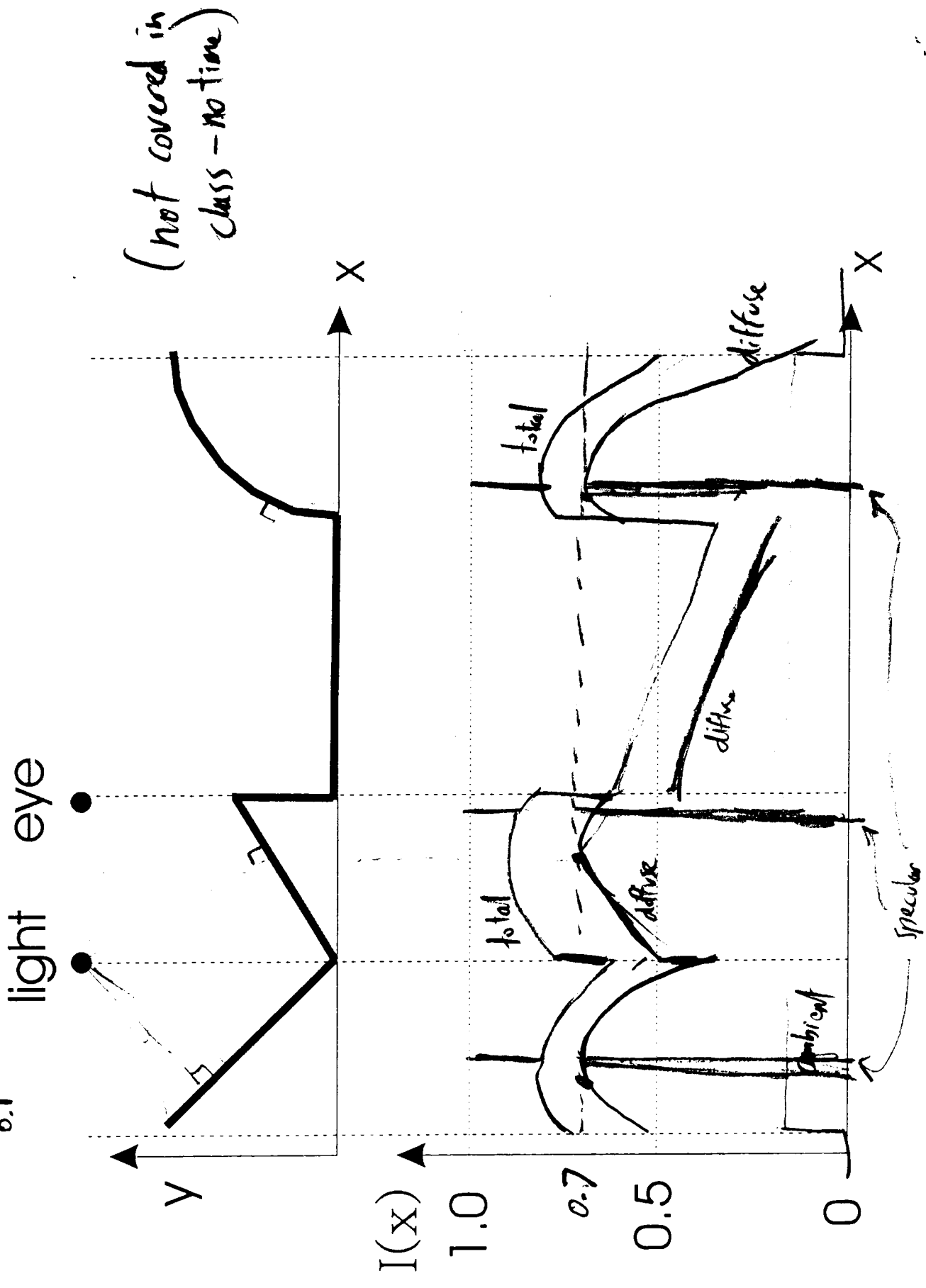
$$= \begin{bmatrix} 0.12 \\ 0.12 \\ 0 \end{bmatrix} + \begin{bmatrix} 0.42 \\ 0.42 \\ 0 \end{bmatrix} + \begin{bmatrix} 0.5 \\ 0.5 \\ 0 \end{bmatrix} = \begin{bmatrix} 1.04 \\ 1.04 \\ 0 \end{bmatrix} \Rightarrow \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix}$$

Sketch the ambient, diffuse, specular, and total illumination for the following scene as a function of x . Assume the Phong illumination model,

For a grey-scale world, ~~to~~
i.e., $k_r = k_g = k_b$

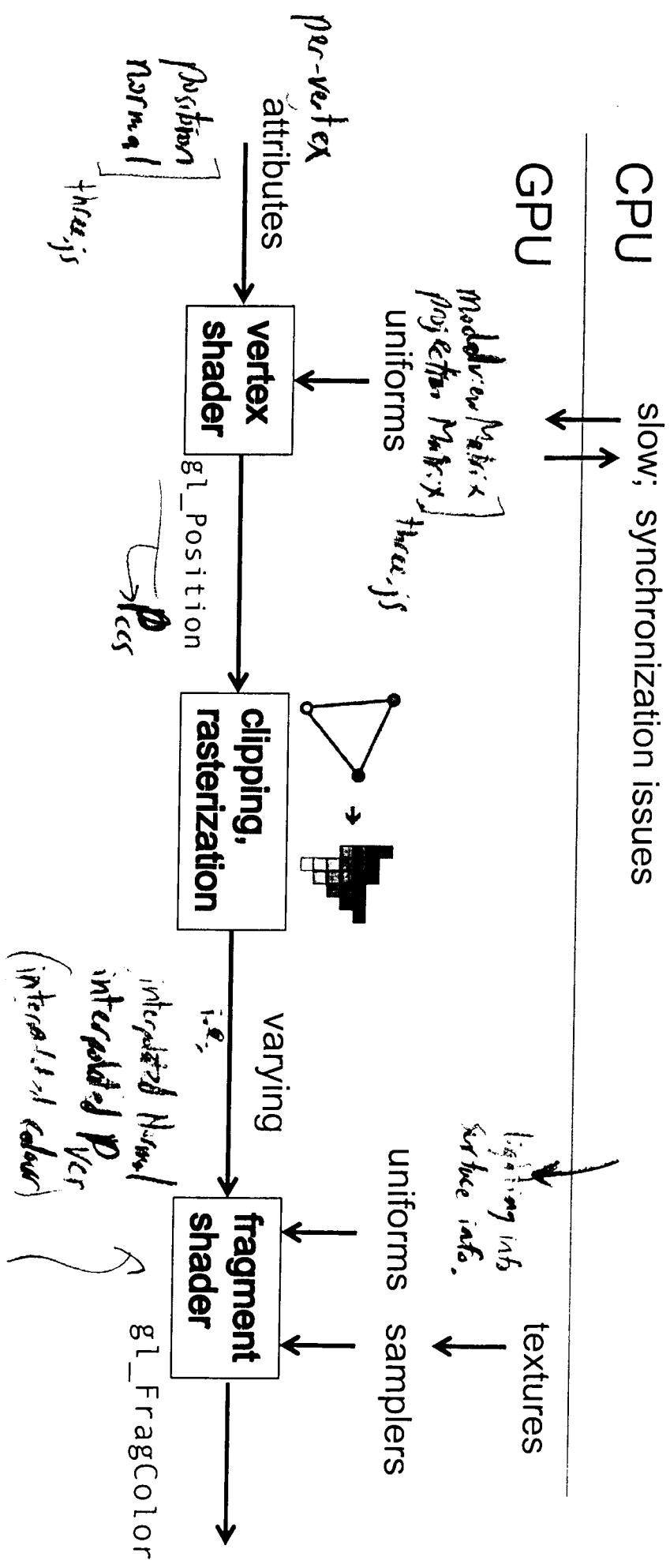
$$I = k_a I_a + k_d I_d(N \cdot L) + k_s I_s (R \cdot V)^n,$$

where $k_a = 0.1$, $k_d = 0.7$, $k_s = 0.7$, $I_a = I_d = I_s = 1.0$, $n = 100$.



(began with a quick shader toy demo)

Shader Overview



+ live coding demo of three.js, building a shader that renders N.L as a gray-scale colour, i.e. basic diffuse illumination.

$$I_a k_a + I_L k_d (N \cdot L) + I_L k_s R \cdot 1$$

THREE.JS Built-in uniforms and attributes for GL_SL shaders

VERTEX SHADER

```
uniform mat4 modelMatrix;           // = object.matrixWorld
uniform mat4 modelViewMatrix;       // = camera.matrixWorldInverse * object.matrixWorld
uniform mat4 projectionMatrix;      // = camera.projectionMatrix
uniform mat4 viewMatrix;            // = camera.matrixWorldInverse
uniform mat3 normalMatrix;          // = inverse transpose of modelViewMatrix
uniform vec3 cameraPosition;        // = camera position in world space

attribute vec3 position;            // vertex position
attribute vec3 normal;              // vertex normal
attribute vec2 uv;                  // texture coordinate
attribute vec2 uv2;                 // texture coordinate
```

The vertex shader should always output:

- `gl_Position` This is a `vec4` that gives the vertex coord after projection
- any "varying" variables you wish to have interpolated and passed on to the fragment shader

Note that you can therefore calculate the position of a vertex in the vertex shader by either:

```
gl_Position = projectionMatrix * modelViewMatrix * vec4( position, 1.0 );
gl_Position = projectionMatrix * viewMatrix * modelMatrix * vec4( position, 1.0 );
```

FRAGMENT SHADER

```
uniform mat4 viewMatrix;            // = camera.matrixWorldInverse
uniform vec3 cameraPosition;        // = camera position in world space
```

The fragment shader should also declare any "varying" variables that it will receive as input

The fragment shader should always output:

- `gl_FragColor` This is a `vec4` that describes the desired "fragment" or pixel color